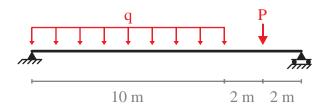
# Homework 1 Due: Friday, September 25, 2015 @ 5:00 PM in E218

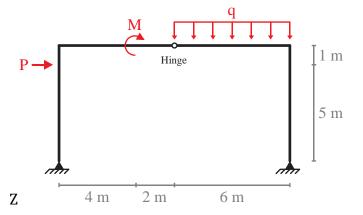
For each of the systems shown below:

- i) Find the reactions and draw the complete FBD
- ii) For the beam and frame: draw the shear and moment diagrams (onto the actual structure) For the truss: calculate axial forces and label on the FBD
- iii) Sketch the approximate deformed shape (you do not need to calculate for deflections) Show all calculations, provide all critical values for shear and moment diagrams, use a ruler for diagrams, and use consistent sign convention. M = 5 kNm, P = 10 kN, q = 2 kN/m. 10 pts each.

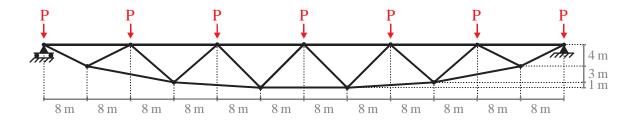
#### **1.** Beam:



#### **2.** Frame:



#### 3. Truss:



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## Homework 2 Due: Friday, October 2, 2015 @ 5:00 PM in E218

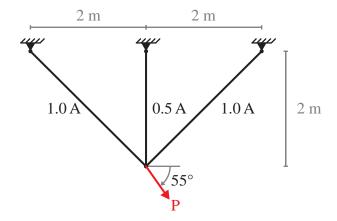
Solve each problem by hand:

- i) Redraw the diagram and label your degrees of freedom
- ii) Generate the element and global stiffness matrices
- iii) Solve for the displacements, reactions, and axial forces
- iv) Draw the FBD (with axial forces labeled) and sketch the deformed shape
- Also perform an analysis using SAP2000:

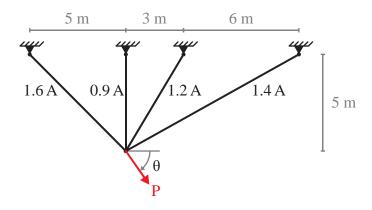
  v) Provide labeled images of your input geometry (with loads shown) and the deformed shape
  - vi) Compare (tabulate and discuss) your hand calculations with your SAP2000 analysis
- **1.** 1D truss: P = 60 kN,  $E = 200\ 000 \text{ MPa}$ ,  $A = 1000 \text{ mm}^2$ , L = 3 m. **15 pts**



**2.** 2D truss: P = 100 kN, E = 200 000 MPa,  $A = 1000 \text{ mm}^2$ . **20 pts** 



**3.** 2D truss: Find the magnitude (P) and direction ( $\theta$ ) required to obtain a displacement at the bottom node of {u, v} = {3 mm, -2 mm}. E = 200 000 MPa, A = 10 000 mm<sup>2</sup>. Hint: how many unknown displacements are there? **20 pts** 



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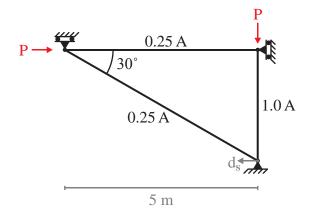
### Homework 3 Due: Friday, October 9, 2015 @ 5:00 PM in E218

Solve Questions 1 and 2 by hand:

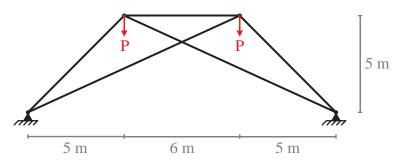
- i) Redraw the diagram and label your nodes and degrees of freedom
- ii) Generate the element stiffness matrices, but not the global stiffness matrix
- iii) Solve for the displacements, reactions, and axial forces without the global stiffness matrix
- iv) Draw the FBD (with axial forces labeled) and sketch the deformed shape

Also perform an analysis with your MATLAB program for Questions 1, 2, and 3:

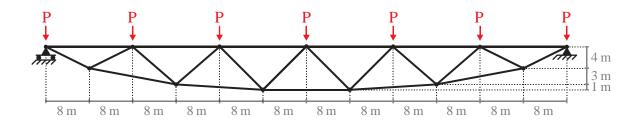
- v) Provide labeled images of your input geometry (with loads shown) and the deformed shape
- vi) Compare (tabulate and discuss) your hand calculations with your MATLAB analysis
- vii) Provide a short description of your codes changes and attach a printout <u>only</u> of the parts of the code that you changed
- **1.** Truss:  $d_S = 1$  mm to the left. P = 100 kN, E = 200 000 MPa, A = 2000 mm<sup>2</sup>. **15 pts**



2. Truss: P = 10 kN,  $E = 120\ 000 \text{ MPa}$ ,  $A = 1500 \text{ mm}^2$ . You will need to use symmetry. 15 pts



**3.** Truss: Use hand calculations from HW1 for relevant comparisons. P = 10 kN, E = 200,000 MPa,  $A = 1200 \text{ mm}^2$ . **10 pts** 



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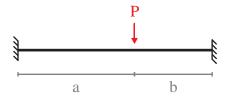
#### Homework 4 Due: Friday, October 16, 2015 @ 5:00 PM in E218

Solve **Questions 1 and 2** by hand:

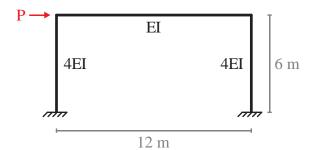
- i) Redraw the diagram and label your nodes and degrees of freedom
- ii) Generate the element stiffness matrices and the global stiffness matrix
- iii) Solve for the displacements, reactions, and internal moments and shears
- iv) Draw the Free Body, moment, and shear diagrams, and sketch the deformed shape

Code in the beam element into MATLAB and perform an analysis for **Questions 2 and 3**:

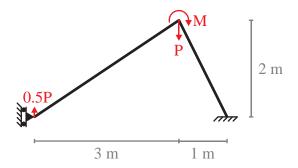
- v) Provide labeled images of your input geometry (with loads shown) and the deformed shape
- vi) Compare (tabulate and discuss) your hand calculations with your MATLAB analysis
- vii) Provide a short description of your codes changes and attach a printout <u>only</u> of the parts of the code that you changed
- **1.** Beam: Solve in variable form. E, I are constant. Hint:  $a^3 + 3a^2b + 3ab^2 + b^3 = (a + b)^3$ . **10 pts**



**2.** Frame: Ignore axial deformations. P = 12 kN, E = 30~000 MPa,  $I = 2 \times 10^9$  mm<sup>4</sup>. **20 pts** 



**3.** Frame: You do not need to provide a comparison with any hand calculations, but you still need to provide a table of results. Also, draw the Free Body, moment and shear diagrams by hand. P = 200 kN, M = 100 kNm, E = 100 000 MPa,  $A = 5000 \text{ mm}^2$ ,  $I = 200 \text{ x } 10^6 \text{ mm}^4$ . **10 pts** 



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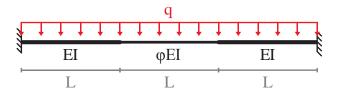
### Homework 5 Due: Friday, October 23, 2015 @ 5:00 PM in E218

For all questions:

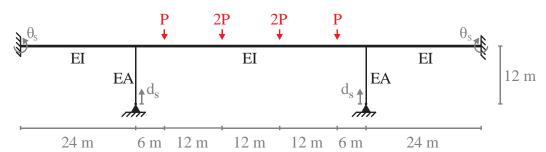
- i) Find the Equivalent Nodal Forces by hand (be sure to include diagrams) Solve **Questions 1 and 2** by hand:
  - ii) Redraw the diagram and label your nodes and degrees of freedom
  - iii) Generate the element stiffness matrices, but not the global stiffness matrix
  - iv) Solve for displacements, reactions, and internal forces without the global stiffness matrix
  - v) Draw the FBD, moment and shear diagrams, and sketch the deformed shape

Code in the hinge element into MATLAB and perform an analysis for **Questions 2 and 3**:

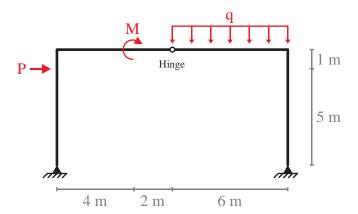
- vi) Provide labeled images of your input geometry with loading and the deformed shape
- vii) Compare (tabulate and discuss) your hand calculations with your software analysis
- viii) Provide a short description of your codes changes and attach a printout <u>only</u> of the parts of the code that you changed
- 1. Beam: Find  $\varphi$  that makes the moments zero at a distance L from either support. 15 pts



**2.** Beam/Truss Hybrid: The horizontal beam is supported by two truss elements. P = 60 kN,  $\theta_S = 1 \times 10^{-4} \text{ rad}$ ,  $d_s = 2 \text{ mm}$ , E = 50 000 MPa,  $I = 1.2 \times 10^{12} \text{ mm}^4$ ,  $A = 90 000 \text{ mm}^2$ . **25 pts** 



**3.** Frame: Tabulate displacements, reactions, internal forces, and draw shear, moment, and free body diagrams. Use hand calculations from HW1 for relevant comparisons. M = 5 kNm, P = 10 kN, Q = 2 kN/m, Q = 2



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