

1.

a. $O(n)$ increases by 1 when n is in the series.

2, 2^2 , 2^{2^2} , $2^{2^{2^2}}$, etc.

$O(2)$ $n=16$

$O(3)$ $n=256$

$O(4)$ $n=65536$

$O(x)$ $n=2^{2^x}$

Solve for n $O(\log(\log(n)))$

Final = $\theta(\log(\log(n)))$

b. "for(int i=0; i<=n; i++)" runs n times

Only triggers inner loop \sqrt{n} times.

an $O(1)$ event gets triggered i^3 times

$n=36$: $6^3 + 12^3 + 18^3$

$n=49$: $7^3 + 14^3 + 21^3$

From $0 \rightarrow \sqrt{n}$ add i^3

$\sqrt{n}^3 \sqrt{n}^4 = O(\sqrt{n} * n^3)$

Final = $\theta(\sqrt{n} * n^3)$

c. First loop runs in $O(n)$ time

inside loop runs only approximately $\log(n)$ times

triggers another $O(n)$ loop

input 100 output ~ 300

input 1000 output ~ 3000

Final $\theta(n(\log(n)))$

d. call rfunc

2 things that do something

loop($N, n == \sqrt{n}$)

$O(1)$

$O(1)$

Rhelp(n)

Rfunc($n-m, m$)

$O(n/\sqrt{n} * O(2) + O(n))$

Final = $\theta(n^2/\sqrt{n})$

