

$[STUDENT, MODULE]$
 $LEVEL ::= I \mid C \mid H \mid M$
 $next_lower == \{M \mapsto H, H \mapsto C, C \mapsto I\}$

$prereq : MODULE \leftrightarrow MODULE$

$prereq^+ \cap id\ MODULE = \emptyset$

$level : MODULE \rightarrow LEVEL$
 $no_mods : STUDENT \rightarrow (STUDENT \leftrightarrow MODULE) \rightarrow LEVEL \leftrightarrow \mathbb{N}$

$\forall s : STUDENT; r : STUDENT \leftrightarrow MODULE; l : LEVEL \mid$
 $r \llbracket \{s\} \rrbracket \cap level \sim \llbracket \{l\} \rrbracket \in \mathbb{F}\ MODULE \bullet$
 $no_mods\ s\ r\ l = \#(r \llbracket \{s\} \rrbracket \cap level \sim \llbracket \{l\} \rrbracket)$

$Enrolled$
 $enrolled : \mathbb{F}\ STUDENT$
 $module : \mathbb{F}\ MODULE$
 $registered : STUDENT \leftrightarrow MODULE$
 $registered \in enrolled \leftrightarrow module$

$EnrolledP$
 $Enrolled$
 $passed : STUDENT \leftrightarrow MODULE$
 $passed \subseteq registered$
 $\forall r : registered \bullet \{first\ r\} \times prereq \llbracket \{second\ r\} \rrbracket \subseteq passed$

$Enrol$
 $\Delta Enrolled$
 $e? : STUDENT$
 $e? \notin enrolled$
 $enrolled' = enrolled \cup \{e?\}$
 $module' = module$
 $registered' = registered$

$Register$
 $\Delta Enrolled$
 $e? : STUDENT$
 $m? : MODULE$
 $e? \in enrolled$
 $m? \in module \setminus registered \llbracket \{e?\} \rrbracket$
 $enrolled' = enrolled$
 $module' = module$
 $registered' = registered \cup \{e? \mapsto m?\}$

RegisterP

$\Delta EnrolledP$

Register

$passed' = passed$

Deregister

$\Delta Enrolled$

$e? : STUDENT$

$m? : MODULE$

$e? \in enrolled$

$m? \in registered \setminus \{e?\}$

$registered' = registered \setminus \{e? \mapsto m?\}$

Transfer

$\Delta Enrolled$

$e? : STUDENT$

$from? : MODULE$

$to? : MODULE$

$e? \mapsto from? \in registered$

$to? \in module \setminus \{from?\}$

$e? \mapsto to? \notin registered$

$registered' = registered \setminus \{e? \mapsto from?\} \cup \{e? \mapsto to?\}$

$enrolled' = enrolled$

$module' = module$