

## Relationship Between Energy, Momentum, Wavelength

Momentum ( $p$ ) to classical kinetic energy ( $E$ ):

$$E = \frac{p^2}{2m}$$

Energy to wavelength (De Broglie) [1]:

$$\lambda = \frac{h}{p}$$

## Spherical Harmonics

Due to a spherical shaped electrical force field, we cannot just use sine waves in 1D, but we need the 3D version, spherical harmonics [1]. We see this when we compute quantum energy levels and states for the hydrogen atom [2].

From spherical harmonics, we get three important quantum numbers.  $n$  is the principal quantum number representing energy levels.  $l$  is the quantum number representing angular momentum.  $m$  is the quantum number representing angular momentum projection (or magnetic orbital quantum number) [3].

## Bibliography

- [1] “The Schrödinger Equation.” [Online]. Available: [https://math.libretexts.org/Bookshelves/Differential\\_Equations/Differential\\_Equations\\_\(Chasnov\)/09%3A\\_Partial\\_Differential\\_Equations/9.08%3A\\_The\\_Schrodinger\\_Equation](https://math.libretexts.org/Bookshelves/Differential_Equations/Differential_Equations_(Chasnov)/09%3A_Partial_Differential_Equations/9.08%3A_The_Schrodinger_Equation)
- [2] “The Hydrogen Atom.” [Online]. Available: [https://phys.libretexts.org/Bookshelves/University\\_Physics/University\\_Physics\\_\(OpenStax\)/University\\_Physics\\_III\\_-\\_Optics\\_and\\_Modern\\_Physics\\_\(OpenStax\)/08%3A\\_Atomic\\_Structure/8.02%3A\\_A\\_The\\_Hydrogen\\_Atom](https://phys.libretexts.org/Bookshelves/University_Physics/University_Physics_(OpenStax)/University_Physics_III_-_Optics_and_Modern_Physics_(OpenStax)/08%3A_Atomic_Structure/8.02%3A_A_The_Hydrogen_Atom)
- [3] “Orbital Magnetic Dipole Moment of the Electron.” [Online]. Available: [https://phys.libretexts.org/Bookshelves/University\\_Physics/University\\_Physics\\_\(OpenStax\)/University\\_Physics\\_III\\_-\\_Optics\\_and\\_Modern\\_Physics\\_\(OpenStax\)/08%3A\\_Atomic\\_Structure/8.03%3A\\_Orbital\\_Magnetic\\_Dipole\\_Moment\\_of\\_the\\_Electron](https://phys.libretexts.org/Bookshelves/University_Physics/University_Physics_(OpenStax)/University_Physics_III_-_Optics_and_Modern_Physics_(OpenStax)/08%3A_Atomic_Structure/8.03%3A_Orbital_Magnetic_Dipole_Moment_of_the_Electron)