

Merge sort

```
void mergesort (int *a, int low, int high)
```

```
{
```

```
    int mid;
```

```
    if (low < high)
```

```
    {
```

```
        mid = (low + high) / 2;
```

```
        mergesort (a, low, mid);
```

```
        mergesort (a, mid + 1, high);
```

```
        merge (a, low, high, mid);
```

```
    }
```

```
return;
```

```
}
```

```
void merge (int *a, int low, int high, int mid)
```

```
{
```

```
    int i, j, k, c[50];
```

```
    i = low
```

```
    k = low
```

```
    j = mid + 1
```

```
    while (i ≤ mid & j ≤ high)
```

```
    { if (a[i] < a[j])
```

```
        { c[k] = a[i]
```

```
          k++; i++;
```

```
        }
```

```
    else
```

```
    { c[k] = a[j]
```

```
      k++; j++;
```

```
    }
```

```
}
```

```
while (i ≤ mid)
```

```
{ c[k] = a[i]; k++; i++;
```

```
}
```



```

while (j < high)
{
    C[k] = A[i]
    k++ ; j++ ;
}

```

}

```

for (int i = low ; i <= high ; i++)

```

```

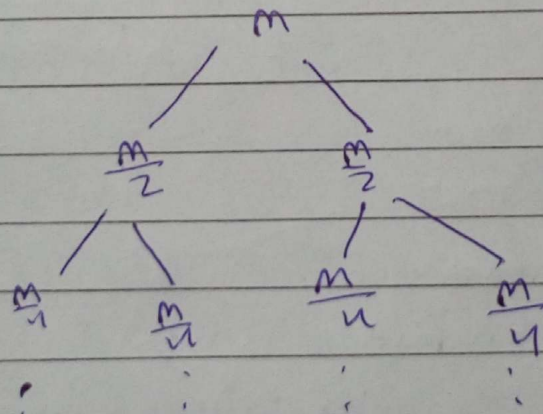
{
    A[i] = C[i] ;
}

```

Conceptually, a merge sort works as follows

- 1) Divide the unsorted list into n sublists
- 2) Repeated merge sublists to produce new sorted sublists until there is only 1 sublist remaining.

So, in merge sort the tree goes like this



$$T(m) = 2T\left(\frac{m}{2}\right) + O(m)$$

At each level we are merging some smaller segment to form bigger one. Merging sorted array to form sorted array takes $O(m)$. Since there are \log_2^N levels the total time complexity - $O(N \log^N)$

Proof

~~Given~~ Assume that it gives sorted array for $\frac{N}{2}$ elements and if merging is correct then by this merging of $\frac{N}{2} + \frac{N}{2}$ elements

gives sorted array of N elements.
Now ~~return~~ in the last level when no of
elements = 1 it returns sorted array
so whole array will become sorted.

Quick Sort

```
void quickSort (int arr[], int l, int r)
{
    int i = l ; int j = r
    int temp;
    int pivot = arr [(l+r)/2]

    while (i <= j) {

        while (arr[i] < pivot) i++;

        while (arr[j] > pivot) j--;

        if (i < j) { swap(arr[i], arr[j]);
                    i++;
                    j--;
                }

        if (l < j) quickSort (arr, l, j);

        if (i < r) quickSort (arr, i, r);
    }
}
```


In quick sort we choose a pivot element and partition the array about the pivot point. then we recursively sort the left side of pivot element for sorting and then the right side.

Since after partitioning the ~~partition~~ pivot element comes to it's right place in sorted array and the the left side and right side also goes for partitioning

Running Time Analysis

~~$T(n) = \frac{n^2}{2}$~~

Let k be the position of pivot element

$$\therefore T(n) = T(k-1) + T(n-k) + O(n)$$

this comes to $O(n \log n)$ for average k

For worst case $k=1$

$$T(n) = T(n-1) + O(n)$$

this is $O(n^2)$

\therefore when array is already sorted in decreasing order. quick sort takes $O(n^2)$

memory complexity = $O(n)$ since we used only one array