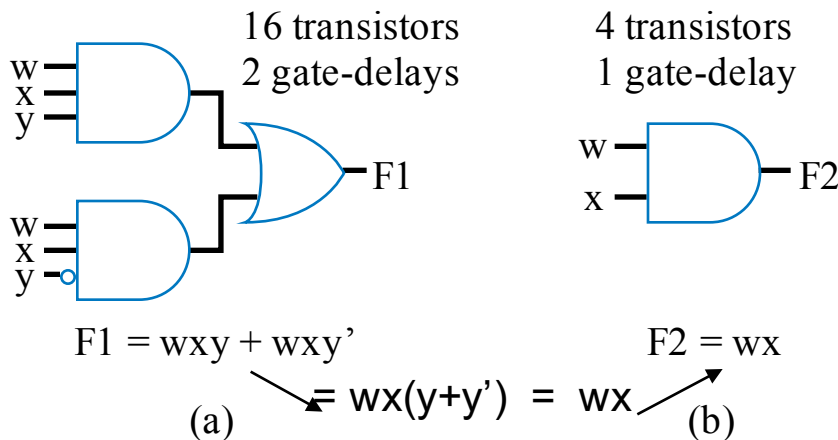


# Topic 4

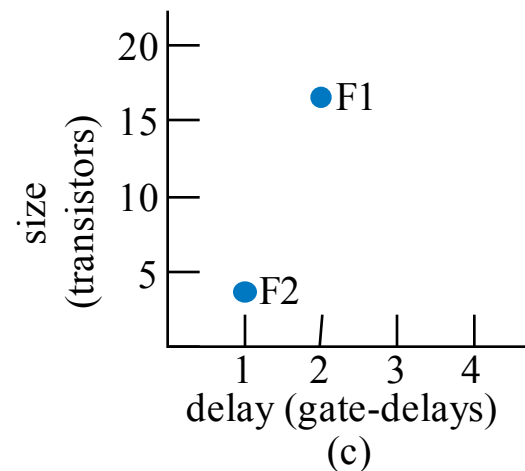
## Logic Optimization

# Simplification and Optimization

- **How can we build better circuits?**
- **Let's consider two important design criteria**
  - **Delay** – the time from inputs changing to new correct stable output
  - **Size** – the number of transistors
  - For quick estimation, assume
    - Every gate has delay of “1 gate-delay”
    - Every gate *input* requires 2 transistors
    - Ignore inverters for simplicity



Transforming F1 to F2 represents an **optimization**: Better in all criteria of interest



# Logic Optimization

- **Two-level size optimization using algebraic methods**
  - Goal: circuit with only two levels (**AND-OR network**), with minimum transistors
  - Sum-of-products yields two levels
    - $F = abc + abc'$  is sum-of-products
    - $G = w(xy + z)$  is not

## Example

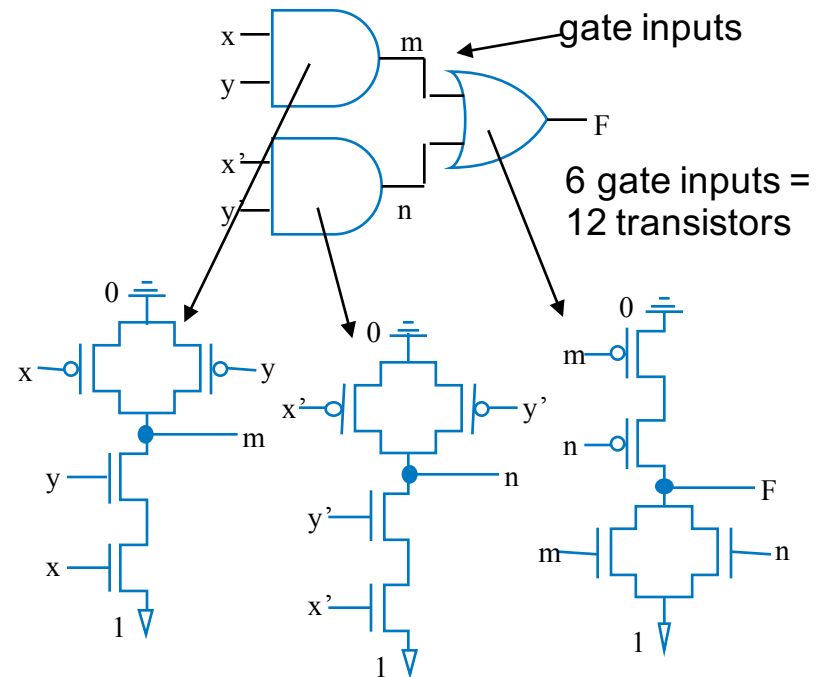
$$F = xyz + xyz' + x'y'z' + x'y'z$$

$$F = xy(z + z') + x'y'(z + z')$$

$$F = xy*1 + x'y'*1$$

$$F = xy + x'y'$$

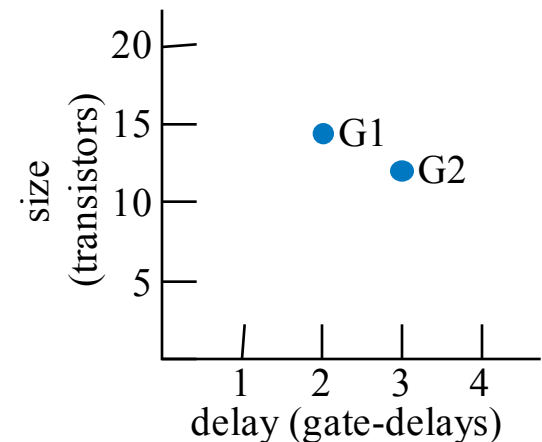
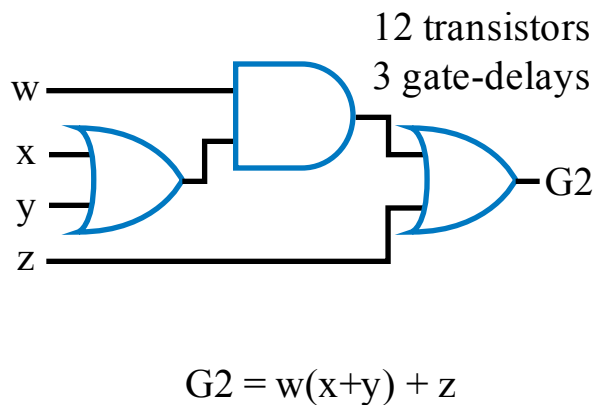
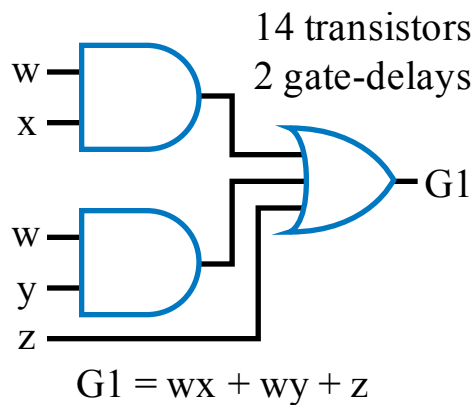
4 literals + 2 terms = 6 gate inputs



# Logic Optimization

- **Multi-level optimization**
  - Improves some, but worsens other

Transforming G1 to G2 represents a **tradeoff**. Some criteria better, others worse

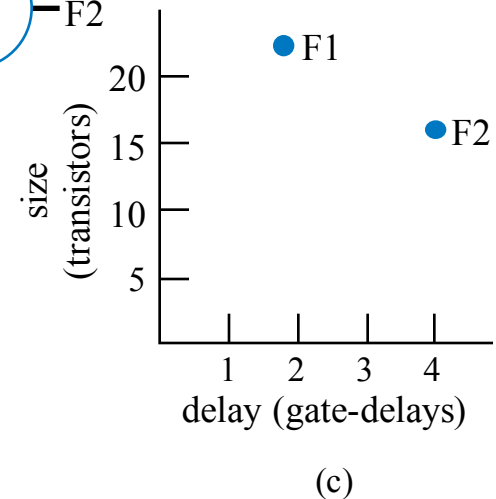
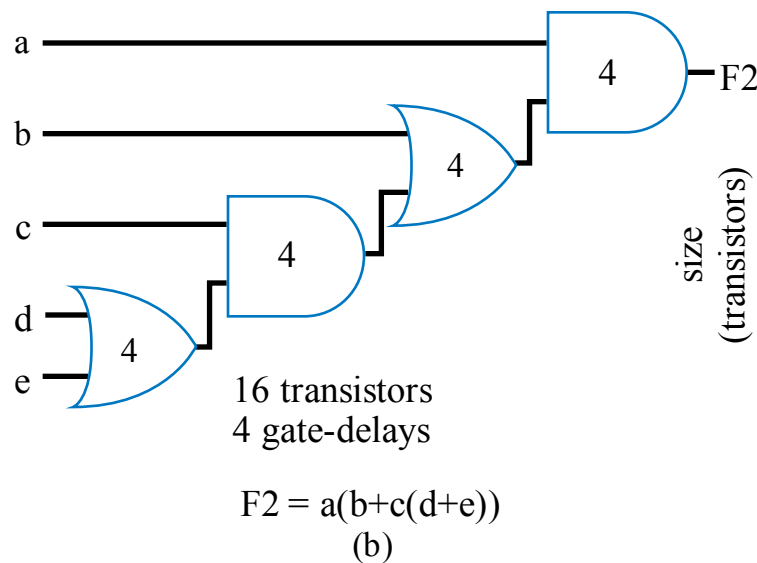
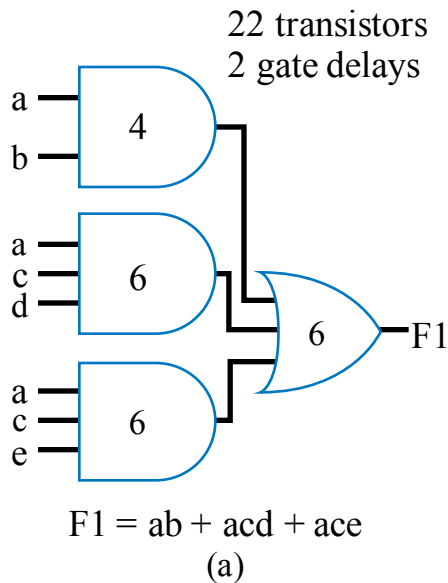


# Performance/Size Tradeoffs

- **Delay & Size tradeoff**

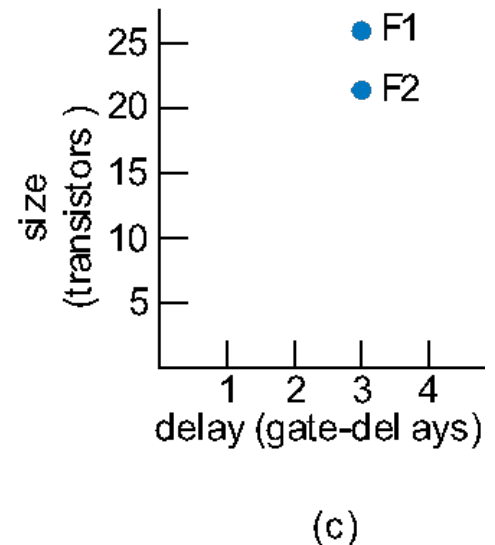
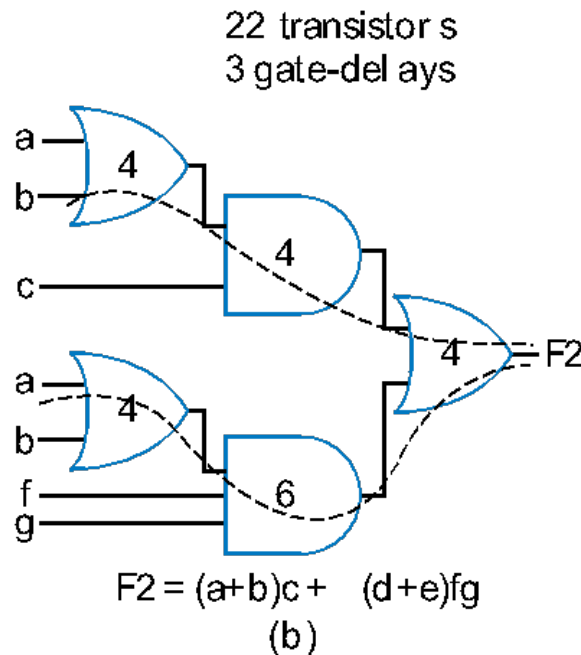
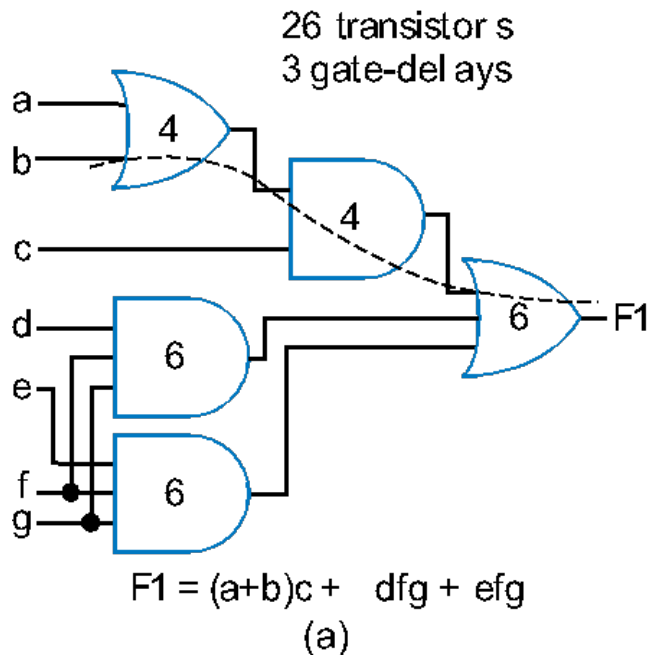
- We don't always need the speed of two level logic
- Multiple levels may yield fewer gates
- Example

- $F1 = ab + acd + ace \rightarrow F2 = ab + ac(d + e) = a(b + c(d + e))$
- General technique: Factor out literals



# Critical Path

- **Critical path:** longest delay path from an input to output
- **Optimization**
  - Reduce delay by shortening length of critical path
  - Reduce size by using multiple levels on non-critical paths
    - But may make non-critical path become critical path



# Logic Optimization

- **optimization using other techniques**
  - Karnaugh-map (later)
  - Quine-McCluskey (not in this class)

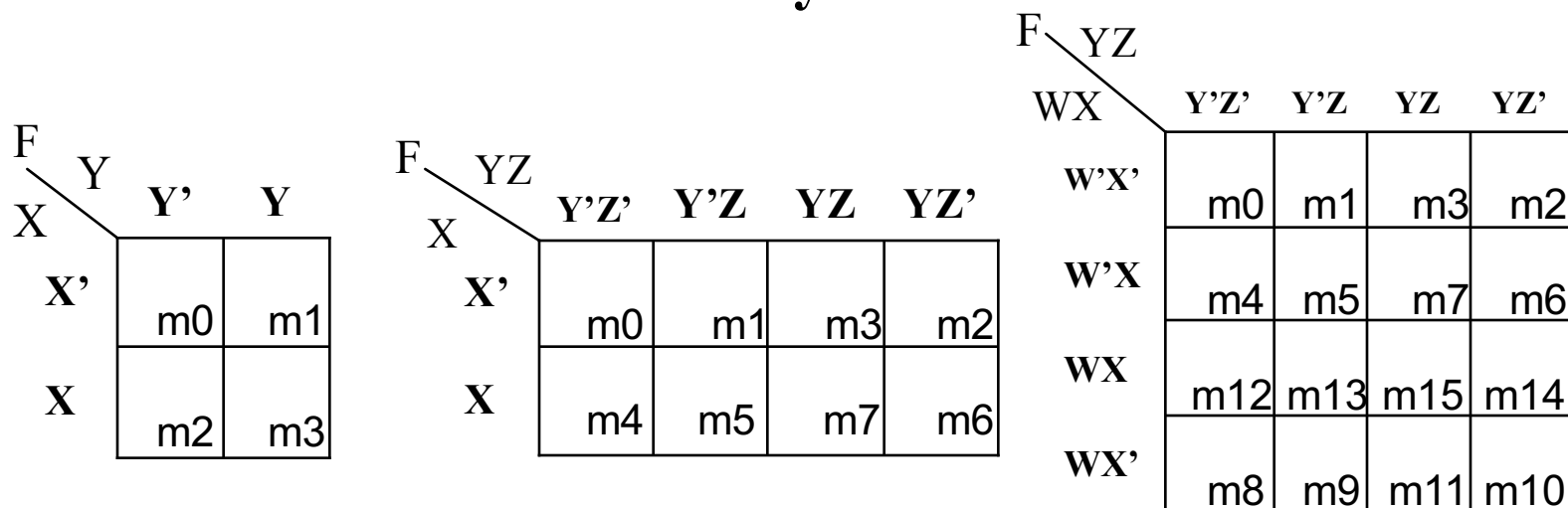
# Karnaugh Map (K-map) Technique

- A graphical technique used to *simplify* a logic equation
- A way to show the *relationship* between the logic inputs and corresponding output
  - Like truth table
- Much cleaner and more *procedural* than algebraic simplification by theorems of Boolean algebra
- Theoretically, it can be used for any number of input variables,
  - BUT is only practical for less than six, we will limit our discussion to logic equations with *five or less* variables



# Building a K-map

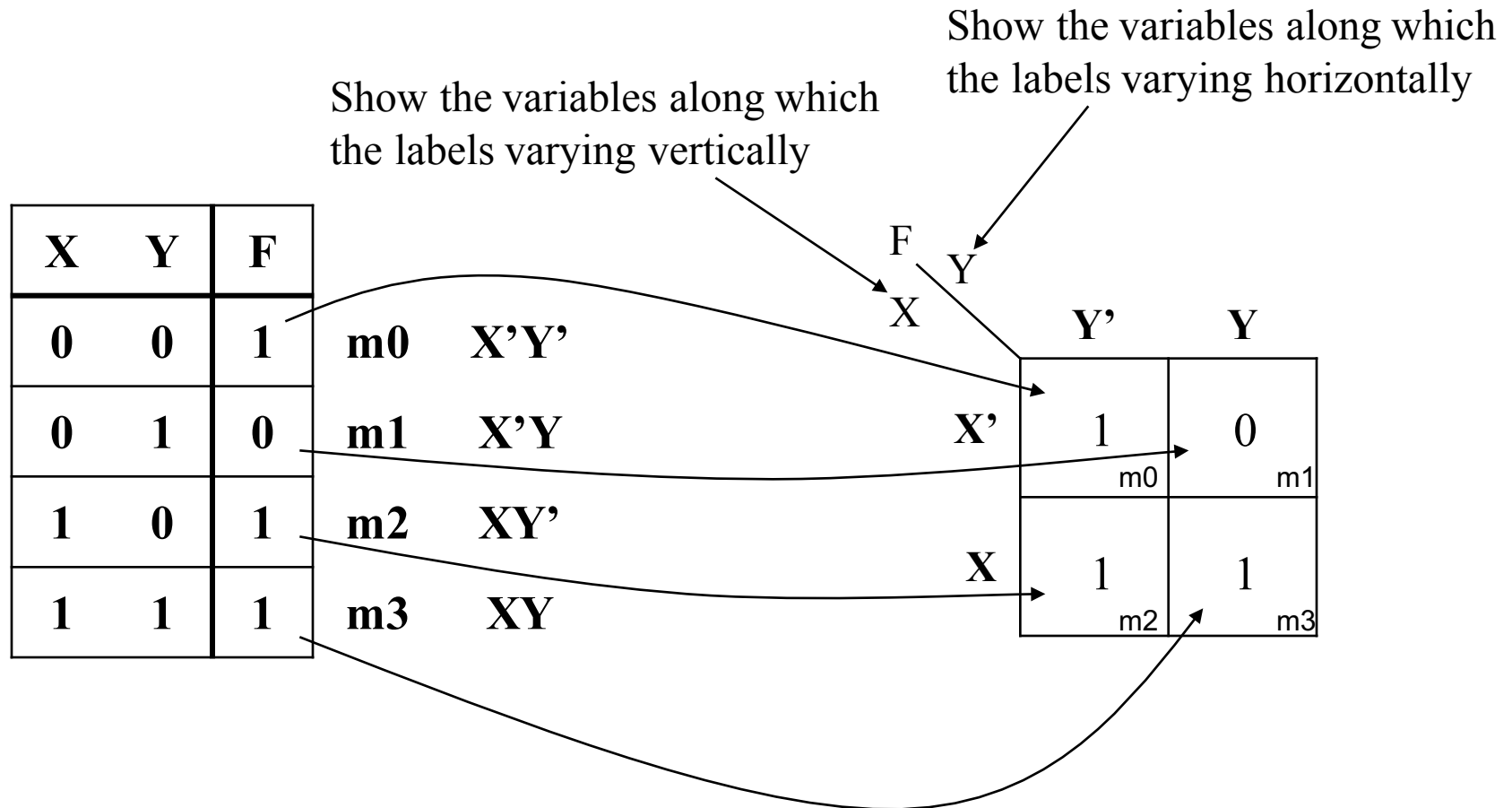
- **K-map can be filled up directly from a truth table**
  - Each minterm corresponds to a cell in the K-map
- **K-map cells are labeled so that both horizontal and vertical movement differ only in one variable**



- **Since the adjacent cells differ in only one variable, they can be grouped to create simpler terms in the sum-of-product expression.**

# Two-Variable K-map

- There are four minterms – 2 by 2 square map



# Three-Variable K-map

- There are  $2^3 = 8$  minterms – 2 by 4 rectangular map

Show the variables along which  
the labels varying vertically

Show the variables along which  
the labels varying horizontally

X	Y	Z	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

**m0**  $X'Y'Z'$   
**m1**  $X'Y'Z$   
**m2**  $X'YZ'$   
**m3**  $X'YZ$   
**m4**  $XY'Z'$   
**m5**  $XY'Z$   
**m6**  $XYZ'$   
**m7**  $XYZ$

		YZ			
	X	Y'Z'	Y'Z	YZ	YZ'
X'		1 m0	0 m1	1 m3	1 m2
X		0 m4	0 m5	1 m7	0 m6

# Four-Variable K-map

- There are  $2^4=16$  minterms – 4 by 4 square map

W	X	Y	Z	F
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

m0	$W'X'Y'Z'$
m1	$W'X'Y'Z$
m2	$W'X'YZ'$
m3	$W'X'YZ$
m4	$W'XY'Z'$
m5	$W'XY'Z$
m6	$W'XYZ'$
m7	$W'XYZ$
M8	$WX'Y'Z'$
m9	$WX'Y'Z$
M10	$WX'YZ'$
m11	$WX'YZ$
m12	$WXY'Z'$
m13	$WXY'Z$
m14	$WXYZ'$
m15	$WXYZ$

Show the variables along which the labels varying vertically or horizontally

		$Y'Z'$	$Y'Z$	$YZ$	$YZ'$
$W'X'$	1 m0	0 m1	1 m3	1 m2	
$W'X$	0 m4	0 m5	1 m7	0 m6	
$WX$	1 m12	0 m13	1 m15	0 m14	
$WX'$	1 m8	1 m9	0 m11	0 m10	

# Label the Rows and Columns by 0 and 1

F X \		Y	Y'	Y
		0	1	
X'	0	1	0	
		m0	m1	
X	1	1	1	
		m2	m3	

F X \		YZ	Y'Z'	Y'Z	YZ	YZ'
		00	01	11	10	
X'	0	1	0	1	1	
		m0	m1	m3	m2	
X	1	0	0	1	0	
		m4	m5	m7	m6	

F WX \		YZ	Y'Z'	Y'Z	YZ	YZ'
		00	01	11	10	
W'X'	00	1	0	1	1	
		m0	m1	m3	m2	
W'X	01	0	0	1	0	
		m4	m5	m7	m6	
WX	11	1	0	1	0	
		m12	m13	m15	m14	
WX'	10	1	1	0	0	
		m8	m9	m11	m10	

**0** represents the primed form  
**1** represents the unprimed form

# Simplify – Grouping and Canceling

- Group is in shape of rectangle or square
- Group the adjacent 1's until all the 1's are grouped

		Y	
F		0	1
X	0	1	0
X'Y'	1	0	0

No adjacent 1's, the  
minterm cannot be  
further simplified:  
 $F = X'Y'$

		Y	
F		0	1
X	0	1	1
X'	1	0	0

Two adjacent 1's:  
 $F = X'Y' + X'Y$   
 $= X'(Y' + Y)$   
 $= X' \cdot 1$   
 $= X'$

**If both primed and unprimed forms of a letter appear in the same group, the letter can be canceled**

A group corresponds to a Sum-of-Minterm expression

# Grouping and Canceling

- No zeros in the group**

F \ YZ		X			
		00	01	11	10
0	0	0	1	1	0
	1	0	0	1	0

*(A 2x2 group of 1s in the top-right quadrant is circled in black, but the entire table is crossed out with a large red X.)*

F \ YZ		X			
		00	01	11	10
0	0	0	1	1	0
	1	0	0	1	0

*(A 2x2 group of 1s in the top-right quadrant is circled in red, and a 2x1 group of 1s in the bottom-right quadrant is circled in blue.)*

- The number of 1's in the group should be  $2^N$ ,  $N = 0, 1, 2, \dots$**

F \ YZ		X			
		00	01	11	10
0	0	1	1	1	0
	1	0	0	0	0

*(A 1x3 group of 1s in the top-left quadrant is circled in black, but the entire table is crossed out with a large red X.)*

F \ YZ		X			
		00	01	11	10
0	0	1	1	1	0
	1	0	0	0	0

*(A 1x3 group of 1s in the top-left quadrant is circled in red, and a 1x2 group of 1s in the top-middle is circled in blue.)*

# Grouping and Canceling

- Group as many adjacent 1's as possible

Redundant term

		YZ		X'Z		
F	X	00	01	11	10	
0		0	1	1	0	
1		0	0	1	0	

YZ

$$\begin{aligned}
 F &= X'Y'Z + X'YZ + XYZ \\
 &= (X'Y'Z + X'YZ) + (X'YZ + XYZ) \\
 &= X'Z(Y' + Y) + YZ(X' + X) \\
 &= X'Z + YZ
 \end{aligned}$$

Redundant terms

		YZ			
F	X	00	01	11	10
0		1	1	1	1
X'	1	0	0	1	1

Y

$$\begin{aligned}
 F &= X'Y'Z' + X'Y'Z + X'YZ + X'YZ' + XYZ + XYZ' \\
 &= (X'Y'Z' + X'Y'Z + X'YZ + X'YZ') + \\
 &\quad (X'YZ + X'YZ' + XYZ + XYZ') \\
 &= (X'Y' + X'Y) + (X'Y + XY) \\
 &= X' + Y
 \end{aligned}$$



# Grouping and Canceling

- Group as many adjacent 1's as possible

$F$   $YZ$   
 $WX$

	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	0	1	0
10	1	0	0	0

$W'$ , because  
 horizontally, both  $Y$  and  $Y'$  appear,  $Y$  cancels  
 both  $Z$  and  $Z'$  are included,  $Z$  cancels;  
 vertically, both  $X$  and  $X'$  appear,  $X$  cancels.  
 That leaves the 0 for  $W$  – primed  $W$ .

$XYZ$ , because  
 only  $W$  and  $W'$  appear,  $W$  cancels.  
 The remaining term 111 implies  $XYZ$

$Y'Z'$ , because  
 both  $W$  and  $W'$  appear, and both  $X$  and  $X'$  appear,  
 So  $W$  and  $X$  cancel.  
 That leaves the 00 for  $YZ$  – primed  $Y$  and primed  $Z$ .

# Grouping and Canceling

- Edges wrap around

		YZ			
		00	01	11	10
X	0	1	0	0	1
	1	1	0	0	1

$$F = Z'$$

		YZ			
		00	01	11	10
WX	00	1	0	0	1
	01	1	0	0	1
	11	0	0	0	0
	10	1	0	0	1

$$F = \mathbf{W'Z'} + \mathbf{X'Z'}$$

# Grouping and Canceling

- **Summary**

- Group is in shape of rectangle or square
- Group the adjacent 1's until all the 1's are grouped
- The number of 1's in the group should be  $2^N$ ,  $N = 0, 1, 2, \dots$
- Collect as many 1's as possible in the same group
- No zeros in the group
- Edges wrap around
- If both primed and unprimed forms of a letter appear in a same group, the letter cancels
- The simplified result will be a sum-of-product form; the number of the product terms is decided by the number of the groups

# Group Patterns of 2-Variable Map

	0	1
0	1	0
1	0	1

	0	1
0	1	1
1	0	0

	0	1
0	0	1
1	0	1

	0	1
0	1	1
1	1	1

- **Summary**

- A group of one cell represents a minterm, giving a term of two literals
- A group of two cells represents a term of one literal
- A group of all the four cells gives a logic 1

# Group Patterns of 3-Variable Map

	00	01	11	10
0	1	0	1	0
1	0	1	0	1

	00	01	11	10
0	1	1	1	0
1	0	0	1	1

	00	01	11	10
0	1	1	0	1
1	1	1	1	

	00	01	11	10
0	1	1	1	1
1	1	0	0	1

	00	01	11	10
0	1	1	1	1
1	1	1	1	0

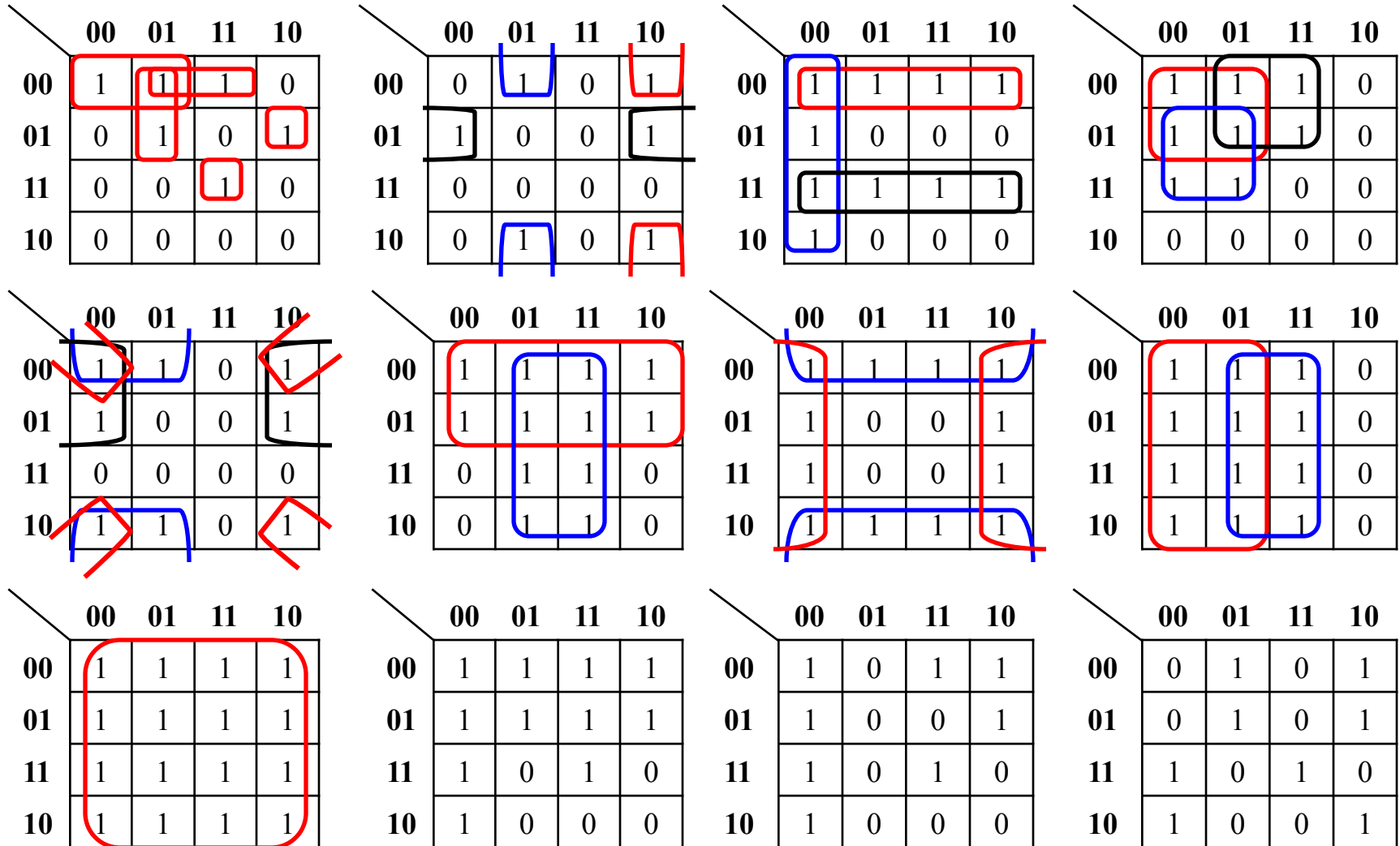
	00	01	11	10
0	1	1	1	1
1	1	1	1	1

# Group Patterns of 3-Variable Map

- **Summary**

- A group of one cell represents a minterm, giving a term of three literals
- A group of two cells represents a term of two literals
- A group of four cells represents a term of one literal
- A group of all the eight cells gives a logic 1

# Group Patterns of 4-Variable Map



# Group Patterns of 4-Variable Map

- **Summary**
  - A group of one cell represents a minterm, giving a term of four literals
  - A group of two cells represents a term of three literals
  - A group of four cells represents a term of two literals
  - A group of eight cells represents a term of one literal
  - A group of all the sixteen cells gives a logic 1
- **The more the number of cells in one group, the less the number of literals that group represents, hence cheaper to implement using logic gates**



# Prime Implicants

- Implicant: is a product term
- A **prime implicant (PI)** is a group that cannot be entirely contained by another implicant

F	YZ			
	00	01	11	10
WX	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	0	0	0	0
10	0	0	0	0

— Prime implicant

..... Not prime implicants

F	YZ			
	00	01	11	10
WX	00	01	11	10
00	1	1	1	0
01	0	0	1	0
11	0	0	0	0
10	0	0	0	1

# Essential Prime Implicants

- A **prime implicant (PI)** is **essential** if a cell is covered **ONLY** by that PI
- The **essential PIs** can be found by
  - looking at each cell marked as 1 and not covered by any other essential PI
  - and checking the number of PIs that cover it

F YZ WX		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	1	1	1

# Essential Prime Implicants

- Check each cell marked as 1, only if it has not been covered by an essential PI

		F YZ			
WX		00	01	11	10
	00	<b>1</b>	0	1	<b>1</b>
	01	0	1	1	0
	11	0	1	1	0
	10	<b>1</b>	1	1	<b>1</b>

Essential PI:  $X'Z'$

		F YZ			
WX		00	01	11	10
	00	<b>1</b>	0	<b>1</b>	<b>1</b>
	01	0	1	1	0
	11	0	1	1	0
	10	<b>1</b>	1	<b>1</b>	<b>1</b>

No essential PIs found

# Essential Prime Implicants

F		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	<b>1</b>	1	0
	11	0	1	1	0
	10	1	1	1	1

Essential PI: XZ

F		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	<b>1</b>	1	1

No essential PIs found

# Essential Prime Implicants

F		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	1	<b>1</b>	1

No essential PIs found

# Essential Prime Implicants

F \ WX \ YZ		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	1	1	1

Essential PIs

F \ WX \ YZ		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	1	1	0
	11	0	1	1	0
	10	1	1	1	1

Non essential PIs

- **Essential PIs have to be used in the simplified equation**
- **Cells not covered by essential PIs can be represented by any PIs covering them**

$$F = X'Z' + XZ + WX'(\text{or } WZ) + X'Y(\text{or } YZ)$$

# Product-of-Sum Simplification – An Alternate Method

- Redraw the K-map for  $F'$  by switching 1's and 0's

W	X	Y	Z	F	F'
0	0	0	0	1	0
0	0	0	1	1	0
0	0	1	0	1	0
0	0	1	1	1	0
0	1	0	0	0	1
0	1	0	1	0	1
0	1	1	0	0	1
0	1	1	1	1	0
1	0	0	0	1	0
1	0	0	1	1	0
1	0	1	0	0	1
1	0	1	1	0	1
1	1	0	0	1	0
1	1	0	1	0	1
1	1	1	0	0	1
1	1	1	1	0	1

		F			
		YZ			
WX		00	01	11	10
	00	1	1	1	1
	01	0	0	1	0
	11	1	0	0	0
	10	1	1	0	0

		F'			
		YZ			
WX		00	01	11	10
	00	0	0	0	0
	01	1	1	0	1
	11	0	1	1	1
	10	0	0	1	1

# Product-of-Sum Simplification – An Alternate Method

- Two forms of the same truth table

F		YZ			
WX		00	01	11	10
		00	01	11	10
00		1	1	1	1
01		0	0	1	0
11		1	0	0	0
10		1	1	0	0

Sum-of-Product form:

$$F = \underline{W'X'} + \underline{X'YZ} + \underline{WY'Z'} + \underline{W'YZ}$$

F'		YZ			
WX		00	01	11	10
		00	01	11	10
00		0	0	0	0
01		1	1	0	1
11		0	1	1	1
10		0	0	1	1

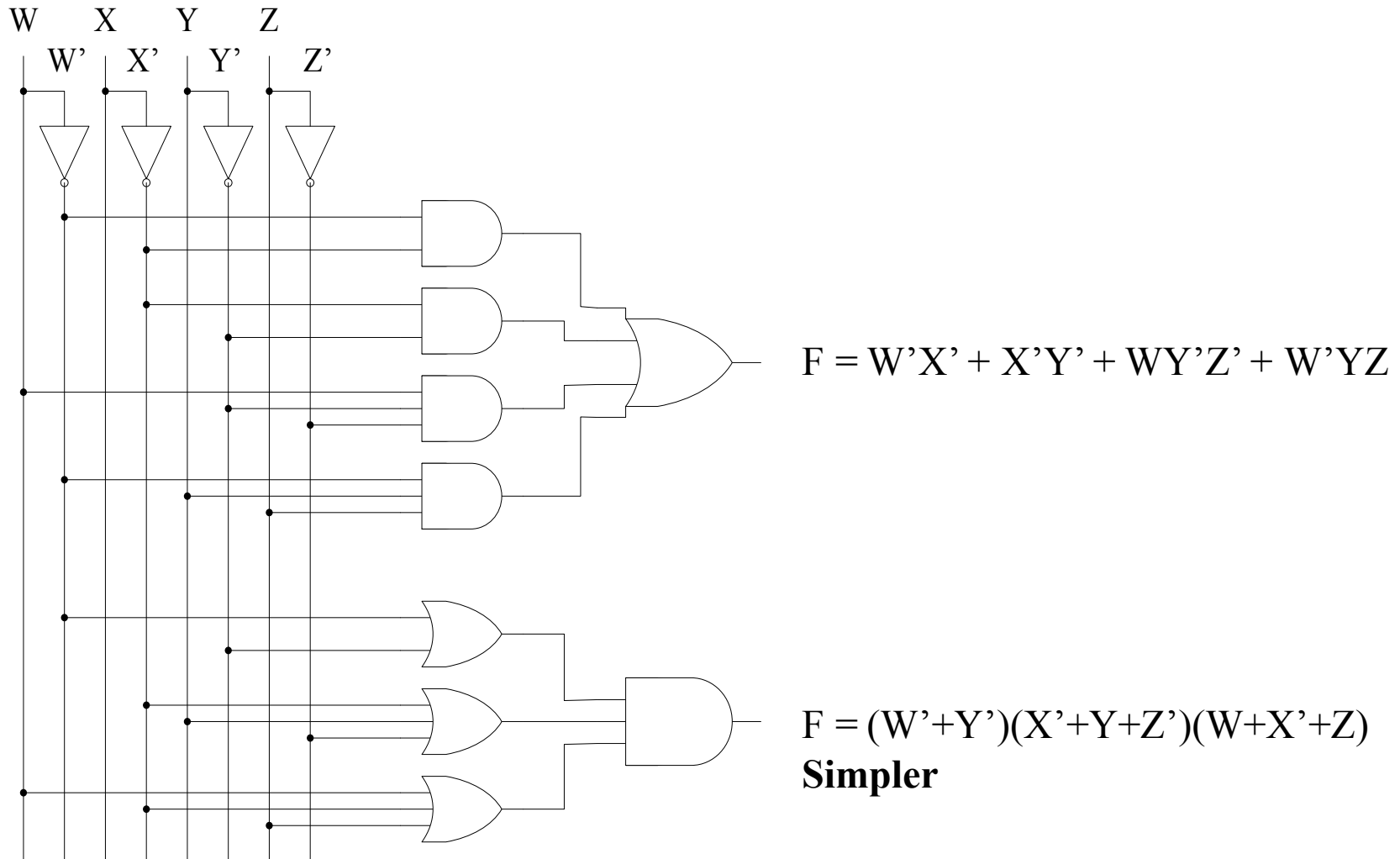
$$F' = \underline{WY} + XY'Z + W'XZ'$$

Product-of-Sum form:

$$\begin{aligned}
 F &= (F')' && \text{(DeMorgan's Law)} \\
 &= (WY + XY'Z + W'XZ')' \\
 &= (WY)' (XY'Z)' (W'XZ')' \\
 &= (W' + Y')(X' + Y + Z')(W + X' + Z)
 \end{aligned}$$



# Product-of-Sum Simplification – An Alternate Method



# Simplify Any Standard Sum-of-Product Form

**Method 1: fill out the table directly**

- $F = A'C + A'BD + AB'C + BCD$



A	B	C	D	F	
0	0	0	0	0	m0
0	0	0	1	0	m1
0	0	1	0	1	m2
0	0	1	1	1	m3
0	1	0	0	0	m4
0	1	0	1	1	m5
0	1	1	0	1	m6
0	1	1	1	1	m7
1	0	0	0	0	m8
1	0	0	1	0	m9
1	0	1	0	1	m10
1	0	1	1	1	m11
1	1	0	0	0	m12
1	1	0	1	0	m13
1	1	1	0	0	m14
1	1	1	1	1	m15

F	CD			
	00	01	11	10
AB				
00	0	0	1	1
01	0	1	1	1
11	0	0	1	0
10	0	0	1	1



# Simplify Any Standard Sum-of-Product Form

- **$F = A'C + A'BD + AB'C + BCD$** 
  - **Method 2: convert any form of equation to sum-of-minterm**
    - AND with sum of the primed and unprimed forms of the missing literal, one at a time until all the missing literals are considered
    - Remove the duplicated minterms

$$\begin{aligned} F &= A'C + A'BD + AB'C + BCD \\ &= A'C (B+B') + A'BD (C+C') + AB'C (D+D') + BCD (A+A') \\ &= A'BC + A'B'C + A'BCD + A'BC'D + AB'CD + \\ &\quad AB'CD' + ABCD + A'BCD \\ &= A'BC (D+D') + A'B'C (D+D') + A'BCD + A'BC'D + AB'CD + \\ &\quad AB'CD' + ABCD + A'BCD \\ &= A'BCD + A'BCD' + A'B'CD + A'B'CD' + A'BCD + A'BC'D + \\ &\quad AB'CD + AB'CD' + ABCD + A'BCD \\ &= \Sigma m(7, 6, 3, 2, 7, 5, 11, 10, 15, 7) \\ &= \Sigma m(2, 3, 5, 6, 7, 10, 11, 15) \end{aligned}$$

# Simplify Any Standard Sum-of-Product Form

- $F = A'C + A'BD + AB'C + BCD$

A	B	C	D	F	
0	0	0	0	0	m0
0	0	0	1	0	m1
0	0	1	0	1	m2
0	0	1	1	1	m3
0	1	0	0	0	m4
0	1	0	1	1	m5
0	1	1	0	1	m6
0	1	1	1	1	m7
1	0	0	0	0	m8
1	0	0	1	0	m9
1	0	1	0	1	m10
1	0	1	1	1	m11
1	1	0	0	0	m12
1	1	0	1	0	m13
1	1	1	0	0	m14
1	1	1	1	1	m15

F		CD			
		00	01	11	10
AB	00	0	0	1	1
	01	0	1	1	1
	11	0	0	1	0
	10	0	0	1	1

After simplification:

$$F = A'C + A'BD + B'C + CD$$

(Essential PI?)

# Don't Care Conditions

- The possible input combinations might not be all valid or not for consideration for a device
  - Hence we don't care what the corresponding outputs are under those conditions
  - Called **don't care** conditions
  - Mark the corresponding outputs by **X**

A	B	C	D	F
<i>0</i>	<i>0</i>	<i>0</i>	<i>0</i>	<i>X</i>
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
<i>1</i>	<i>0</i>	<i>0</i>	<i>1</i>	<i>X</i>
1	0	1	0	1
1	0	1	1	1
<i>1</i>	<i>1</i>	<i>0</i>	<i>0</i>	<i>X</i>
<i>1</i>	<i>1</i>	<i>0</i>	<i>1</i>	<i>X</i>
<i>1</i>	<i>1</i>	<i>1</i>	<i>0</i>	<i>X</i>
1	1	1	1	1

# Don't Care Conditions

- By employing **don't care** conditions, logic equations can be further simplified

- Example:

$$F(A, B, C, D) = \sum m(2, 3, 5, 6, 7, 10, 11, 15) + \sum d(0, 9, 12, 13, 14)$$

- Fill out the K-map with 1's and X's
  - Each "X" can be either 0 or 1 depending upon the needs of simplification
  - Not all X's have to be considered
- Apply the same grouping and canceling rules before using 'X':  $F = A'C + A'BD + B'C + CD$   
after:  $F = C + BD$  (Essential PI?)

F		CD			
		00	01	11	10
AB	00	X <sub>0</sub>	0 <sub>1</sub>	1 <sub>3</sub>	1 <sub>2</sub>
	01	0 <sub>4</sub>	1 <sub>5</sub>	1 <sub>7</sub>	1 <sub>6</sub>
	11	X <sub>12</sub>	1 <sub>13</sub>	1 <sub>15</sub>	1 <sub>14</sub>
	10	0 <sub>8</sub>	X <sub>9</sub>	1 <sub>11</sub>	1 <sub>10</sub>

# Dealing with Five Variables

<i>E</i>	A	B	C	D	F
0	0	0	0	0	X
0	0	0	0	1	0
0	0	0	1	0	1
0	0	0	1	1	1
0	0	1	0	0	0
0	0	1	0	1	1
0	0	1	1	0	1
0	0	1	1	1	1
0	1	0	0	0	0
0	1	0	0	1	X
0	1	0	1	0	1
0	1	0	1	1	1
0	1	1	0	0	X
0	1	1	0	1	X
0	1	1	1	0	X
0	1	1	1	1	1

<i>E</i>	A	B	C	D	F
1	0	0	0	0	1
1	0	0	0	1	1
1	0	0	1	0	0
1	0	0	1	1	X
1	0	1	0	0	X
1	0	1	0	1	1
1	0	1	1	0	0
1	0	1	1	1	0
1	1	0	0	0	1
1	1	0	0	1	X
1	1	0	1	0	1
1	1	0	1	1	0
1	1	1	0	0	1
1	1	1	0	1	1
1	1	1	1	0	X
1	1	1	1	1	0

***E'***

F \ CD \ AB	00	01	11	10
00	X <sub>0</sub>	0 <sub>1</sub>	1 <sub>3</sub>	1 <sub>2</sub>
01	0 <sub>4</sub>	1 <sub>5</sub>	1 <sub>7</sub>	1 <sub>6</sub>
11	X <sub>12</sub>	X <sub>13</sub>	1 <sub>15</sub>	X <sub>14</sub>
10	0 <sub>8</sub>	X <sub>9</sub>	1 <sub>11</sub>	1 <sub>10</sub>

***E***

F \ CD \ AB	00	01	11	10
00	1 <sub>0</sub>	1 <sub>1</sub>	X <sub>3</sub>	0 <sub>2</sub>
01	X <sub>4</sub>	1 <sub>5</sub>	0 <sub>7</sub>	0 <sub>6</sub>
11	1 <sub>12</sub>	1 <sub>13</sub>	0 <sub>15</sub>	X <sub>14</sub>
10	1 <sub>8</sub>	X <sub>9</sub>	1 <sub>11</sub>	0 <sub>10</sub>

$$F = E'(C+BD) + E(C'+B'D)$$

# Power Optimization

- **Power is another important design criteria**
  - Measured in Watts (energy/second)
    - Rate at which energy is consumed
- **Increasingly important as more transistors on a chip**
  - Power not scaling down at same rate as size
    - cooling is difficult
  - CMOS technology: Switching a wire from 0 to 1 consumes power (known as *dynamic power*)
    - $P = k * CV^2f$ 
      - k: constant; C: capacitance of wires; V: voltage; f: switching frequency
    - Power reduction methods
      - Reduce voltage: But slower, and there's a limit
      - What else?



# Using Low-Power Gates on Non-Critical Paths

- **Another method: Use low-power gates**
  - Multiple versions of gates may exist
    - Fast/high-power, and slow/low-power, versions
  - Use **slow/low-power gates on non-critical paths**
    - Reduces power, without increasing delay

