# Chapter 5: Other Relational Languages

- Query-by-Example (QBE)
- Quel
- Datalog

Database Systems Concepts

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### Query-by-Example (QBE)

- Basic Structure
- Queries on One Relation
- Queries on Several Relations
- The Condition Box
- The Result Relation
- Ordering the Display of Tuples
- Aggregate Operations
- Modification of the Database

### QBE — Basic Structure

- A graphical query language which is based (roughly) on the domain relational calculus
- Two dimensional syntax system creates templates of relations that are requested by users
- Queries are expressed "by example"

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# Skeleton Tables

branch	branch-name	branch-city	assets

customer	customer-name	customer-street	customer-city

loan	branch-name	loan-number	amount

# Skeleton Tables (Cont.)

borrower	customer-name	loan-number

account	branch-name	account-number	balance

depositor	customer-name	account-number

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# Queries on One Relation

• Find all loan numbers at the Perryridge branch.

loan	branch-name	loan-number	amount
	Perryridge	P <i>x</i>	

- x is a variable (optional)
- P. means print (display)
- duplicates are removed

loan	branch-name	loan-number	amount
	Perryridge	P.ALL.	

- duplicates are not removed

# Queries on One Relation (Cont.)

- Display full details of all loans
  - Method 1:

loan	branch-name	loan-number	amount
	P <i>x</i>	P <i>y</i>	P <i>z</i>

- Method 2: shorthand notation

loan	branch-name	loan-number	amount
P.			

• Find the loan number of all loans with a loan amount of more than \$700.

loan	branch-name	loan-number	amount
		P.	>700

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# Queries on One Relation (Cont.)

 Find the loan numbers of all loans made jointly to Smith and Jones.

borrower	customer-name	loan-number
	"Smith"	P <i>x</i>
	"Jones"	_X

• Find the loan numbers of all loans made to Smith, Jones or both.

borrower	customer-name	loan-number
	"Smith"	P <i>x</i>
	"Jones"	P <i>y</i>

# **Queries on Several Relations**

• Find the names of all customers who have a loan from the Perryridge branch.

loan	branch-name	loan-number	amount
	Perryridge	_X	

borrower	customer-name	loan-number
	P <i>y</i>	_X

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# Queries on Several Relations (Cont.)

• Find the names of all customers who have both an account and a loan at the bank.

depositor	customer-name	account-number
	P <i>x</i>	

borrower	customer-name	loan-number
	_X	

# Queries on Several Relations (Cont.)

• Find the names of all customers who have an account at the bank, but do not have a loan from the bank.

depositor	ositor customer-name account-number	
	P <i>x</i>	

borrower	customer-name	loan-number	
	_X		

¬ means "there does not exist"

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# Queries on Several Relations

• Find all customers who have at least two accounts.

depositor	customer-name	account-number
	P <i>x</i>	_ <i>y</i>
	_X	¬ _ <i>y</i>

 $\neg$  means "not equal to"

#### The Condition Box

- Allows the expression of constraints on domain variables that are either inconvenient or impossible to express within the skeleton tables.
- Find all account numbers with a balance between \$1,300 and \$2,000 but not exactly \$1,500.

account	branch-name	account-number	balance
		P.	_X

*conditions*

$$_{-}x = ( ≥ 1300 \text{ and } ≤ 2000 \text{ and } ¬ 1500)$$

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### The Result Relation

- Find the *customer-name*, *account-number*, and *balance* for all customers who have an account at the Perryridge branch.
  - We need to:
    - \* Join depositor and account.
    - \* Project customer-name, account-number, and balance.
  - To accomplish this we:
    - \* Create a skeleton table, called *result*, with attributes *customer-name*, *account-number*, and *balance*.
    - \* Write the query.

# The Result Relation (Cont.)

• The resulting query is:

branch-name	account-number	balance
Perryridge	_ <i>y</i>	_Z

depositor	customer-name	account-number
	_X	_ <i>y</i>

result	customer-name	account-number	balance
P.	_X	_ <i>y</i>	_Z

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# Ordering the Display of Tuples

- AO = ascending order; DO = descending order.
   When sorting on multiple attributes, the sorting order is specified by including with each sort operator (AO or DO) an integer surrounded by parentheses.
- List all account numbers at the Perryridge branch in ascending alphabetic order with their respective account balances in descending order.

account	branch-name	account-number	balance
	Perryridge	P.AO(1).	P.DO(2).

# Aggregate Operations

- The aggregate operators are AVG, MAX, MIN, SUM, and CNT
- The above operators must always be postfixed with "ALL." (e.g., SUM.ALL.or AVG.ALL.\_x).
- Find the total balance of all the accounts maintained at the Perryridge branch.

account	branch-name	account-number	balance
	Perryridge		P.SUM.ALL.

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# **Aggregate Operations (Cont.)**

• Find the total number of customers having an account at the bank.

depositor	customer-name	account-number
	P.CNT.UNQ.ALL.	

Note: UNQ is used to specify that we want to eliminate duplicates.

### **Query Examples**

• Find the average balance at each branch.

account	branch-name	account-number	balance
	P.G.		P.AVG.ALLx

#### Note:

- The "G" in "P.G" is analogous to SQL's **group by** construct
- The "ALL" in the "P.AVG.ALL" entry in the balance column ensures that all balances are considered
- Find the average account balance at only those branches where the average account balance is more than \$1,200. Add the condition box:

conditions

AVG.ALL.\_x > 1200

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### **Query Example**

• Find all customers who have an account at all branches located in Brooklyn:

depositor	customer-name	account-number
	P.G <i>x</i>	_ <i>y</i>

account	branch-name	account-number	balance
	CNT.UNQ.ALLz	- <i>y</i>	

branch	branch-name	branch-city	assets
	_Z	Brooklyn	
	_ <i>W</i>	Brooklyn	

# Query Example (Cont.)

#### conditions

 $CNT.UNQ.ALL.\_z = CNT.UNQ.ALL.\_w$ 

- CNT.UNQ.ALL.\_w specifies the number of distinct branches in Brooklyn.
- CNT.UNQ.ALL.\_z specifies the number of distinct branches in Brooklyn at which customer x has an account.

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### **Modification of the Database – Deletion**

- Deletion of tuples from a relation is expressed by use of a D. command. In the case where we delete information in only some of the columns, null values, specified by —, are inserted.
- Delete customer Smith

customer	customer-name	customer-street	customer-city
D.	Smith		

• Delete the *branch-city* value of the branch whose name is "Perryridge".

branch	branch-name	branch-city	assets
	Perryridge	D.	

# **Deletion Query Examples**

• Delete all loans with a loan amount between \$1300 and \$1500.

loan	branch-name	loan-number	amount
D.		_ <i>y</i>	_X

conditions
$$-x = ( \ge 1300 \text{ and } \le 1500)$$

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# **Deletion Query Examples (Cont.)**

• Delete all accounts at branches located in Brooklyn.

account	branch-name	account-number	balance
D.	_X	_ <i>y</i>	

depositor	customer-name	account-number
D.		_У

branch	branch-name	branch-city	assets
-	_X	Brooklyn	

#### **Modification of the Database – Insertion**

- Insertion is done by placing the I. operator in the query expression.
- Insert the fact that account A-9732 at the Perryridge branch has a balance of \$700.

account	branch-name	account-number	balance
I.	Perryridge	A-9732	700

 Provide as a gift for all loan customers of the Perryridge branch, a new \$200 savings account for every loan account they have, with the loan number serving as the account number for the new savings account.

(next slide)

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### **Modification of the Database – Insertion (Cont.)**

account	branch-name	account-number	balance
I.	Perryridge	_X	200

depositor	customer-name	account-number
I.	_ <i>y</i>	_X

loan	branch-name	loan-number	amount
	Perryridge	_X	

borrower	customer-name	account-number
	_ <i>y</i>	_X

### Modification of the Database – Updates

- Use the U. operator to change a value in a tuple without changing *all* values in the tuple. QBE does not allow users to update the primary key fields.
- Update the asset value of the of the Perryridge branch to \$10,000,000.

branch	branch-name	branch-city	assets
	Perryridge		U.10000000

• Increase all balances by 5 percent.

account	branch-name	account-number	balance
U.			_x * 1.05
			_X

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- Basic Structure
- Simple Queries
- Tuple Variables
- Aggregate Functions
- Modification of the Database
- Set Operations
- Quel and the Tuple Relational Calculus

#### **Quel** — Basic Structure

- Introduced as the query language for the Ingres database system, developed at the University of California, Berkeley.
- Basic structure parallels that of the tuple relational calculus.
- Most Quel queries are expressed using three types of clauses:
   range of, retrieve, and where.
  - Each tuple variable is declared in a range of clause.

#### range of t is r

declares *t* to be a tuple variable restricted to take on values of tuples in relation *r*.

- The retrieve clause is similar in function to the select clause of SQL.
- The **where** clause contains the selection predicate.

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### **Quel Query Structure**

• A typical Quel query is of the form:

```
range of t_1 is r_1
range of t_2 is r_2
\vdots
range of t_m is r_m
retrieve (t_{i_1}.A_{j_1}, t_{i_2}.A_{j_2}, ..., t_{i_n}.A_{j_n})
where P
```

- Each  $t_i$  is a tuple variable.
- Each  $r_i$  is a relation.
- Each  $A_{i\nu}$  is an attribute.
- The notation t.A denotes the value of tuple variable t on attribute A.

### **Quel Query Structure (Cont.)**

- Quel does not include relational algebra operations like intersect, union, and minus.
- Quel does not allow nested subqueries (unlike SQL).
  - Cannot have a nested retrieve-where clause inside a where clause.
- These limitations do not reduce the expressive power of Quel, but the user has fewer alternatives for expressing a query.

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### **Simple Queries**

Find the names of all customers having a loan at the bank.

range of t is borrower
retrieve (t.customer-name)

 To remove duplicates, we must add the keyword unique to the retrieve clause:

range of t is borrower retrieve unique (t.customer-name)

### **Query Over Several Relations**

 Find the names of all customers who have both a loan and an account at the bank.

> range of s is borrower range of t is depositor retrieve unique (s.customer-name) where t.customer-name = s.customer-name

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# Tuple Variables

- Certain queries need to have two distinct tuple variables ranging over the same relation.
- Find the name of all customers who live in the same city as Jones does.

### **Tuple Variables (Cont.)**

- When a query requires only one tuple variable ranging over a relation, we can omit the **range of** statement and use the relation name itself as an implicitly declared tuple variable.
- Find the names of all customers who have both a loan and an account at the bank.

**retrieve unique** (borrower.customer-name) **where** depositor.customer-name = borrower.customer-name

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# Aggregate Functions

- Aggregate functions in Quel compute functions on groups of tuples.
- Grouping is specified as part of each aggregate expression.
- Quel aggregate expressions may take the following forms:

```
aggregate function (t.A) aggregate function (t.A where P) aggregate function (t.A by s.B_1, s.B_2, ..., s.B_n where P)
```

- aggregate function is one of count, sum, avg, max, min, countu, sumu, avgu, or any
- t and s are tuple variables
- A,  $B_1$ ,  $B_2$ , ...,  $B_n$  are attributes
- P is a predicate similar to the where clause in a retrieve

### **Aggregate Functions (Cont.)**

- The functions countu, sumu, and avgu are identical to count, sum, and avg, respectively, except that they remove duplicates from their operands.
- An aggregate expression may appear anywhere a constant may appear; for example, in a where clause.

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### **Example Queries**

• Find the average account balance for all accounts at the Perryridge branch.

range of t is account retrieve avg (t.balance where t.branch-name = "Perryridge")

• Find all accounts whose balance is higher than the average balance of Perryridge-branch accounts.

range of u is account
range of t is account
retrieve (t.account-number)
where t.balance > avg (u.balance where
u.branch-name = "Perryridge")

#### **Example Queries**

- Find all accounts whose balance is higher than the average balance at the branch where the account is held.
  - Compute for each tuple t in account the average balance at branch t.branch-name.
  - In order to form these groups of tuples, use the by construct in the aggregate expression.

The query is:

range of u is account
range of t is account
retrieve (t.account-number)
where t.balance > avg (u.balance by t.branch-name
where u.branch-name = t.branch-name)

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### **Example Query**

• Find the names of all customers who have an account at the bank, but do not have a loan from the bank.

range of t is depositor
range of u is borrower
retrieve unique (t.customer-name)
where any (u.loan-number by t.customer-name
where u.customer-name = t.customer-name) = 0

• The use of a comparison with **any** is analogous to the "there exists" quantifier of the relational calculus.

# Example Query

- Find the names of all customers who have an account at all branches located in Brooklyn.
  - First determine the number of branches in Brooklyn.
  - Compare this number with the number of distinct branches in Brooklyn at which each customer has an account.

```
range of t is depositor
range of u is account
range of s is branch
range of w is branch
retrieve unique (t.customer-name)
where countu (s.branch-name by t.customer-name
where u.account-number = t.account-number
and u.branch-name = s.branch-name
and s.branch-city = "Brooklyn") =
countu (u.branch-name where u.branch-city = "Brooklyn")
```

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### **Modification of the Database – Deletion**

• The form of a Quel deletion is

range of *t* is *r* delete *t* where *P* 

- The tuple variable *t* can be implicitly defined.
- The predicate P can be any valid Quel predicate.
- If the where clause is omitted, all tuples in the relation are deleted.

#### **Deletion Query Examples**

• Delete all tuples in the *loan* relation.

range of t is loan delete t

• Delete all Smith's account records.

range of t is depositor delete t where t.customer-name = "Smith"

Delete all account records for branches located in Needham.

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# **Modification of the Database – Insertion**

- Insertions are expressed in Quel using the append command.
- Insert the fact that account A-9732 at the Perryridge branch has a balance of \$700.

append to account (branch-name = "Perryridge", account-number = A-9732, balance = 700)

#### **Insertion Query Example**

 Provide as a gift for all loan customers of the Perryridge branch, a new \$200 savings account for every loan account that they have. Let the loan number serve as the account number for the new savings account.

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### **Modification of the Database – Updates**

- Updates are expressed in Quel using the replace command.
- Increase all account balances by 5 percent.

range of t is account
replace t (balance = 1.05 \* t.balance)

 Pay 6 percent interest on accounts with balances over \$10,000, and 5 percent on all other accounts.

> range of t is account replace t (balance = 1.06 \* balance) where t.balance > 10000 replace t (balance = 1.05 \* balance) where t.balance < 10000

### **Set Operations**

- Quel does not include relational algebra operations like intersect, union, and minus.
- To construct queries that require the use of set operations, we must create temporary relations (via the use of regular Quel statements).
- Example: To create a temporary relation *temp* that holds the names of all depositors of the bank, we write

range of *u* is *depositor* retrieve into *temp* unique (*u.customer-name*)

• The **into** *temp* clause causes a new relation, *temp*, to be created to hold the result of this query.

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### **Example Queries**

- Find the names of all customers who have an account, a loan, or both at the bank.
- Since Quel has no union operation, a new relation (called temp) must be created that holds the names of all borrowers of the bank.
- We find all borrowers of the bank and insert them in the newly created relation *temp* by using the **append** command.

range of s is borrower append to temp unique (s.customer-name)

• Complete the guery with:

range of t is temp
retrieve unique (t.customer-name)

### **Example Queries**

- Find the names of all customers who have an account at the bank but do not have a loan from the bank.
- Create a temporary relation by writing:

range of *u* is *depositor* retrieve into *temp* (*u.customer-name*)

• Delete from *temp* those customers who have a loan.

range of s is borrower
range of t is temp
delete t
where t.customer-name = s.customer-name

• *temp* now contains the desired list of customers. We write the following to complete our query.

range of t is temp
retrieve unique (t.customer-name)

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### **Quel and the Tuple Relational Calculus**

The following Quel query

range of 
$$t_1$$
 is  $r_1$  range of  $t_2$  is  $r_2$ 

.

range of  $t_m$  is  $r_m$  retrieve unique  $(t_{i_1}.A_{j_1}, t_{i_2}.A_{j_2}, ..., t_{i_n}.A_{j_n})$  where P

would be expressed in the tuple relational calculus as:

$$\{t \mid \exists t_1 \in r_1, t_2 \in r_2, ..., t_m \in r_m (t_{i_1}.A_{j_1}] = t_{i_1}[A_{j_1}] \land t[r_{i_2}.A_{j_2}] = t_{i_2}[A_{j_2}] \land ... \land t[r_{i_n}.A_{j_n}] = t_{i_n}[A_{j_n}] \land P(t_1, t_2, ..., t_m)\}$$

### Quel and TRC (Cont.)

- t₁ ∈ r₁ ∧ t₂ ∈ r₂ ∧ ... ∧ tm ∈ rm
   Constrains each tuple in t₁, t₂, ..., tm to take on values of tuples in the relation over which it ranges.
- $t[r_{i_1}.A_{j_1}] = t_{i_1}[A_{j_1}] \wedge t_{i_2}[A_{j_2}] = t[r_{i_2}.A_{j_2}] \wedge ... \wedge t[r_{i_n}.A_{j_n}] = t_{i_n}[A_{j_n}]$ Corresponds to the **retrieve** clause of the Quel query.
- P(t<sub>1</sub>, t<sub>2</sub>, ..., t<sub>m</sub>)
   The constraint on acceptable values for t<sub>1</sub>, t<sub>2</sub>, ..., t<sub>m</sub> imposed by the where clause in the Quel query.
- Quel achieves the power of the relational algebra by means of the any aggregate function and the use of insertion and deletion on temporary relations.

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### Datalog

- Basic Structure
- Syntax of Datalog Rules
- Semantics of Nonrecursive Datalog
- Safety
- Relational Operations in Datalog
- Recursion in Datalog
- The Power of Recursion

### **Basic Structure**

- Prolog-like logic-based language that allows recursive queries; based on first-order logic.
- A Datalog program consists of a set of *rules* that define views.
- Example: define a view relation *v1* containing account numbers and balances for accounts at the Perryridge branch with a balance of over \$700.

$$v1(A, B) := account("Perryridge", A, B), B > 700.$$

 Retrieve the balance of account number "A-217" in the view relation v1.

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### **Example Queries**

- Each rule defines a set of tuples that a view relation must contain.
- The set of tuples in a view relation is then defined as the union of all the sets of tuples defined by the rules for the view relation.
- Example:

```
interest-rate(A, 0) :- account(N, A, B), B < 2000 interest-rate(A, 5) :- account(N, A, B), B >= 2000
```

 Define a view relation c that contains the names of all customers who have a deposit but no loan at the bank:

```
c(N) := depositor(N, A), not is-borrower(N). is-borrower(N) := borrower(N, L).
```

### Syntax of Datalog Rules

• A positive literal has the form

$$p(t_1, t_2, \ldots, t_n)$$

- p is the name of a relation with n attributes
- each  $t_i$  is either a constant or variable
- A negative literal has the form

**not** 
$$p(t_1, t_2, ..., t_n)$$

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### Syntax of Datalog Rules (Cont.)

• Rules are built out of literals and have the form:

$$p(t_1, t_2, ..., t_n) :- L_1, L_2, ..., L_n.$$

- each of the  $L_i$ 's is a literal
- head the literal  $p(t_1, t_2, ..., t_n)$
- body the rest of the literals
- A fact is a rule with an empty body, written in the form:

$$p(v_1, v_2, ..., v_n).$$

- indicates tuple  $(v_1, v_2, ..., v_n)$  is in relation p

#### Semantics of a Rule

- A ground instantiation of a rule (or simply instantiation) is the result of replacing each variable in the rule by some constant.
- Rule defining v1

```
v1(A, B) := account("Perryridge", A, B), B > 700.
```

• An instantiation of above rule:

```
v1("A-217", 750) :- account("Perryridge", "A-217", 750), 750 > 700.
```

- The body of rule instantiation R' is *satisfied* in a set of facts (database instance) I if
  - 1. For each positive literal  $q_i(v_{i,1}, ..., v_{i,n_i})$  in the body of R', I contains the fact  $q(v_{i,1}, ..., v_{i,n_i})$ .
  - 2. For each negative literal **not**  $q_j(v_{j,1}, ..., v_{j,n_j})$  in the body of R', I does not contain the fact  $q_i(v_{j,1}, ..., v_{j,n_i})$ .

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### Semantics of a Rule (Cont.)

 We define the set of facts that can be inferred from a given set of facts I using rule R as:

$$infer(R, I) = \{p(t_1, ..., t_{n_i}) \mid \text{ there is an instantiation } R' \text{ of } R$$
  
where  $p(t_1, ..., t_{n_i})$  is the head of  $R'$ , and  
the body of  $R'$  is satisfied in  $I$ 

• Given a set of rules  $\mathcal{R} = \{R_1, R_2, \dots, R_n\}$ , we define

$$infer(R_1, I) = infer(R_1, I) \cup infer(R_2, I) \cup ... \cup infer(R_n, I)$$

### Layering of Rules

• Define the interest on each account in Perryridge.

```
interest(A, I) := perryridge-account(A, B),

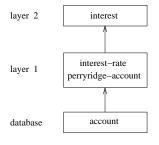
interest-rate(A, R), I = B * R/100.

perryridge-account(A, B) := account("Perryridge", A, B).

interest-rate(A, 0) := account(N, A, B), B < 2000.

interest-rate(A, 5) := account(N, A, B), B >= 2000.
```

Layering of the view relations



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### Layering of Rules (Cont.)

#### Formally:

- A relation is in layer 1 if all relations used in the bodies of rules defining it are stored in the database.
- A relation is in layer 2 if all relations used in the bodies of rules defining it are either stored in the database, or are in layer 1.
- A relation p is in layer i + 1 if
  - it is not in layers 1, 2, . . . , i
  - all relations used in the bodies of rules defining p are either stored in the database, or are in layers 1, 2, ..., i

# Semantics of a Program

Let the layers in a given program be 1, 2, ..., n. Let  $\mathcal{R}_i$  denote the set of all rules defining view relations in layer i.

- Define  $I_0$  = set of facts stored in the database.
- Define  $I_{i+1} = I_i \cup infer(\mathcal{R}_{i+1}, I_i)$
- The set of facts in the view relations defined by the program
   (also called the *semantics of the program*) is given by the set of
   facts I<sub>n</sub> corresponding to the highest layer n.

Note: Can instead define semantics using view expansion like in relational algebra, but above definition is better for handling extensions such as recursion.

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### Safety

• It is possible to write rules that generate an infinite number of answers.

$$gt(X, Y) := X > Y$$
  
not-in-loan(B, L) := **not** loan(B, L)

To avoid this possibility Datalog rules must satisfy the following safety conditions.

- Every variable that appears in the head of the rule also appears in a non-arithmetic positive literal in the body of the rule.
- Every variable appearing in a negative literal in the body of the rule also appears in some positive literal in the body of the rule.

### **Relational Operations in Datalog**

• Project out attribute account-name from account.

$$query(A) := account(N, A, B).$$

• Cartesian product of relations  $r_1$  and  $r_2$ .

query
$$(X_1, X_2, ..., X_n, Y_1, Y_2, ..., Y_m) := r_1(X_1, X_2, ..., X_n), r_2(Y_1, Y_2, ..., Y_m).$$

• Union of relations  $r_1$  and  $r_2$ .

query 
$$(X_1, X_2, ..., X_n) := r_1(X_1, X_2, ..., X_n)$$
.  
query  $(X_1, X_2, ..., X_n) := r_2(X_1, X_2, ..., X_n)$ .

• Set difference of  $r_1$  and  $r_2$ .

query 
$$(X_1, X_2, ..., X_n) := r_1(X_1, X_2, ..., X_n),$$
  
**not**  $r_2(X_1, X_2, ..., X_n).$ 

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### Recursion in Datalog

Create a view relation *empl* that contains every tuple (X, Y) such that X is directly or indirectly managed by Y.

$$empl(X, Y) := manager(X, Y).$$
  
 $empl(X, Y) := manager(X, Z), empl(Z, Y).$ 

• Find the direct and indirect employees of Jones.

? 
$$empl(X, "Jones")$$
.

manager

employee-name	manager-name	
Alon	Barinsky	
Barinsky	Estovar	
Corbin	Duarte	
Duarte	Jones	
Estovar	Jones	
Jones	Klinger	
Rensal	Klinger	

#### **Semantics of Recursion in Datalog**

 The view relations of a recursive program containing a set of rules R are defined to contain exactly the set of facts I computed by the iterative procedure Datalog-Fixpoint

```
procedure Datalog-Fixpoint
I = \text{set of facts in the database}
repeat
Old\_I = I
I = I \cup infer(\mathcal{R}, I)
until \ I = Old\_I
```

- At the end of the procedure,  $infer(\mathcal{R}, I) = I$
- *I* is called a *fixpoint* of the program.
- Datalog-Fixpoint computes only true facts so long as no rule in the program has a negative literal.

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### The Power of Recursion

- Recursive views make it possible to write queries, such as transitive closure queries, that cannot be written without recursion or iteration.
- A view V is said to be **monotonic** if given any two sets of facts  $I_1$  and  $I_2$  such that  $I_1 \subseteq I_2$ ,  $E_V(I_1) \subseteq E_V(I_2)$ , where  $E_V$  is the expression used to define V.
- Procedure *Datalog-Fixpoint* is sound provided the function *infer* is monotonic.
- Relational algebra views defined using only the operators:
   Π, σ, ×, ⋈, ∪, ∩ and ρ are monotonic. Views using are not monotonic.