

ප්‍රතිකර්මණ අභ්‍යාසය

සුළු කරන්න.

a. $\frac{a}{5} + \frac{2a}{5}$

b. $\frac{8}{x} - \frac{3}{x}$

c. $\frac{7}{3m} + \frac{3}{4m} - \frac{8}{m}$

d. $\frac{9}{x+2} + \frac{1}{x}$

e. $\frac{1}{m+2} - \frac{2}{m+3}$

f. $\frac{a+3}{a^2-4} + \frac{1}{a+2}$

g. $\frac{2}{x^2-x-2} - \frac{1}{x^2-1}$

h. $\frac{1}{x^2-9x+20} - \frac{1}{x^2-11x+30}$

$$\begin{aligned} \text{a. } & \frac{a}{5} + \frac{2a}{5} \\ &= \underline{\underline{\frac{3a}{5}}} \end{aligned}$$

$$\begin{aligned} \text{b. } & \frac{8}{x} - \frac{3}{x} \\ &= \underline{\underline{\frac{5}{x}}} \end{aligned}$$

$$\begin{aligned} \text{c. } & \frac{7}{3m} + \frac{3}{4m} - \frac{8}{m} \\ &= \frac{28}{12m} + \frac{9}{12m} - \frac{96}{12m} \\ &= \underline{\underline{-\frac{59}{12m}}} \end{aligned}$$

$$\begin{aligned} \text{d. } & \frac{9}{x+2} + \frac{1}{x} \\ &= \frac{9x+x+2}{x(x+2)} \\ &= \underline{\underline{\frac{10x+2}{x(x+2)}}} \end{aligned}$$

$$\begin{aligned} \text{e. } & \frac{1}{m+2} - \frac{2}{m+3} \\ &= \frac{(m+3) - 2(m+2)}{(m+2)(m+3)} \\ &= \frac{m+3-2m-4}{(m+2)(m+3)} \\ &= \frac{-m-1}{(m+2)(m+3)} \\ &= \underline{\underline{\frac{-(m+1)}{(m+2)(m+3)}}} \end{aligned}$$

$$\begin{aligned} \text{f. } & \frac{a+3}{a^2-4} + \frac{1}{a+2} \\ &= \frac{a+3}{(a-2)(a+2)} + \frac{1}{a+2} \\ &= \frac{a+3+a-2}{(a-2)(a+2)} \\ &= \frac{2a+1}{(a-2)(a+2)} // \\ &= \underline{\underline{\frac{2a+1}{a^2-4}}} \end{aligned}$$

$$\begin{aligned}
 \text{g. } & \frac{2}{x^2 - x - 2} - \frac{1}{x^2 - 1} \\
 &= \frac{2}{(x-2)(x+1)} - \frac{1}{(x-1)(x+1)} \\
 &= \frac{2(x-1) - (x-2)}{(x-2)(x+1)(x-1)} \\
 &= \frac{2x - 2 - x + 2}{(x-2)(x+1)(x-1)} \\
 &= \frac{x}{(x-2)(x+1)(x-1)}
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - x - 2 \\
 &= x^2 - 2x + x - 2 \\
 &= x(x-2) + 1(x-2) \\
 &= (x-2)(x+1)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 1 \\
 &= (x-1)(x+1)
 \end{aligned}$$

$$\begin{aligned}
 \text{h. } & \frac{1}{x^2 - 9x + 20} - \frac{1}{x^2 - 11x + 30} \\
 &= \frac{1}{(x-4)(x-5)} - \frac{1}{(x-5)(x-6)} \\
 &= \frac{(x-6) - (x-4)}{(x-4)(x-5)(x-6)} \\
 &= \frac{x-6-x+4}{(x-4)(x-5)(x-6)} \\
 &= \frac{-2}{(x-4)(x-5)(x-6)}
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 9x + 20 \\
 &= x^2 - 4x - 5x + 20 \\
 &= x(x-4) - 5(x-4) \\
 &= (x-4)(x-5)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 11x + 30 \\
 &= x^2 - 5x - 6x + 30 \\
 &= x(x-5) - 6(x-5) \\
 &= (x-5)(x-6)
 \end{aligned}$$

7.1 අභ්‍යාසය

පහත දැක්වෙන විජීය භාග සුළු කරන්න.

$$\text{a. } \frac{6}{x} \times \frac{2}{3x}$$

$$\text{b. } \frac{x}{5} \times \frac{3}{xy}$$

$$\text{c. } \frac{2a}{15} \times \frac{5}{9}$$

$$\text{d. } \frac{4m}{5n} \times \frac{3}{2m}$$

$$\text{e. } \frac{x+1}{8} \times \frac{2x}{x+1}$$

$$\text{f. } \frac{3a-6}{3a} \times \frac{1}{a-2}$$

$$\text{g. } \frac{x^2}{2y+5} \times \frac{4y+10}{3x}$$

$$\text{h. } \frac{m^2-4}{m+1} \times \frac{m^2+2m+1}{m+2}$$

$$\text{i. } \frac{x^2-5x+6}{x^2-1} \times \frac{x^2-2x-3}{x^2-9}$$

$$\text{j. } \frac{a^2-b^2}{a^2-2ab+b^2} \times \frac{2a-2b}{a^2+ab}$$

$$\begin{aligned} \text{a. } & \frac{\cancel{6}^2}{x} \times \frac{2}{\cancel{3}x} \\ &= \frac{4}{x^2} \end{aligned}$$

$$\begin{aligned} \text{b. } & \frac{\cancel{x}}{5} \times \frac{3}{\cancel{xy}} \\ &= \frac{3}{5y} \end{aligned}$$

$$\begin{aligned} \text{c. } & \frac{2a}{\cancel{15}_3} \times \frac{\cancel{5}}{9} \\ &= \frac{2a}{27} \end{aligned}$$

$$\begin{aligned} \text{d. } & \frac{\cancel{4}^2m}{5n} \times \frac{3}{\cancel{2}m} \\ &= \frac{6}{5n} \end{aligned}$$

$$\begin{aligned} \text{e. } & \frac{\cancel{x+1}_4}{8} \times \frac{\cancel{2x}}{\cancel{x+1}} \\ &= \frac{x}{4} \end{aligned}$$

$$\begin{aligned} \text{f. } & \frac{3a-6}{3a} \times \frac{1}{a-2} \\ &= \frac{\cancel{3(a-2)}}{\cancel{3}a} \times \frac{1}{\cancel{a-2}} \\ &= \frac{1}{a} \end{aligned}$$

$$\begin{aligned} \text{g. } & \frac{x^2}{2y+5} \times \frac{4y+10}{3x} \\ &= \frac{\cancel{x}^2 \cancel{x}}{\cancel{2}y+5} \times \frac{2(\cancel{2}y+5)}{\cancel{3}x} \\ &= \frac{2x}{3} \end{aligned}$$

$$\begin{aligned} \text{h. } & \frac{m^2-4}{m+1} \times \frac{m^2+2m+1}{m+2} \\ &= \frac{(m-2)(\cancel{m+2})}{\cancel{m+1}} \times \frac{(m+1)(\cancel{m+1})}{\cancel{m+2}} \\ &= \underline{\underline{(m-2)(m+1)}} \end{aligned}$$

$$\begin{aligned} \text{i. } & \frac{x^2-5x+6}{x^2-1} \times \frac{x^2-2x-3}{x^2-9} \\ &= \frac{(x-2)(x-3)}{(x-1)(\cancel{x+1})} \times \frac{(\cancel{x-3})(x+1)}{(\cancel{x-3})(x+3)} \\ &= \frac{(x-2)(x-3)}{(x-1)(x+3)} \end{aligned}$$

$$\begin{aligned} & x^2-2x-3 \\ &= x^2-3x+x-3 \\ &= x(x-3)+1(x-3) \\ &= (x-3)(x+1) \end{aligned}$$

$$\begin{aligned} \text{j. } & \frac{a^2-b^2}{a^2-2ab+b^2} \times \frac{2a-2b}{a^2+ab} \\ &= \frac{(\cancel{a-b})(\cancel{a+b})}{(\cancel{a-b})(\cancel{a-b})} \times \frac{2(\cancel{a-b})}{a(\cancel{a+b})} \\ &= \frac{2}{a} \end{aligned}$$

$$\begin{aligned} & a^2-2ab+b^2 \\ &= a^2-ab-ab+b^2 \\ &= a(a-b)-b(a-b) \\ &= (a-b)(a-b) \end{aligned}$$

7.2 අනුපාසය

පහත දැක්වෙන විෂය භාග සුළු කරන්න.

a. $\frac{5}{x} \div \frac{10}{x}$

b. $\frac{m}{3n} \div \frac{m}{2n^2}$

c. $\frac{x+1}{y} \div \frac{2(x+1)}{x}$

d. $\frac{2a-4}{2a} \div \frac{a-2}{3}$

e. $\frac{x^2+4x}{3y} \div \frac{x^2-16}{12y^2}$

f. $\frac{p^2+pq}{p^2-pr} \div \frac{p^2-q^2}{p^2-r^2}$

g. $\frac{m^2-4}{m+1} \div \frac{m+2}{m^2+2m+1}$

h. $\frac{x^2y^2+3xy}{4x^2-1} \div \frac{xy+3}{2x+1}$

i. $\frac{a^2-5a}{a^2-4a-5} \div \frac{a^2-a-2}{a^2+2a+1}$ j. $\frac{x^2-8x}{x^2-4x-5} \times \frac{x^2+2x+1}{x^3-8x^2} \div \frac{x^2+2x-3}{x-5}$

a. $\frac{5}{x} \div \frac{10}{x}$
 $= \frac{\cancel{5}}{\cancel{x}} \times \frac{\cancel{x}}{10_2}$
 $= \frac{1}{2}$

b. $\frac{m}{3n} \div \frac{m}{2n^2}$
 $= \frac{\cancel{m}}{3\cancel{n}} \times \frac{2n^2}{\cancel{m}}$
 $= \frac{2n}{3}$

c. $\frac{x+1}{y} \div \frac{2(x+1)}{x}$
 $= \frac{\cancel{x+1}}{y} \times \frac{x}{2(\cancel{x+1})}$
 $= \frac{x}{2y}$

d. $\frac{2a-4}{2a} \div \frac{a-2}{3}$
 $= \frac{2a-4}{2a} \times \frac{3}{a-2}$
 $= \frac{\cancel{2}(a-\cancel{2})}{\cancel{2}a} \times \frac{3}{\cancel{a-2}}$
 $= \frac{3}{a}$

e. $\frac{x^2+4x}{3y} \div \frac{x^2-16}{12y^2}$
 $= \frac{x^2+4x}{3y} \times \frac{12y^2}{x^2-16}$
 $= \frac{x(\cancel{x+4})}{\cancel{3}y} \times \frac{4\cancel{12}y^2 \ y}{(x-4)(\cancel{x+4})}$
 $= \frac{4xy}{x-4}$

$$\text{f. } \frac{p^2 + pq}{p^2 - pr} \div \frac{p^2 - q^2}{p^2 - r^2}$$

$$= \frac{p^2 + pq}{p^2 - pr} \times \frac{p^2 - r^2}{p^2 - q^2}$$

$$= \frac{\cancel{p}(\cancel{p} + q)}{\cancel{p}(\cancel{p} - r)} \times \frac{(\cancel{p} - r)(p + r)}{(p - q)(\cancel{p} + q)}$$

$$= \frac{p + r}{\underline{\underline{p - q}}}$$

$$\text{g. } \frac{m^2 - 4}{m + 1} \div \frac{m + 2}{m^2 + 2m + 1}$$

$$= \frac{m^2 - 4}{m + 1} \times \frac{m^2 + 2m + 1}{m + 2}$$

$$= \frac{(m - 2)(\cancel{m} + 2)}{\cancel{m} + 1} \times \frac{(\cancel{m} + 1)(m + 1)}{\cancel{m} + 2}$$

$$= \underline{\underline{(m - 2)(m + 1)}}$$

$$\text{h. } \frac{x^2y^2 + 3xy}{4x^2 - 1} \div \frac{xy + 3}{2x + 1}$$

$$= \frac{x^2y^2 + 3xy}{4x^2 - 1} \times \frac{2x + 1}{xy + 3}$$

$$= \frac{xy(\cancel{xy} + 3)}{(2x - 1)(\cancel{2x} + 1)} \times \frac{\cancel{2x} + 1}{\cancel{xy} + 3}$$

$$= \frac{xy}{\underline{\underline{(2x - 1)}}}$$

$$\text{i. } \frac{a^2 - 5a}{a^2 - 4a - 5} \div \frac{a^2 - a - 2}{a^2 + 2a + 1}$$

$$= \frac{a^2 - 5a}{a^2 - 4a - 5} \times \frac{a^2 + 2a + 1}{a^2 - a - 2}$$

$$= \frac{a(\cancel{a} - 5)}{(\cancel{a} - 5)(\cancel{a} + 1)} \times \frac{(\cancel{a} + 1)(\cancel{a} + 1)}{(a - 2)(\cancel{a} + 1)}$$

$$= \frac{a}{\underline{\underline{(a - 2)}}}$$

$$\text{j. } \frac{x^2 - 8x}{x^2 - 4x - 5} \times \frac{x^2 + 2x + 1}{x^3 - 8x^2} \div \frac{x^2 + 2x - 3}{x - 5}$$

$$= \frac{x^2 - 8x}{x^2 - 4x - 5} \times \frac{x^2 + 2x + 1}{x^3 - 8x^2} \times \frac{x - 5}{x^2 + 2x - 3}$$

$$= \frac{\cancel{x}(\cancel{x} - 8)}{(\cancel{x} - 5)(\cancel{x} + 1)} \times \frac{(\cancel{x} + 1)(x + 1)}{x^2(\cancel{x} - 8)} \times \frac{\cancel{x} - 5}{(x + 3)(x - 1)}$$

$$= \frac{x + 1}{\underline{\underline{x(x + 3)(x - 1)}}}$$