

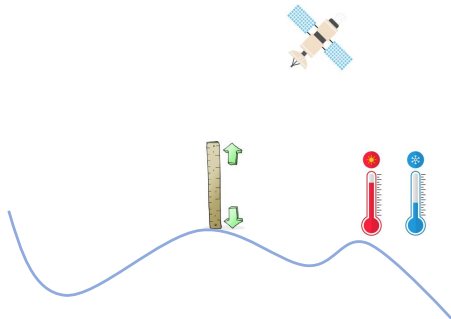
Deep Sea Surface Height Multivariate Interpolation

Théo Archambault *third year Ph.D. candidate at Sorbonne Université, LIP6 and LOCEAN*

Pierre Garcia, Anastase Charantonis, Dominique Béréziat

24 avril 2024

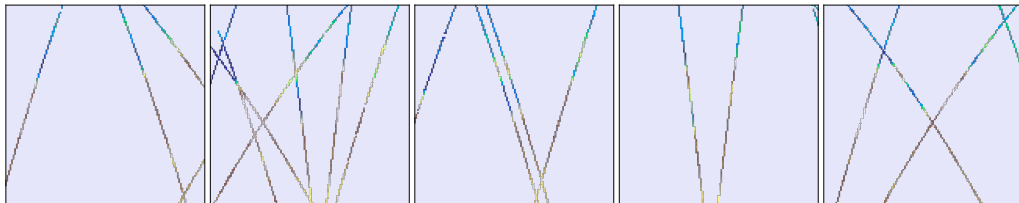
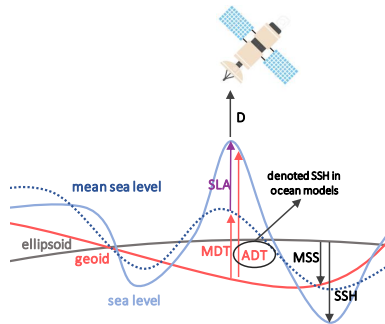
Multi-Variate satellite surface observations of the ocean



Sea Surface Height

- Used to derive surface currents to geostrophic approximation
- Measurement principle : return time of a radar pulse
- Nadir-pointing altimeters : only measure data along their ground tracks^a

a. We use the L3 reprocessed DUACS data.

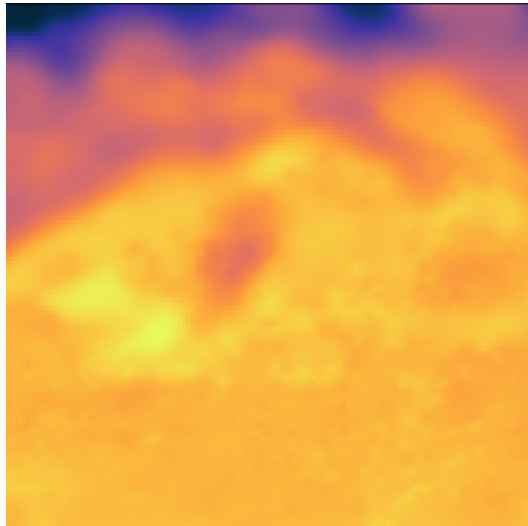


Sea Surface Temperature

- Measurement principle : Direct infra-red image with high resolution ($1/25^\circ$)
- Clouds introduce gaps in data
- L4 SST fields^a : obtained through linear Optimal Interpolation combining several satellites and in-situ data.
- Noise : high-frequency instrumental errors and blurring.
- Advected by the currents.

a. We use the Multiscale Ultra-high Resolution dataset

SST MUR



Data

Observing System Simulation Experiment

We use an OSSE : we emulate satellite observations on a simulation (GLORYS12, CMEMS).

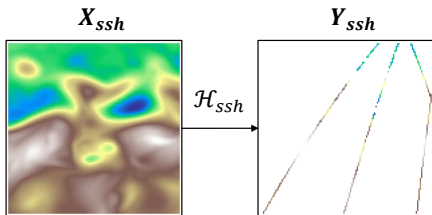
We assume that $\mathbf{Y} = \mathcal{H}(\mathbf{X}) + \varepsilon$

Observing System Simulation Experiment

We use an OSSE : we emulate satellite observations on a simulation (GLORYS12, CMEMS).

We assume that $\mathbf{Y} = \mathcal{H}(\mathbf{X}) + \varepsilon$

- \mathcal{H}_{ssh} : SSH along the satellite path + noise

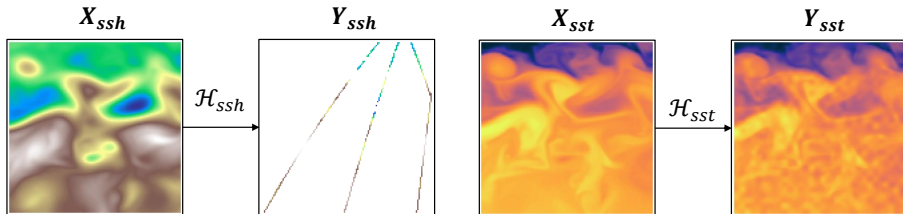


Observing System Simulation Experiment

We use an OSSE : we emulate satellite observations on a simulation (GLORYS12, CMEMS).

We assume that $\mathbf{Y} = \mathcal{H}(\mathbf{X}) + \varepsilon$

- \mathcal{H}_{ssh} : SSH along the satellite path + noise
- \mathcal{H}_{sst} : SST blurred in cloudy area + noise

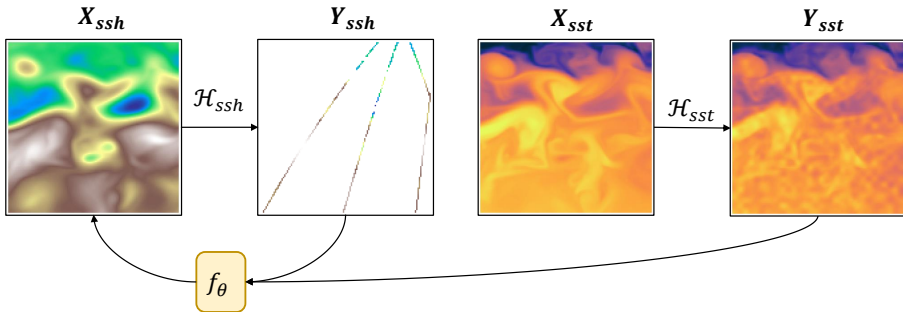


Observing System Simulation Experiment

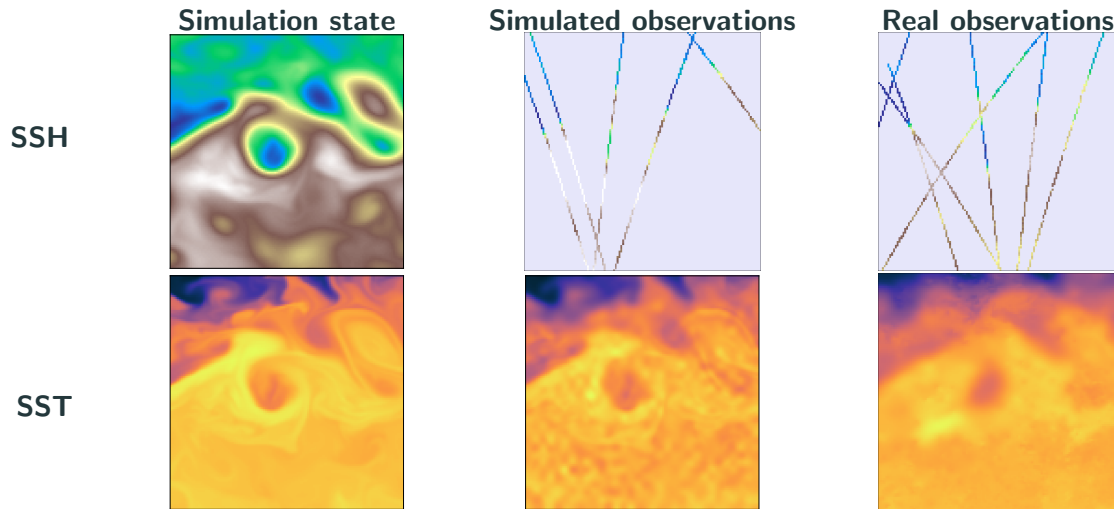
We use an OSSE : we emulate satellite observations on a simulation (GLORYS12, CMEMS).

We assume that $\mathbf{Y} = \mathcal{H}(\mathbf{X}) + \varepsilon$

- \mathcal{H}_{ssh} : SSH along the satellite path + noise
- \mathcal{H}_{sst} : SST blurred in cloudy area + noise
- f_{θ} : NN inversion \mathcal{H}_{ssh} using SSH and SST observations

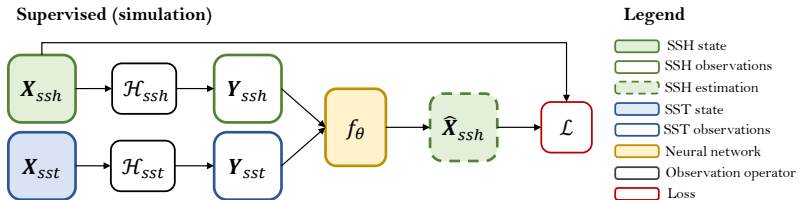


Domain gap ?

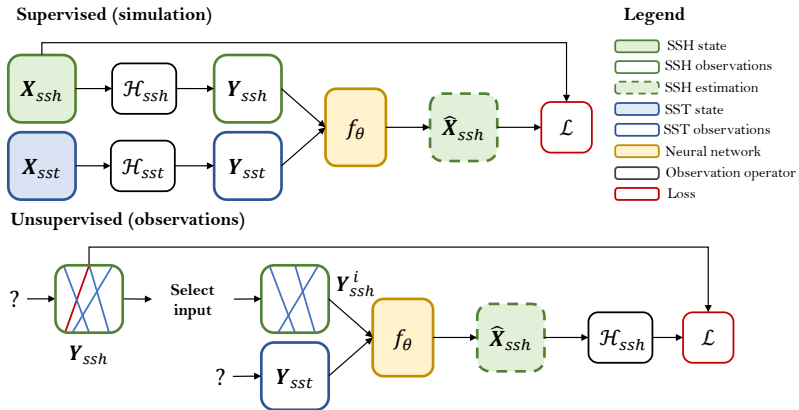


**Proposed Method : simulation
pre-training and observations
fine-tuning**

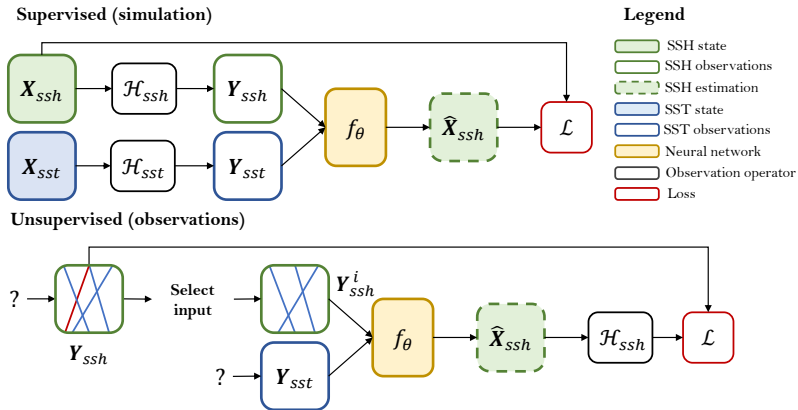
Learning method



Learning method

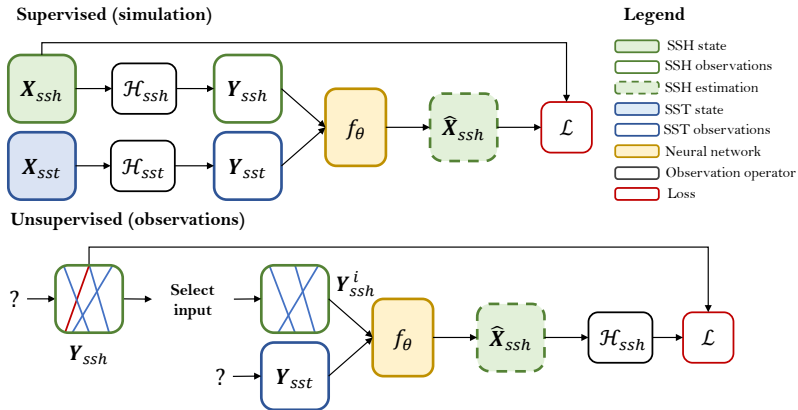


Learning method



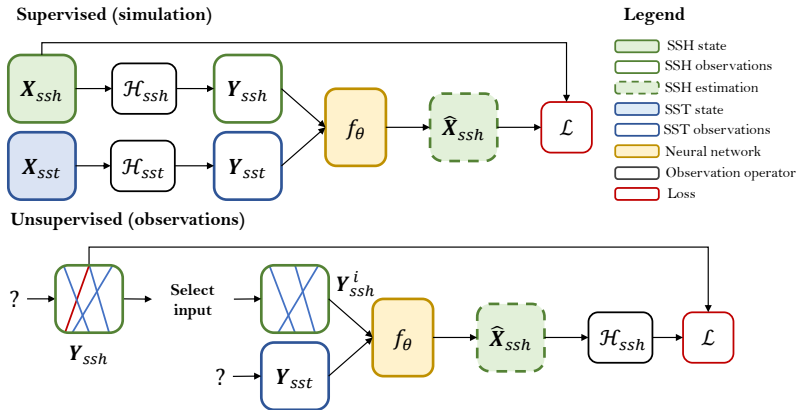
- Subset input data Y_{ssh}^i , and estimates \hat{X}_{ssh} from (Y_{ssh}^i, Y_{sst}) .

Learning method



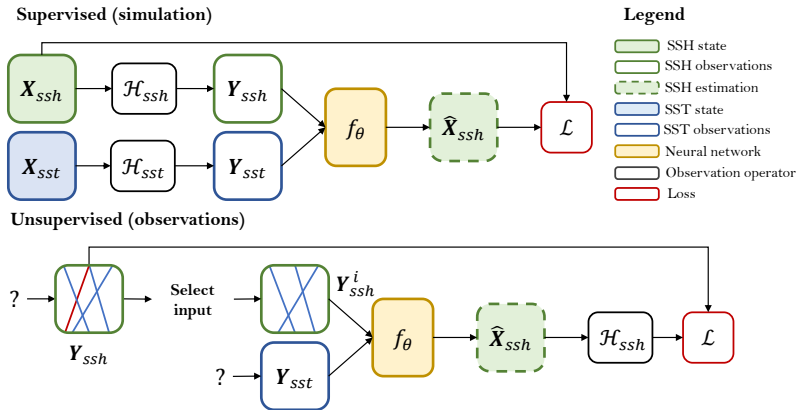
- Subset input data Y_{ssh}^i , and estimates \hat{X}_{ssh} from (Y_{ssh}^i, Y_{sst}) .
- Apply \mathcal{H}_{ssh} to \hat{X}_{ssh} before computing the loss.

Learning method



- Subset input data \mathbf{Y}_{ssh}^i , and estimates $\hat{\mathbf{X}}_{ssh}$ from $(\mathbf{Y}_{ssh}^i, \mathbf{Y}_{sst})$.
- Apply \mathcal{H}_{ssh} to $\hat{\mathbf{X}}_{ssh}$ before computing the loss.
- Removing some input observations helps to estimate the entire map accurately.

Learning method



- Subset input data Y_{ssh}^i , and estimates \hat{X}_{ssh} from (Y_{ssh}^i, Y_{sst}) .
- Apply \mathcal{H}_{ssh} to \hat{X}_{ssh} before computing the loss.
- Removing some input observations helps to estimate the entire map accurately.
- f_θ : Attention-Based Encoder Decoder taking 21 days of observations.

Results

Evaluation on a real observation dataset : the *Ocean Data Challenge 2021*.

- 1 year of data on the Gulf Stream area
- Provides state-of-the-art reconstruction methods
- Evaluation on independent data
- Metrics : μ the RMSE score (in cm), σ_t its temporal std (in cm), λ_x the half-resolved spatial wavelength (in km)

Evaluation on a real observation dataset : the *Ocean Data Challenge 2021*.

- 1 year of data on the Gulf Stream area
- Provides state-of-the-art reconstruction methods
- Evaluation on independent data
- Metrics : μ the RMSE score (in cm), σ_t its temporal std (in cm), λ_x the half-resolved spatial wavelength (in km)

We want to test :

- SST impact : training using SSH , $SSH + nSST$, $SSH + SST$
- The learning strategy

Comparing training strategies

Given the supervised and the unsupervised learning, we derive 3 strategies ;

Comparing training strategies

Given the supervised and the unsupervised learning, we derive 3 strategies ;

- **Observations only** : unsupervised training on real-world observations.

Input data	SSH			SSH+nSST			SSH+SST		
Learning method	μ	σ_t	λ_x	μ	σ_t	λ_x	μ	σ_t	λ_x
Observation	6.52	1.95	111	6.13	1.84	104	—	—	—

Comparing training strategies

Given the supervised and the unsupervised learning, we derive 3 strategies ;

- **Observations only** : unsupervised training on real-world observations.
- **Simulation only** : supervised training on simulation and direct inference on real-world data.

Input data	SSH			SSH+nSST			SSH+SST		
Learning method	μ	σ_t	λ_x	μ	σ_t	λ_x	μ	σ_t	λ_x
Observation	6.52	1.95	111	6.13	1.84	104	—	—	—
Simulation	6.35	1.9	112	6.2	1.87	108	6.85	2.22	111

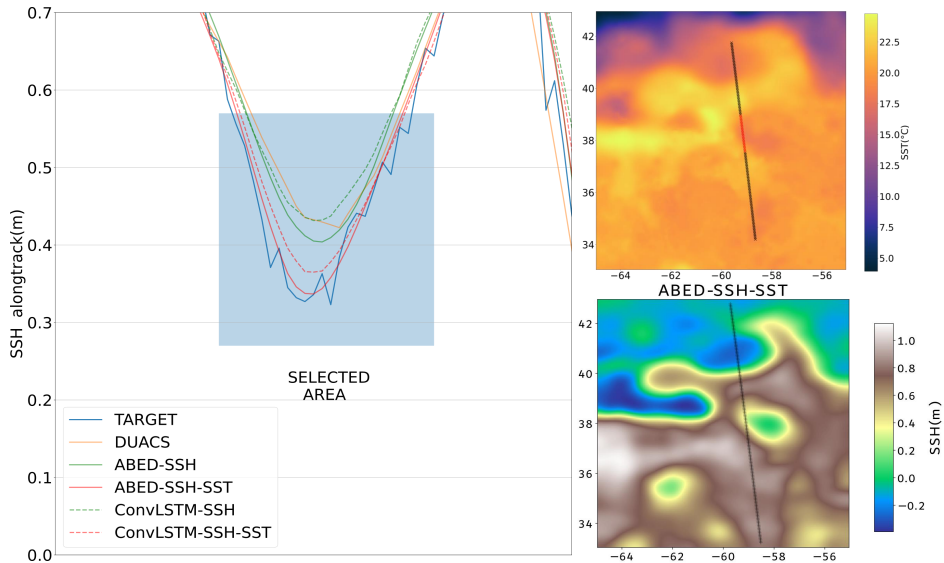
Comparing training strategies

Given the supervised and the unsupervised learning, we derive 3 strategies ;

- **Observations only** : unsupervised training on real-world observations.
- **Simulation only** : supervised training on simulation and direct inference on real-world data.
- **Both** : Supervised pre-training on simulation and unsupervised fine-tuning on real-world observations.

Input data	SSH			SSH+nSST			SSH+SST		
Learning method	μ	σ_t	λ_x	μ	σ_t	λ_x	μ	σ_t	λ_x
Observation	6.52	1.95	111	6.13	1.84	104	—	—	—
Simulation	6.35	1.9	112	6.2	1.87	108	6.85	2.22	111
Both	6.27	1.85	110	5.77	1.64	102	5.77	1.6	103

Improvements brought by SST



Conclusion

- Pre-training and fine-tuning improve the reconstruction.
- Especially with SST.

Thank you for your attention

Contact : *theo.archambault@lip6.fr* Web :



State-of-the-art comparison

Method	SST	NN	Learning	$\mu(cm)$	$\sigma_t(cm)$	$\lambda_x(km)$
DUACS	✗	✗	✗	7.66	2.66	138
DYMOST	✗	✗	✗	6.75	2.00	121
MIOST	✗	✗	✗	6.75	2.00	121
BFN	✗	✗	✗	7.46	2.59	114
4DVarNet	✗	✓	simulation	6.56	1.84	104
MUSTI	✓	✓	observation	6.26	1.96	107
CONVLSTM	✗	✓	observation	6.82	1.86	108
CONVLSTM	✓	✓	observation	6.29	1.60	102
ABED-SSH	✗	✓	both	6.27	1.85	110
ABED-SSH-SST	✓	✓	both	5.74	1.61	102

Architecture

Attention-Based Encoder-Decoder (ABED).

- Two encoding blocks reducing spatial dimensions
- Spatio-Temporal Attention modules (*inspired by CBAM*)
 - Temporal attention : performs channel and temporal attention together
 - Spatial attention
- Decoding blocks to increase spatial dimensions

