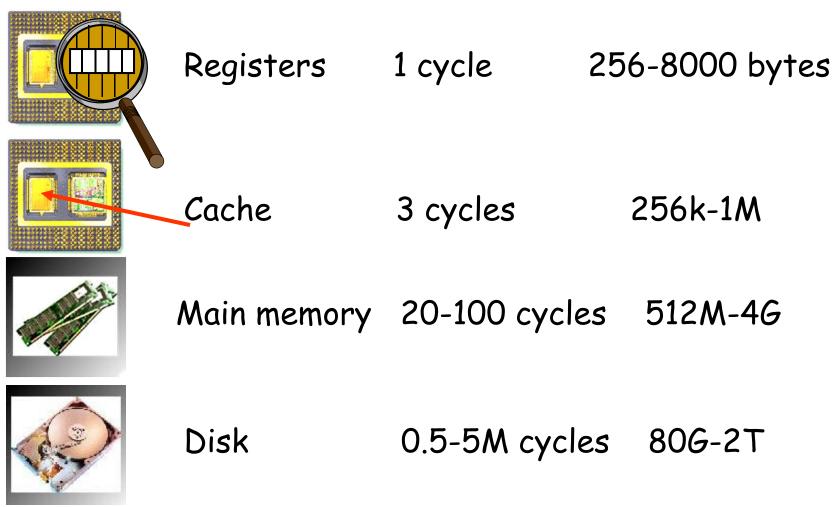
Register Allocation

Lecture 16

Lecture Outline

- Memory Hierarchy Management
- Register Allocation
 - Register interference graph
 - Graph coloring heuristics
 - Spilling
- Cache Management

The Memory Hierarchy



Managing the Memory Hierarchy

- Most programs are written as if there are only two kinds of memory: main memory and disk
 - Programmer is responsible for moving data from disk to memory (e.g., file I/O)
 - Hardware is responsible for moving data between memory and caches
 - Compiler is responsible for moving data between memory and registers

Current Trends

- Power usage limits
 - Size and speed of registers/caches
 - Speed of processors
- But
 - The cost of a cache miss is very high
 - Typically requires 2-3 caches to bridge fast processor with large main memory
- It is very important to:
 - Manage registers properly
 - Manage caches properly
- Compilers are good at managing registers

The Register Allocation Problem

- Intermediate code uses unlimited temporaries
 - Simplifies code generation and optimization
 - Complicates final translation to assembly
- Typical intermediate code uses too many temporaries

The Register Allocation Problem (Cont.)

The problem:

Rewrite the intermediate code to use no more temporaries than there are machine registers

· Method:

- Assign multiple temporaries to each register
- But without changing the program behavior

History

- Register allocation is as old as compilers
 - Register allocation was used in the original FORTRAN compiler in the '50s
 - Very crude algorithms
- A breakthrough came in 1980
 - Register allocation scheme based on graph coloring
 - Relatively simple, global and works well in practice

An Example

Consider the program

$$a := c + d$$

 $e := a + b$
 $f := e - 1$

 Can allocate a, e, and f all to one register (r₁):

$$r_1 := r_2 + r_3$$

 $r_1 := r_1 + r_4$
 $r_1 := r_1 - 1$

- Assume a and e dead after use
 - Temporary a can be "reused" after e := a + b
 - So can temporary e

- A dead temporary is not needed
 - A dead temporary can be reused

The Idea

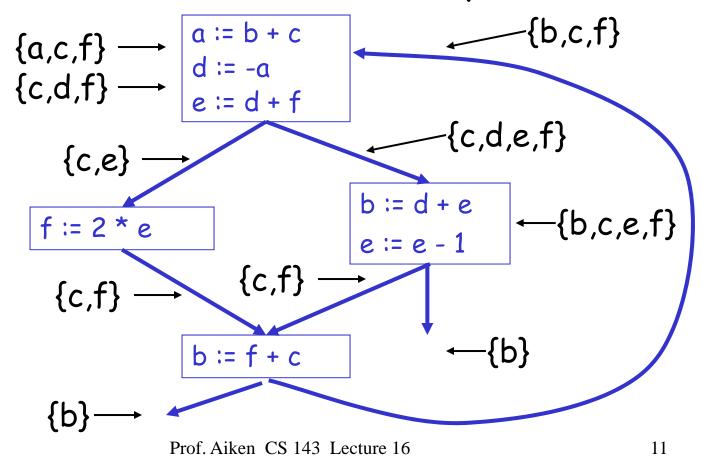
Temporaries t_1 and t_2 can share the same register if at any point in the program at most one of t_1 or t_2 is live.

Or

If t_1 and t_2 are live at the same time, they cannot share a register

Algorithm: Part I

· Compute live variables for each point:

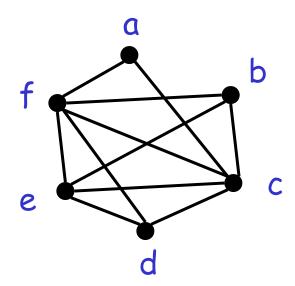


The Register Interference Graph

- Construct an undirected graph
 - A node for each temporary
 - An edge between t_1 and t_2 if they are live simultaneously at some point in the program
- · This is the register interference graph (RIG)
 - Two temporaries can be allocated to the same register if there is no edge connecting them

Example

For our example:



- E.g., b and c cannot be in the same register
- E.g., b and d could be in the same register

Notes on Register Interference Graphs

- Extracts exactly the information needed to characterize legal register assignments
- Gives a global (i.e., over the entire flow graph) picture of the register requirements
- After RIG construction the register allocation algorithm is architecture independent

Definitions

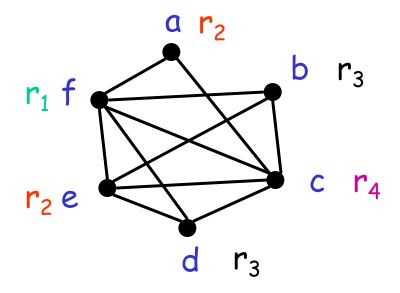
- A <u>coloring of a graph</u> is an assignment of colors to nodes, such that nodes connected by an edge have different colors
- A graph is k-colorable if it has a coloring with k colors

Register Allocation Through Graph Coloring

- In our problem, colors = registers
 - We need to assign colors (registers) to graph nodes (temporaries)
- Let k = number of machine registers
- If the RIG is k-colorable then there is a register assignment that uses no more than k registers

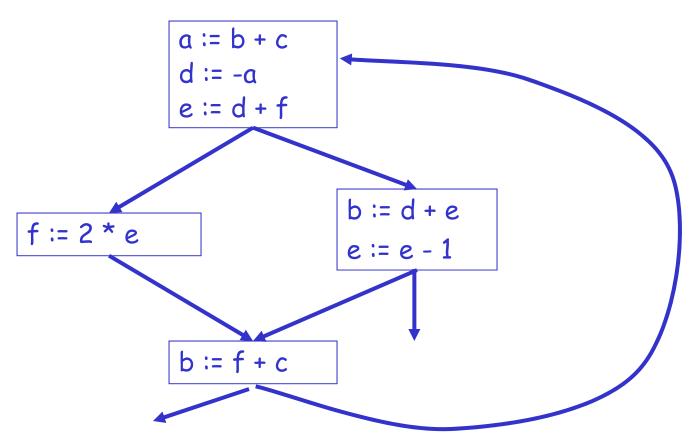
Graph Coloring Example

Consider the example RIG



- There is no coloring with less than 4 colors
- There are 4-colorings of this graph

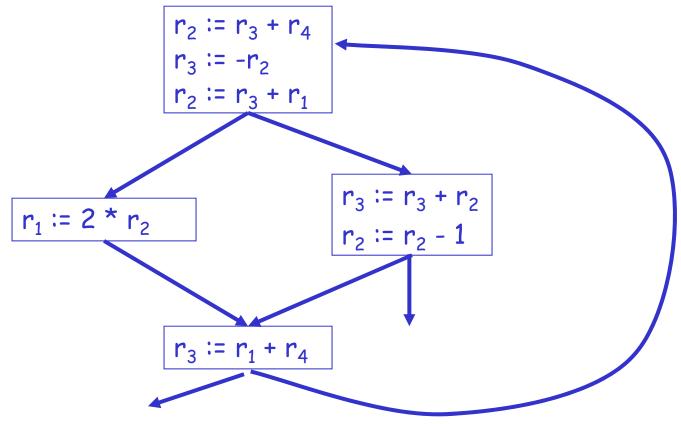
Example Review



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Example After Register Allocation

Under this coloring the code becomes:



Computing Graph Colorings

- How do we compute graph colorings?
- It isn't easy:
 - 1. This problem is very hard (NP-hard). No efficient algorithms are known.
 - Solution: use heuristics
 - 2. A coloring might not exist for a given number of registers
 - Solution: later

Graph Coloring Heuristic

Observation:

- Pick a node t with fewer than k neighbors in RIG
- Eliminate t and its edges from RIG
- If resulting graph is k-colorable, then so is the original graph

· Why?

- Let $c_1,...,c_n$ be the colors assigned to the neighbors of t in the reduced graph
- Since n < k we can pick some color for t that is different from those of its neighbors

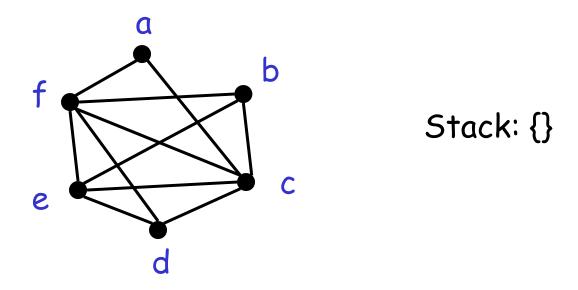
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Graph Coloring Heuristic

- The following works well in practice:
 - Pick a node t with fewer than k neighbors
 - Put t on a stack and remove it from the RIG
 - Repeat until the graph has one node
- Assign colors to nodes on the stack
 - Start with the last node added
 - At each step pick a color different from those assigned to already colored neighbors

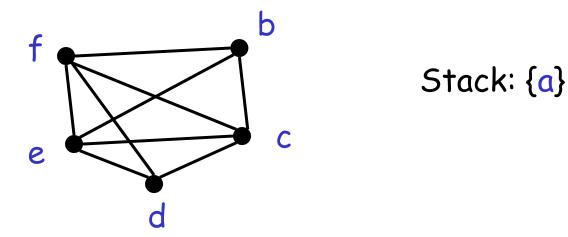
Graph Coloring Example (1)

• Start with the RIG and with k = 4:



· Remove a

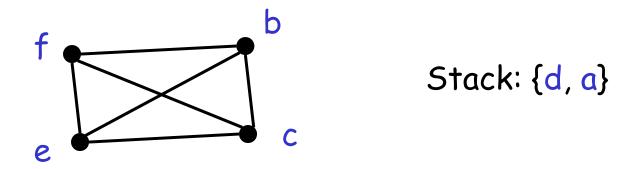
Graph Coloring Example (2)



· Remove d

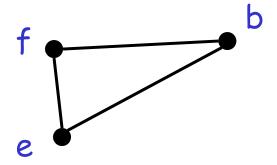
Graph Coloring Example (3)

Note: all nodes now have fewer than 4 neighbors



· Remove c

Graph Coloring Example (4)



Stack: {c, d, a}

· Remove b

Graph Coloring Example (5)



Stack: {b, c, d, a}

· Remove e

Graph Coloring Example (6)

f

Stack: {e, b, c, d, a}

· Remove f

Graph Coloring Example (7)

 Now start assigning colors to nodes, starting with the top of the stack

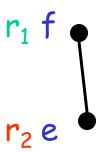
Stack: {f, e, b, c, d, a}

Graph Coloring Example (8)

$$r_1 f \bullet$$

Stack: {e, b, c, d, a}

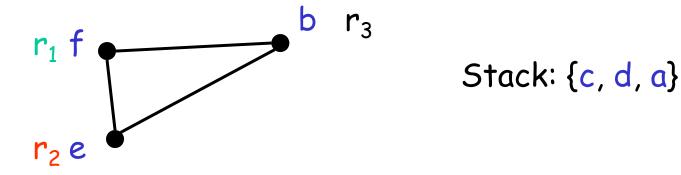
Graph Coloring Example (9)



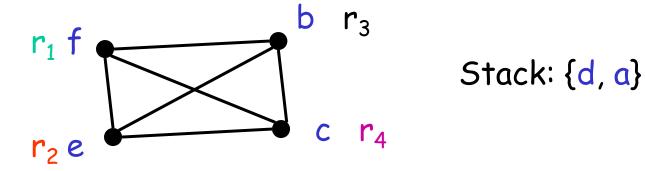
Stack: {b, c, d, a}

· e must be in a different register from f

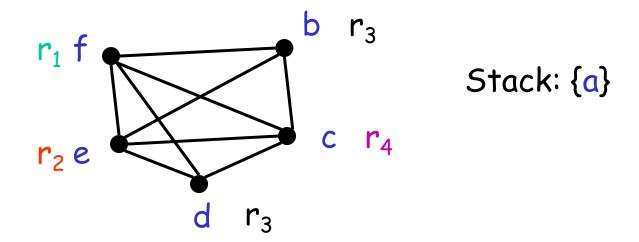
Graph Coloring Example (10)



Graph Coloring Example (11)

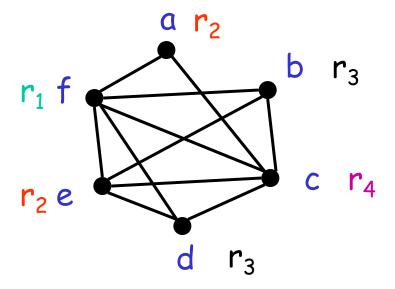


Graph Coloring Example (12)



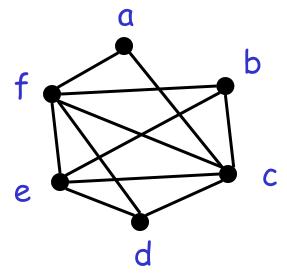
d can be in the same register as b

Graph Coloring Example (13)



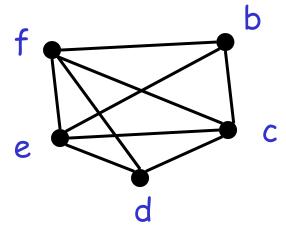
What if the Heuristic Fails?

- What if all nodes have k or more neighbors?
- Example: Try to find a 3-coloring of the RIG:



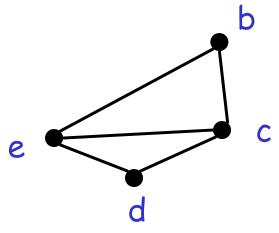
What if the Heuristic Fails?

- Remove a and get stuck (as shown below)
- · Pick a node as a candidate for spilling
 - A spilled temporary "lives" in memory
 - Assume that f is picked as a candidate



What if the Heuristic Fails?

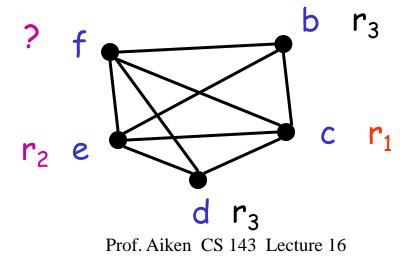
- Remove f and continue the simplification
 - Simplification now succeeds: b, d, e, c



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What if the Heuristic Fails?

- Eventually we must assign a color to f
- We hope that among the 4 neighbors of f we use less than 3 colors \Rightarrow optimistic coloring

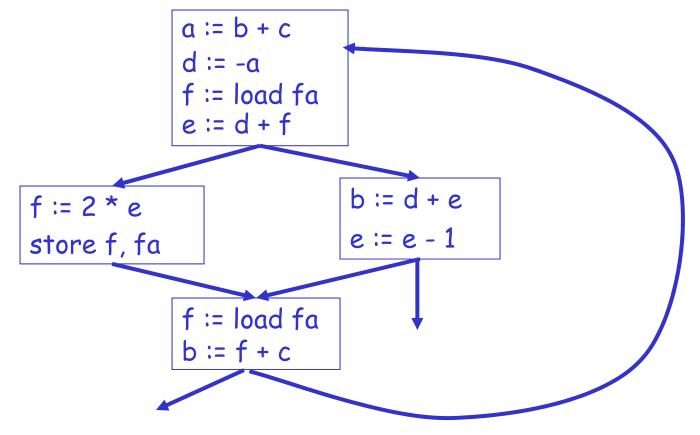


Spilling

- · If optimistic coloring fails, we spill f
 - Allocate a memory location for f
 - Typically in the current stack frame
 - · Call this address fa
- Before each operation that reads f, insert
 f := load fa
- After each operation that writes f, insert store f, fa

Spilling Example

This is the new code after spilling f

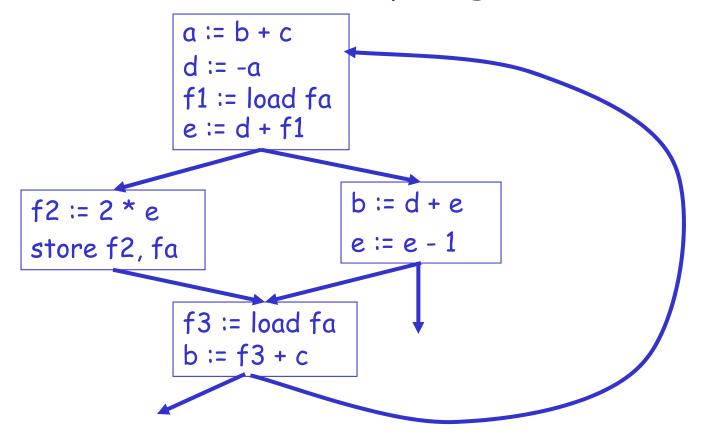


A Problem

- This code reuses the register name f
- · Correct, but suboptimal
 - Should use distinct register names whenever possible
 - Allows different uses to have different colors

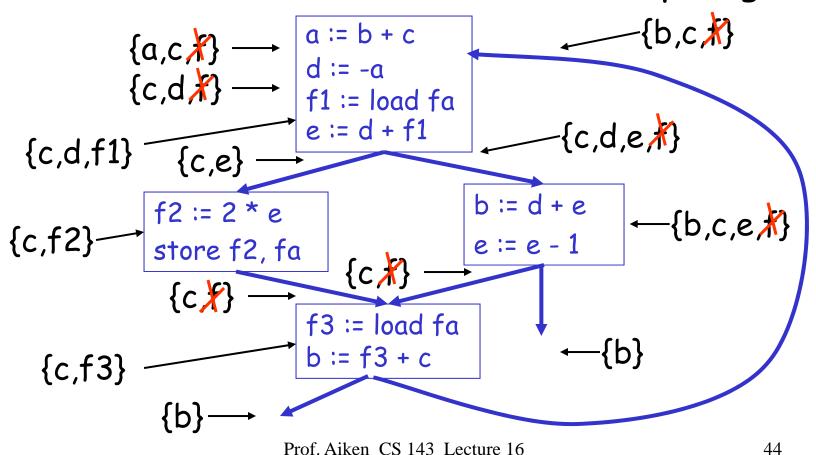
Spilling Example

This is the new code after spilling f



Recomputing Liveness Information

The new liveness information after spilling:

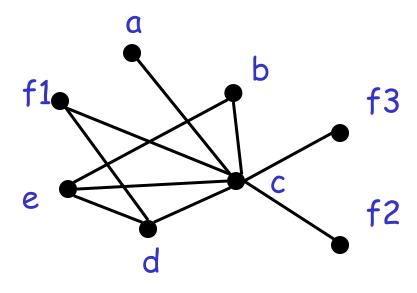


Recomputing Liveness Information

- New liveness information is almost as before
 - Note f has been split into three temporaries
- fi is live only
 - Between a fi := load fa and the next instruction
 - Between a store fi, fa and the preceding instr.
- Spilling reduces the live range of f
 - And thus reduces its interferences
 - Which results in fewer RIG neighbors
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Recompute RIG After Spilling

- Some edges of the spilled node are removed
- In our case f still interferes only with c and d
- And the resulting RIG is 3-colorable



Spilling Notes

- Additional spills might be required before a coloring is found
- The tricky part is deciding what to spill
 - But any choice is correct
- Possible heuristics:
 - Spill temporaries with most conflicts
 - Spill temporaries with few definitions and uses
 - Avoid spilling in inner loops

Caches

- · Compilers are very good at managing registers
 - Much better than a programmer could be
- · Compilers are not good at managing caches
 - This problem is still left to programmers
 - It is still an open question how much a compiler can do to improve cache performance
- Compilers can, and a few do, perform some cache optimizations

Cache Optimization

Consider the loop

```
for(j := 1; j < 10; j++)
for(i=1; i<1000; i++)
a[i] *= b[i]
```

- This program has terrible cache performance
 - · Why?

Cache Optimization (Cont.)

· Consider the program:

```
for(i=1; i<1000; i++)
for(j := 1; j < 10; j++)
a[i] *= b[i]
```

- Computes the same thing
- But with much better cache behavior
- Might actually be more than 10x faster
- · A compiler can perform this optimization
 - called loop interchange

Conclusions

- Register allocation is a "must have" in compilers:
 - Because intermediate code uses too many temporaries
 - Because it makes a big difference in performance
- Register allocation is more complicated for CISC machines