

CSE P 517: Homework 1

Language Models

Due Jan 15 Fri 11:59pm 2021

Submission instructions Submit 2 files on [Canvas](#):

- 1 **Report:** (HW1.pdf): You will submit a typed report in the pdf format. The quality of report will be a very important aspect of grading. Key points to keep in mind are (1) clarity (neat organization with graphs and tables whenever applicable) and (2) insightful analysis and commentaries. When writing about “*error analysis*”, an important practice in any NLP project, try to make concrete arguments through examples. The report will typically be about 2-5 pages in total, but there will be no formal restriction on font sizes, page margins, or even number of pages.
 - 2 **Code:** (HW1.tgz): Whenever applicable, you will also submit your code together with a neatly written README file to instruct how to run your code with different settings. We prefer either Python or Java code for compatibility reasons. Discuss with the teaching crew in advance if you want to use some other programming language. While we recommend that you always follow good coding practice (commenting, structuring), we will not grade your code based on such qualities of code writing practice.
- *Late submission:* please check the class homepage for the late submission policy. These credits are to accommodate your conference trips, deadlines, and illness. You may use your credits whenever you want! Therefore, please do not contact the teaching crew to ask whether you may use your unused credits, unless there are circumstances that require clarification.

1 [Programming] Language Models (6 pts)

For the first part of this assignment, you will implement unigram, bigram, and trigram language models. Recall that the probability of seeing a sentence $\mathbf{s} = \{x_1, \dots, x_n\}$ can be modeled as follows if using the trigram models without the special START symbols:

$$p(\mathbf{s}) = p(x_1 \dots x_n) = q(x_1)q(x_2|x_1) \prod_{i=3}^n q(x_i | x_{i-2}, x_{i-1})$$

$q(x_i | x_{i-2}, x_{i-1})$ is the probability of seeing the current word x_i after seeing the bigram (x_{i-2}, x_{i-1}) . Always assume that the last word is the special STOP symbol, i.e., $x_n = \text{STOP}$. Alternatively, if you like to include the special START symbols, you can instead do the following:

$$p(\mathbf{s}|\text{START}_2, \text{START}_1) = p(x_1 \dots x_n|\text{START}_2, \text{START}_1) = \prod_{i=1}^n q(x_i | x_{i-2}, x_{i-1})$$

1.1 Dataset

For problem 1 and 2 of this assignment, you are provided with `CSEP517-HW1-Data-Small.zip`, which contains following three files:

- `brown.train.txt`: data to train your language model with (i.e. to estimate $q(x_i | x_{i-2}, x_{i-1})$)
- `brown.dev.txt`: development data for you to choose the best smoothing parameters
- `brown.test.txt`: test data for evaluating your language model

The data files are formatted with each line containing a tokenized sentence (white spaces mark token boundaries). Note that using the test set for training or finding the best parameters is considered cheating.

1.2 Perplexity

One way to evaluate the language model is computing the perplexity of the model on previously unseen data. Recall that computing the perplexity involves computing the average log probability of the entire corpus:

$$\text{perplexity} = 2^{-l}$$

where

$$l = \frac{1}{M} \sum_{i=1}^m \log_2 p(\mathbf{s}_i) = \frac{1}{M} \sum_{i=1}^m \log_2 p(x_{i1}, \dots, x_{in_i})$$

and M is the total number of words in the text (i.e. the sum of lengths of all sentences).

A word of caution: You will primarily use *brown.dev.txt* as the previously unseen data while (i) developing and testing your code, (ii) trying out different design decisions (e.g., different ways of handling out-of-vocabulary words), (iii) tuning the hyperparameters (see problem # 2 below), and (iv) performing error analysis. For scientific integrity, it is extremely important that you will use the real test data *brown.test.txt* only once just before you report all the final results. Otherwise, you will start overfitting on the test set indirectly. Please don't be tempted to run the same experiment more than once on the test data.

1.3 Tips

When implementing the language model, there are several things to consider:

- Don't forget to handle the out-of-vocabulary (OOV) words by converting some of the low frequency words into UNK during training.
- You will need to include the special STOP word at the end of each sentence. It is optional if you include the special START words.
- Make sure that $q(x_i | x_{i-2}, x_{i-1})$ is a valid probability distribution. More concretely, each trigram probability conditioning on a different history must sum up to 1, e.g., $\sum_i q(x_i | \text{"the cat"}) = 1$ and $\sum_i q(x_i | \text{"the dog"}) = 1$.
- Be mindful of underflow! Code up in the log space, where $\log \prod_i q(x_i) = \sum_i \log q(x_i)$.

1.4 Deliverables

1. Report the perplexity scores of the unigram, bigram, trigram language models for your *training*, *dev* and *test* sets, and elaborate all your design choices (e.g., if you introduced START symbols in addition to STOP symbols, how you handled out-of-vocabulary words). Briefly discuss the experimental results.

2 [Programming] Smoothing (6 pts)

To make your language model work better, you will need to implement the following smoothing techniques:

2.1 Add- K Smoothing

$$p(x_i \mid x_{i-2}, x_{i-1}) = \frac{K + C(x_{i-2}, x_{i-1}, x_i)}{\sum_{x \in \mathcal{V}^*} (K + C(x_{i-2}, x_{i-1}, x))}$$

where $C(x_{i-2}, x_{i-1}, x_i)$ is the trigram count, and \mathcal{V}^* is the set of your entire vocabulary (including special tokens such as OOV words and sentence boundaries).

2.2 Choosing Hyper-parameters

You can use the development data *brown.dev.txt* to decide the best values of the hyper-parameters (K , λ_1 , λ_2 , and λ_3). The fancier way of picking the hyper-parameters for linear interpolation is through Expectation-Maximization (EM), but you haven't learned it yet. For this homework, you will instead do a “grid search”, which means you will simply try a few combinations of “reasonable” values.

2.3 Deliverables

For this part of the homework, you will only work with trigram language models.

1. (a) Report perplexity scores on *training* and *dev* sets for various values of K . Try to cover a couple of orders of magnitude (e.g. $K = 10$, $K = 1$, 0.1 , ...).

(b) Putting it all together, report perplexity on the *test* set, using different smoothing techniques and the corresponding hyper-parameters that you chose from the dev set. Specify those hyper-parameters.
2. If you use only half of the training data, would it in general increase or decrease the perplexity on the previously unseen data? Discuss the reason why.
3. If you convert all words that appeared less than 5 times as UNK (a special symbol for out-of-vocabulary words), would it in general increase or decrease the perplexity on the previously unseen data compared to an approach that converts only a fraction of words that appeared just once as UNK? Discuss the reason why.

3 [Written] Language Model Classifier (3 pts)

One of the possible applications of language models, not covered in the lecture, is text categorization: given a document x as a sequence of words, assigning a category label y . Examples of text categorization include spam email detection $y \in \{spam, not_spam\}$, news topic categorization $y \in \{sport, politics, science, \dots\}$, authorship attribution $y \in \{shakespeare, woolf, pinker, \dots\}$.

3.1 Deliverables

1. Sketch out how you can make use of language models for text categorization. Use equations whenever possible.

Hint: For any document D , the most likely author c^* can be determined as

$$\begin{aligned} c^* &= \operatorname{argmax}_{c \in C} P(c \mid D) \\ &= \operatorname{argmax}_{c \in C} p(D \mid c) p(c) \\ &= \dots? \end{aligned}$$

4 [Bonus] (max 2 pts)

This section is optional and is not required to get full credit for the homework. While students are free to do any subset of bonus portions, there will be at most 2 points awarded out of them in total in the end.

4.1 [Programming] Using the Full Dataset (0.5 pt)

Use the full dataset provided under CSEP517-HW1-Data-Full.zip for problem 1 and 2 above, and report the numerical results.

4.2 [Programming] Linear Interpolation (2 pts)

Implement linear interpolation as your language model in problem 2.

$$p'(x_i | x_{i-2}, x_{i-1}) = \lambda_1 \times p(x_i | x_{i-2}, x_{i-1}) + \lambda_2 \times p(x_i | x_{i-1}) + \lambda_3 \times p(x_i)$$

where $\lambda_1 + \lambda_2 + \lambda_3 = 1$.

Deliverables

1. Report perplexity scores on *training* and *dev* sets for various values of λ_1 , λ_2 , λ_3 . Report no more than 5 different values for your λ 's.
2. Report perplexity on the *test* set, using the corresponding hyper-parameters that you chose from the dev set. Specify those hyper-parameters.

4.3 [Written] Back-off Smoothing (1 pt)

In class, we discussed how back-off can improve the performance of language models. Consider the following back-off scheme. First, we define the sets

$$\begin{aligned}\mathcal{A}(w_{i-1}) &= \{w : c(w_{i-1}, w) > 0\} \\ \mathcal{B}(w_{i-1}) &= \{w : c(w_{i-1}, w) = 0\} \\ \mathcal{A}(w_{i-2}, w_{i-1}) &= \{w : c(w_{i-2}, w_{i-1}, w) > 0\} \\ \mathcal{B}(w_{i-2}, w_{i-1}) &= \{w : c(w_{i-2}, w_{i-1}, w) = 0\}\end{aligned}$$

where c is a function that counts n -grams in the training set. For example, if the bigram "Honey Bunny" appears 22 times in the corpus, we will have $c(\text{Honey}, \text{Bunny}) = 22$.

Now, we can define a back-off trigram model:

$$p(w_i | w_{i-2}, w_{i-1}) = \begin{cases} p_1(w_i | w_{i-2}, w_{i-1}) & \text{If } w_i \in \mathcal{A}(w_{i-2}, w_{i-1}) \\ p_2(w_i | w_{i-2}, w_{i-1}) & \text{If } w_i \in \mathcal{A}(w_{i-1}) \text{ and } w_i \in \mathcal{B}(w_{i-2}, w_{i-1}) \\ p_3(w_i | w_{i-2}, w_{i-1}) & \text{If } w_i \in \mathcal{B}(w_{i-1}) \end{cases}$$

Where:

$$\begin{aligned}p_1(w_i | w_{i-2}, w_{i-1}) &= p_{ML}(w_i | w_{i-2}, w_{i-1}) \\ p_2(w_i | w_{i-2}, w_{i-1}) &= \frac{p_{ML}(w_i | w_{i-1})}{\sum_{w \in \mathcal{B}(w_{i-2}, w_{i-1})} p_{ML}(w | w_{i-1})} \\ p_3(w_i | w_{i-2}, w_{i-1}) &= \frac{p_{ML}(w_i)}{\sum_{w \in \mathcal{B}(w_{i-1})} p_{ML}(w)}\end{aligned}$$

Deliverables

1. Does the above model form a valid probability distribution? Prove your answer. If it does not form a valid probability distribution, suggest how to make it one by modifying p_1 , p_2 and p_3 , using p_{ML} (the maximum likelihood estimate) and/or the count function c , and briefly explain why your modification works.