

$$\begin{aligned}
A &== [ns : \mathbb{F}\mathbb{N}_1] \\
AInit &== [A' \mid ns' = \emptyset] \\
New &== [\Delta A; n? : \mathbb{N}_1 \mid ns' = ns \cup \{n?\}] \\
MSF &== [\Xi A; m! : \mathbb{N}_1 \mid ns \neq \emptyset; m! = \max ns]
\end{aligned}$$

Injective seq ensures the 2 msf are unique.

$AM2SF$
ΞA $m1!, m2! : \mathbb{N}_1$
<hr/> $\# ns > 1$ $m1! = \max ns$ $m2! = \max (ns \setminus \{m1!\})$

$C3$
$cs : \text{iseq } \mathbb{N}_1$
<hr/> $(- < -) \circ cs \subseteq cs \circ (- < -)$

$$LI3 == [A; C3 \mid ns = \text{ran } cs]$$

Note $cs \setminus \langle ma! \rangle$ is not equivalent,
because a sequence is a function, and the domain mapping of $\langle ma! \rangle$ is different
to cs

$C3MSF2$
$\Xi C3; ma!, mb! : \mathbb{N}_1$
<hr/> $\#(\text{ran } cs) \geq 2$ $ma! = \text{last } cs$ $mb! = cs (\# cs - 1)$