CMPT-726

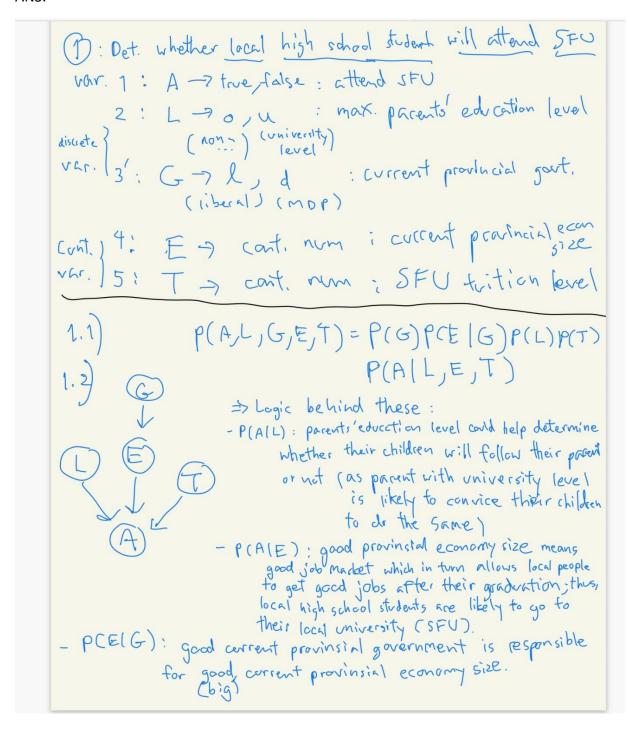
Assignment 3: Graphical Models / Recurrent Neural Networks

Due November 15 at 11:59pm

1. Graphical Models (22 marks)

- 1.1. Draw a simple Bayesian network for this domain.
- 1.2. Write the factored representation for the joint distribution p(A, L, G, E, T) that is described by your Bayesian network.

ANS:



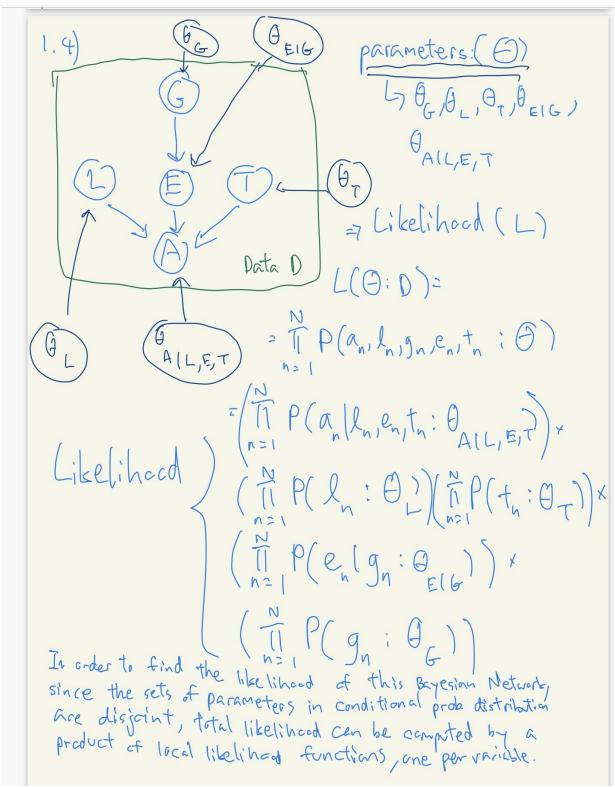
1.3. Supply all necessary conditional distributions. Provide the type of distribution that should be used and give rough guidance / example values for parameters (do this by hand, educated guesses).

ANS:

1.3) => P(E(G) & P(T) ; continuous ru. I use Gaussian distribution with Mean (n) and variance (62) as parameter because it has common occurance in many natural phenomena (so it is common and safe to assume the unknown distributions to be Gaussian distribution. => P(L), P(G), P(A/L,E,T): discrete random var. I use Bernoulli distribution. parameter p is probability of event 1 occurs while 1-p is a probability of event z occurs. For example, PCG) with p = 0.8 is probability that current provinsial government is MPD W/ 80.1. prob while it is Liberal W/ prob of 20%.

1.4. Suppose we had a training set and wanted to learn the parameters of the distributions using maximum likelihood. Denote each of the N examples with its values for each random variable by xn = (an, ln, gn, en, tn). The training set is $\{x1, x2, \ldots, xN\}$. Which elements of the training data are needed to learn the parameters for p(A|paA)? Why?1 Start by writing down the likelihood and argue from there.

ANS:



2. KL Divergence (20 marks)

- 2.1. ANS:
- 2.2. ANS:

(2) KL Divergence 2.1) Ans: KL divergence is not symmetric D(P116) - D(Q11P) may not be zero.

Even though the KL divergence measures the difference between 2 distributions, it is not a distance measure.

This is 120 in 1120. This is because that the KL divergence is not a metric mensure, xx 2.L) Ans Show D (PILP) = 0 from DK(PIIP) = SP(X) ln P(X) dx = Sp(x) [lnp(x)-lnp(x)]dx = Spexylnpexydx - Spexylnpexydx

2.3. ANS:

2.3) KL D Alveys non-negative.

Ans powe
$$D_{kL}(P|Q) \ge 0$$
 or $-D_{kL}(P|Q) \le 0$
 $-D(P|Q) = -\int P(X) \ln P(X) dX$
 $= \int P(X) \ln Q(X) dX$
 $= \int P(X) \ln Q(X) dX$

From Jensen's inequality: log/ln is a concave function concave function

 $= \int P(X) \ln Q(X) dX$
 $= \int P(X) \ln$

2.4. ANS:

2.4),
$$D_{k}(P|IQ) = \ln \frac{6q}{6p} + \frac{6p}{6p} + (N_{p}-N_{q})^{2} - \frac{1}{2}$$

$$= \ln \frac{6q}{6p} + \frac{6^{2}}{26q} - \frac{1}{2} = \ln \frac{6q}{6p} + \frac{6^{2}}{26q} - \frac{6q}{26q}$$

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$$= \ln \frac{6q}{6q} + \frac{6q}{6q} - \frac{6q}{6q}$$

$$= \ln \frac{6q}{6q$$

3. Gated Recurrent Unit (10 marks)

3.1.ANS:

3.2.ANS:

3
$$r_j = 6([W_r \times]_j + [U_r h_{(4-1)}]_j)$$
 $z_j = 6([W_z \times]_j + [U_z h_{(4-1)}]_j)$
 $h_j^{(+)} = z_j h_j^{(+)} + (1-z_j) h_j^{(+)}$
 $h_j^{(+)} = z_j h_j^{(+)} + (1-z_j) h_j^{(+)}$

3.1) We want $h_j^{(+)} = h_j^{(+)}$
 $z_j = h_j^{(+)} + (1-z_j) h_j^{(+)}$
 $z_j = h_j^{(+)} + h_j^{(+)}$

-> the hidden will use just correct content.
(incoming new input x).
note: Z = update gate : helps model
note: Z = opdate gate i helps model determine how much the past information (from previous time steps) is needed to be passed
note: (=) reset gate: helps model
note: (=) reset gate: helps model
occurre now much the past information
to forget. high r -> product will preserve
(roh(+-1)) Past information.
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4. Attention Models (10 marks)

4.1.ANS:

Decause the Transformer model does not require word inputs that will be fed into network to have specific orders or positions. Therefore, it needs some technique (sinusoidal encoding) to help the model incorporates the order of words by adding a position-dependent signal to each wood-embedding.

The sinusoidal encoding does not require the sentence to be fix length compared to one-hat encoding scheme. It was properties of sin(x) and cos(x) [(yclic)] functions to return information of the position of a word in a sentence.

4.2.ANS: