NANYANG TECHNOLOGICAL UNIVERSITY

SEMESTER 2 EXAMINATION 2016-2017

EE2008 / IM1001 – DATA STRUCTURES AND ALGORITHMS

April / May 2017 Time Allowed: 2½ hours

INSTRUCTIONS

- 1. This paper contains 4 questions and comprises 4 pages.
- 2. Answer ALL questions.
- 3. All questions carry equal marks.
- 4. This is a closed-book examination.
- 5. Unless specifically stated, all symbols have their usual meanings.
- 1. (a) Determine the asymptotic upper bound for the number of times the statement "r = r + 1" is executed in the following algorithm.

for
$$i = 1$$
 to n
for $j = 1$ to i
for $k = j$ to n
 $r = r + 1$

(5 Marks)

(b) Use mathematical induction to prove that the following equation is true for every positive integer $n \ge 1$.

$$\sum_{i=1}^{n} (a_i - a_{i-1}) = a_n - a_0$$

(6 Marks)

Note: Question No. 1 continues on page 2.

- (c) Determine the asymptotic upper bound of the following functions using the O(g(n)) notation with the simplest function g(n) possible.
 - (i) $2n \lg(n-2)^2$
 - (ii) *n*!

(8 Marks)

(d) Consider a singly-linked list S with the pointer start pointing to the first node of the list. Each node in the list S stores an integer value. Write an algorithm that computes the sum of all the values stored in S.

(6 Marks)

2. (a) Consider the following recursive algorithm:

```
Algorithm Q(n)

if (n == 0 \text{ or } n == 1)

return 1

else

return Q(n-2) + n + 1
```

Set up a recurrence relation for the number of additions made by the algorithm and solve it.

(7 Marks)

(b) An integer is stored in each node of a doubly-linked list which has a reference *start* that points to the first node of the list. Write an algorithm that deletes the node which stores the last occurrence of a given integer *k* from the list.

(8 Marks)

Note: Question No. 2 continues on page 3.

- (c) Consider the AVL tree in Figure 1.
 - (i) Show the steps taken to balance the tree when a node with value 40 is inserted.
 - (ii) Show the steps taken to balance the tree when a node with value 75 is inserted in the balanced tree in part (i).

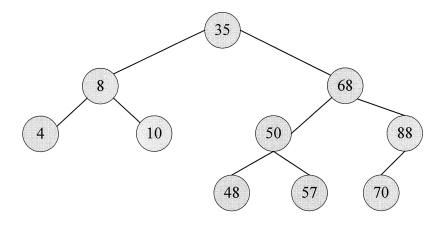


Figure 1

(10 Marks)

3. (a) Consider the following maxheap.

Explain and show clearly what the array looks like in each step if you are required to perform the following operations:

- (i) delete the fourth element of the array while maintaining the maxheap structure;
- (ii) then delete the third element of the array while maintaining the maxheap structure.

(10 Marks)

(b) Explain and show how to perform radix sort on the following sequence:

(7 Marks)

(c) Write an algorithm in pseudocode to determine the number of leaf nodes of a maxheap with value less than x.

(8 Marks)

4. (a) Consider the weighted graph in Figure 2. Explain and show clearly each step to find the shortest path from node A to node H.

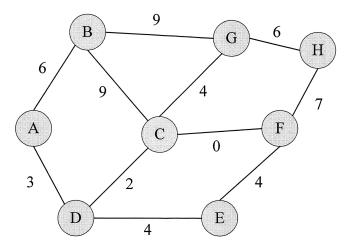


Figure 2

(12 Marks)

- (b) Suppose that a factory manufactures a product that consists of 5 components, which are assembled together. The components need to be assembled according to the following priority:
 - Component 1 can only be assembled after component 2.
 - Component 3 can only be assembled after components 1 and 2.
 - Component 4 can only be assembled after components 2 and 3.
 - Component 5 can only be assembled after components 1 and 4.

Explain clearly how you will use depth first search to come up with a sequence to assemble the 5 components correctly.

(8 Marks)

(c) Given a weighted graph whose edge weights are all non-negative, one wishes to find a shortest path from a source node to a destination node. Professor X claims that one can use Prim's algorithm starting at the source node to find a shortest path to the destination node. Is this claim true or false? Justify your answer.

(5 Marks)

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Please read the following instructions carefully:

- 1. Please do not turn over the question paper until you are told to do so. Disciplinary action may be taken against you if you do so.
- 2. You are not allowed to leave the examination hall unless accompanied by an invigilator. You may raise your hand if you need to communicate with the invigilator.
- 3. Please write your Matriculation Number on the front of the answer book.
- 4. Please indicate clearly in the answer book (at the appropriate place) if you are continuing the answer to a question elsewhere in the book.