
AML: Semester project presentation

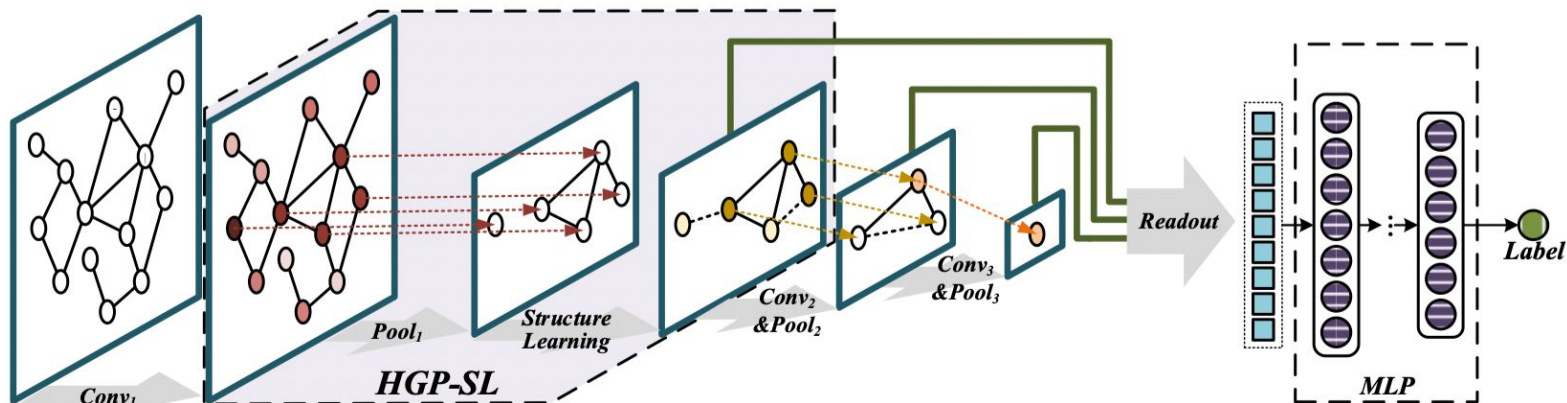
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Project Overview: A GNN project

Goal of this project: Explore possibilities of improving the approach of the paper **Hierarchical Graph Pooling with Structure Learning** by Zhang et al. (2019).



Problem formulation

Bioinformatics: Protein structures can be modeled as graph (nodes = amino acids).

- Two nodes are less than six Angstroms apart \rightarrow there is an edge between them

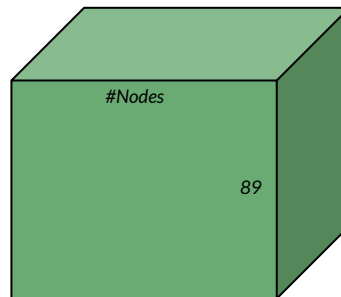
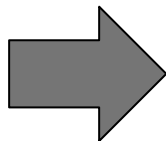
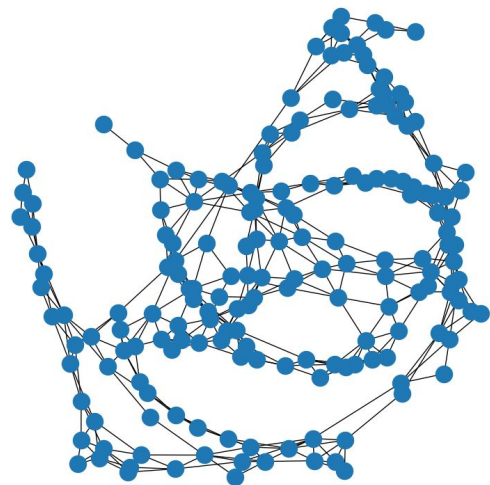
The **D&D dataset**:

- $n = 1178$ protein graphs $G = \{G_1, G_2, \dots, G_n\}$
- A protein graph has the structure $G_i = (V_i, E_i, X_i)$ with n_i nodes and e_i edges:
 - $X_i \in \mathbb{R}^{n_i \times f}$ represents the node feature matrix, f is the dimension of the node attributes
 - **Binary classification:** Graph is an enzyme or not \rightarrow target labels can be represented with label vector $\mathbf{y} \in \mathbb{R}^n$

Training: Training of model with a batch of protein graphs G_L whose label information is \mathbf{y}_L (targets)

Task and Goal: Decide if the protein graph G_i should be classified as an enzyme $y_i = 1$ or not $y_i = 0$.

Model Input (D&D Dataset)



Node/Feature Matrix



Edge Index



Label

Batch Dimension(64)

The 89 features per node include aspects like:

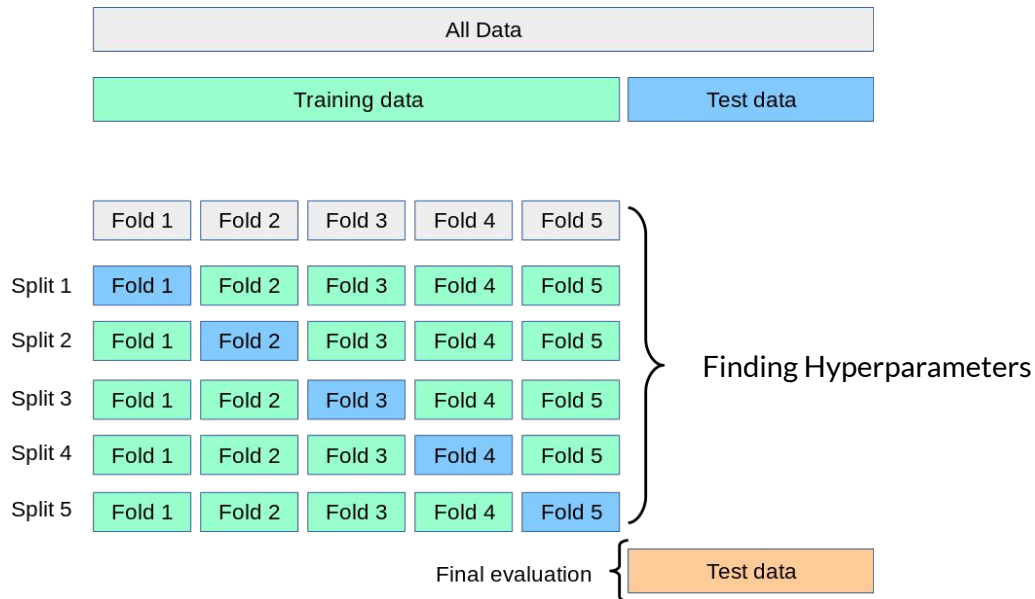
- residue preferences
- secondary structure content
- surface properties
- presence of certain ligands
- cofactors.

Planned self contributions

1. Rebuilding the proposed model from the original paper and bringing it to a newer Python version
2. Implementing the simple baseline model **Shortest-Path Kernel** by Borgwardt and Kriegel (2005)
3. The next step is to apply the following modifications and check them for possible improvements:
 1. Modify the read out function
 2. Introduce a deeper network
 3. Use a different node information score metric
 4. Different top-rank node selection (based on node information score)

Evaluation protocol and Baselines

Evaluation:



Baselines:

- **HPG-SL**: paper's baseline, 80.96%* accuracy.
- **Shortest-Path Kernel**: statistical baseline

* Different evaluation protocol

Shortest-Path Kernel Baseline

- by Borgwardt and Kriegel (2005)
- All paths \rightarrow NP-hard
- shortest path \rightarrow solvable in polynomial time $O(n^3)$
- Algorithm:
 - transform input graphs into shortest path graphs
 - **Definition 3 (Shortest-path graph kernel)** Let G_1 and G_2 be two graphs that are Floyd-transformed into S_1 and S_2 . We can then define our shortest-path graph kernel on $S_1 = (V_1, E_1)$ and $S_2 = (V_2, E_2)$ as

$$k_{\text{shortest paths}}(S_1, S_2) = \sum_{e_1 \in E_1} \sum_{e_2 \in E_2} k_{\text{walk}}^{(1)}(e_1, e_2),$$

where $k_{\text{walk}}^{(1)}$ is a positive definite kernel on edge walks of length 1.

Modifications: Deeper Network

Introduce a deeper network

- According to Zhang et al. (2019), model performs best with $K = 2$ layers
- We tried out $K = 3, 4$, and 5 layers

Motivation:

- *HGP-SL almost achieves the best performance across different datasets when setting $K = 3$, $d = 128$ and $r = 0.8$, respectively. For D&D, they have set $K = 2$.*
- Li et al. (2018): More convolutional layers do not necessarily lead to a better result
 - More layers \rightarrow more difficult to train
 - Mix of features of nodes \rightarrow makes them indistinguishable

Modification: Read out function

Modify the read out function

- Use all subgraphs as in the paper
- Use only the first subgraph
- Use only the last subgraph

$$\mathbf{r}_i^k = \mathcal{R}(\mathbf{H}_i^k) = \sigma\left(\frac{1}{n_i^k} \sum_{p=1}^{n_i^k} \mathbf{H}_i^k(p, :) \parallel \max_{q=1}^d \mathbf{H}_i^k(:, q)\right).$$

$$\mathbf{z}_i = \mathbf{r}_i^1 + \mathbf{r}_i^2 + \cdots + \mathbf{r}_i^K$$

Motivation:

- **Use all:** Used by Zhang et al. (2019) and Zhang et al. (2023)
- **First subgraph:** Node representations may be well distinguishable, but representation might be too complex to find reliable information about class assignment
- **Last subgraph:** Opposite: More convolutional layers have been used
 - Li et al. (2018): Mix of features of nodes \rightarrow makes them indistinguishable

Modifications: Node information score

Use a different node information score metric

- For the node information score, Zhang et al. (2019) use the Manhattan norm. We also tried out the Euclidean norm.

$$\mathbf{p} = \gamma(\mathcal{G}_i) = \|(\mathbf{I}_i^k - (\mathbf{D}_i^k)^{-1} \mathbf{A}_i^k) \mathbf{H}_i^k\|_1,$$

Motivation:

- Gao et al. (2022) state: *Euclidean distance as it represents a common similarity measure that is especially convenient for high-dimensional vectors that might be present in some graph data sets.*

Modifications: Node selection

Different top-rank node selection (based on node information score)

- Essentially is about modifying the pooling ratio r
- We tried out *pooling ratio* $r = 0.2, 0.5, 0.8$

$$\text{idx} = \text{top-rank}(\mathbf{p}, \lceil r * n_i^k \rceil)$$

$$\tilde{\mathbf{H}}_i^{k+1} = \mathbf{H}_i^k(\text{idx}, :)$$

$$\mathbf{A}_i^{k+1} = \mathbf{A}_i^k(\text{idx}, \text{idx}),$$

Motivation:

- *r cannot be too small, otherwise most of the graph structure information will be lost during the pooling process (Zhang et al., 2019).*
- *“HGP-SL almost achieves the best performance across different datasets when setting $K = 3, d = 128$ and $r = 0.8$, respectively”*
- For D&D, r is only 0.3.

Results: One hyperparameter change

	<i>DistanceMetric</i>	<i>Layers</i>	<i>PoolingRatio</i>	<i>Readout</i>	Validation Accuracy		
					avg	min	max
(original)	Manhattan	2	0.3	ALL	76.0	74.0	79.8
(distance)	Euclidean				75.7 (-0.3)	71.6	77.8
(layers)		3			76.0 (=)	74.0	76.8
		4			76.7 (+0.7)	75.0	78.7
		5			75.5 (-0.5)	73.1	77.4
(pooling ratio)			0.8		76.9 (+0.9)	73.5	81.2
			0.5		77.0 (+1.0)	73.1	80.7
			0.2		75.0 (-1.0)	71.2	77.9
(readout)				FIRST	76.1 (+0.1)	73.5	77.4
				LAST	76.1 (+0.1)	73.1	79.7

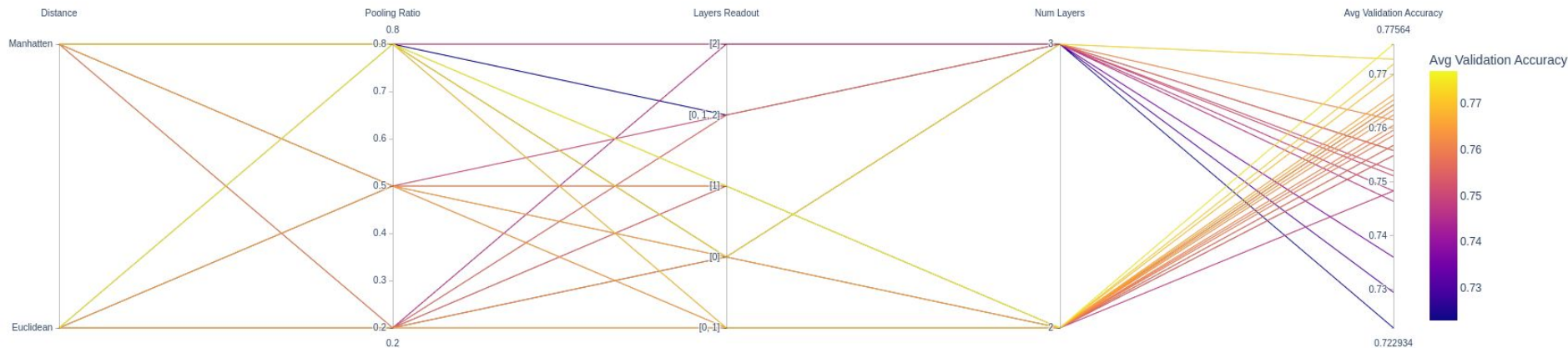
Table 1: Modifications made to the HGP-SL architecture and their evaluation through K-fold cross-validation (K=5) on the D&D dataset.

Results: Grid Search

Hyperparameter	Options	Selected Parameter
Layers	2, 3	2
Pooling Ratio	0.2, 0.5, 0.8	0.8
Distance Metric	Manhattan, Euclidean	Manhattan
Readout Layers	ALL, FIRST, LAST	LAST

Table 2: Grid Search of Hyperparameters

Results: Hyper Parameter Analysis



Only 29/35 hyperparameter combinations could be trained because of limited compute!

Results: Evaluate on Test Set

Model	Training	Test
Shortest Path Kernel	75.9	72.6
$HGP - SL_{original}$	84.4	78.6
Ours	85.6	78.6

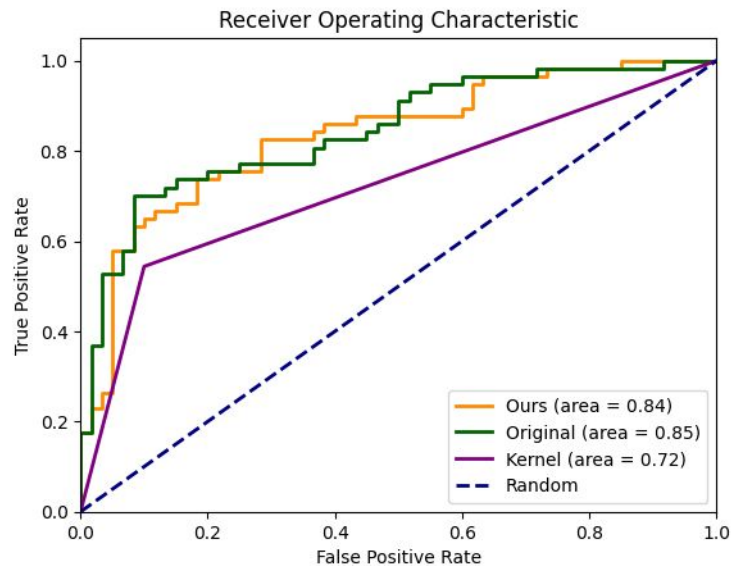
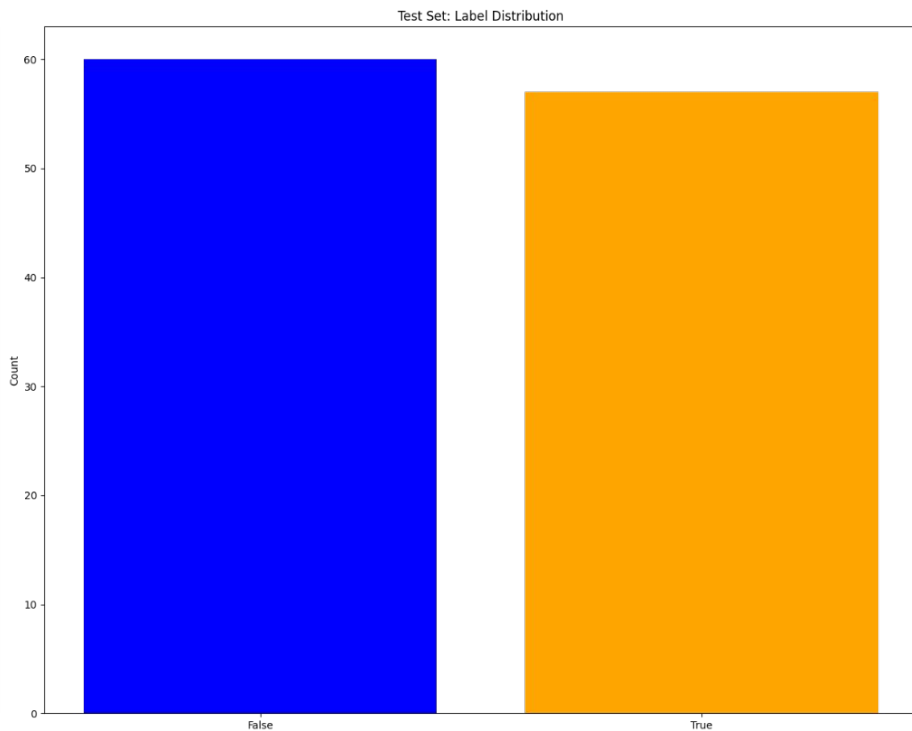
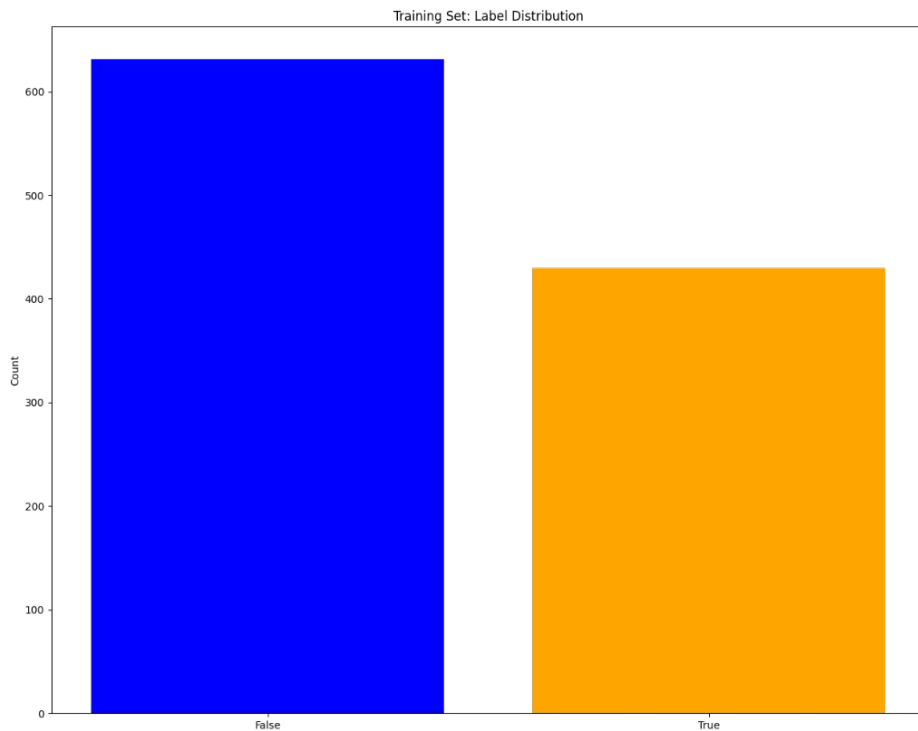


Table 3: Comparison of training and test accuracies with respect to the shortest path baseline and the original $HGP - SL$ paper.

Label distributions: Evaluation



Discussion

- Evaluation protocol (CV) has influence on accuracy data: 80.96% accuracy could not be beaten
- With 78.6% accuracy, our model has equal accuracy to HGP-SL baseline with CV. Shortest Path Kernel baseline was beaten.
- One hyperparameter change: pooling ratio = 0.5 is best
- Grid search revealed that pooling ratio = 0.8 also for DD dataset is the best
 - When considering one change at time, $r = 0.8$ is better than $r = 0.3$ used by HGP-SL baseline → keeping structure information is important
- Deeper network did not bring any improvement → too much information is lost
- Contribution of node information score metric depends on combination
- Utilize some tool for metrics and training logs
- Slightly unbalanced data set split
- Improve hyperparameter tuning: Informed tuning instead of extensive search

References

- Hierarchical Graph Pooling with Structure Learning (Zhang et al., 2019):
<https://arxiv.org/abs/1911.05954>
- Hierarchical Multi-View Graph Pooling With Structure Learning (Zhang et al., 2023):
<https://ieeexplore.ieee.org/document/9460814>
- D&D data set paper (Dobson and Doig, 2003): <https://pubmed.ncbi.nlm.nih.gov/12850146/>
- Shortest-path kernels on graphs (Borgwardt and Kriegel, 2005):
<https://www.dbs.ifi.lmu.de/~borgwardt/papers/BorKri05.pdf>
- iPool—Information-Based Pooling in Hierarchical Graph Neural Networks (Gao et al., 2022):
<https://ieeexplore.ieee.org/document/9392315>
- Deeper Insights into Graph Convolutional Networks for Semi-Supervised Learning (Li et al., 2018): <https://arxiv.org/abs/1801.07606>

Appendix: Label distributions: Training

