

Task 1

The loop runs from 2 to $n+1$. So, the total number of times loop will run will be $n + 1 - 2 = n - 1$ times. Since we don't care about constants or lower terms while calculating time complexities, in θ notation, time complexity of this function is n .

Task 2

The matlab function is saved as fact.m

```
function [factorial] = fact(x)
    if x == 1
        factorial = 1;
        return;
    end
    factorial = x* fact(x-1);
end
```

Task 3

There is a nested loop in use here. For the first loop with i , it will run for n times and the second loop will have a run time depending on i . The run time of this code looks like an arithmetic series which will be:

$$n(n+1)/2 = n^2/2 + n/2$$

we don't care about the constants and lower indexed value so, the time complexity for this function, in θ notation is n^2 .

Task 4

$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ and $B = \begin{bmatrix} e \\ f \end{bmatrix}$ which gives us:

$$A*B = \begin{bmatrix} ae+bf \\ ce+df \end{bmatrix}$$

Task 5

Given, the function: $f(x) = 3x^2 + 5x - 7$.

The first derivative $f'(x)$ would be: $f'(x) = 6x + 5$

For $x=5$, $f'(5) = 30+5 = 35$

Second derivative of $f(x)$ which is $f''(x) = 6$

and, for $x=5$, $f''(5) = 6$

Task 6

We are given, for two events A and B which are independent of each other, $P(A)=0.3$ and $P(B)=0.6$

$P(A \text{ and } B) = 0.3*0.6 = 0.18$ (*Because these are independent events*)

$P(A \text{ or } B) = 0.3 + 0.6 - 0.3*0.6 = 0.72$

$P(\text{not } A) = P(\text{universal}) - P(A) = 1 - 0.3 = 0.7$ (*Total probability is 1.*)

$P(A|B) = P[A \text{ and } B] / P[B] = 0.18/0.6 = 0.3$

Here, probability of getting A given B is 0.3

Task 7

the matlab function is attached in the zipped folder together.

```
%Nabin Chapagain, 1001551151%  
function [avg,stdev] = file_stats(pathname)  
    fileID = fopen(pathname,'r');  
    A = fscanf(fileID, '%f');  
    avg = mean(A);  
    stdev = std(A);  
    fclose(fileID);  
end
```

Task 8

Here, total number of hats available is $40+70+35+15+50+30+60+20+80 = 400$.

Part a: $P(\text{price} < \$75) = (40 + 70 + 15 + 50 + 60 + 20)/400 = 255/400 = 51/80$

Part b: $P(\text{price} < \$75 \mid \text{color} = \text{green}) = P[\text{under } 75 \text{ and green}] / P[\text{green}] = 65/95 = 13/19$

Part c: $P(\text{price} < \$75, \text{color} = \text{green}) = (50+15)/400 = 65/400 = 13/80$