Problem Sheet: Scheme

1. Re-write the following expressions in Scheme and evaluate them using a Scheme interpreter/compiler.

```
(a) (3 \times (5 + (10 \div 5)))

(b) (2 + 3 + 4 + 5)

(c) (1 + (5 + (2 + (10 \div 3))))

(d) (1 + (5 + (2 + (10 \div 3.0))))

(e) (3 + 5) \times (10 \div 2)

(f) (3 + 5) \times (10 \div 2) + (1 + (5 + (2 + (10 \div 3))))
```

2. Define a procedure discount that takes two arguments: an item's initial price and a percentage discount [1]. It should return the new price:

```
> (discount 10 5)
9.50
> (discount 29.90 50)
14.95
```

- 3. Write a function called appearances that returns the number of times its first argument appears as a member of its second argument [1].
- 4. Write a procedure inter that takes two lists as arguments. It should return a list containing every element that appears in both lists, exactly once.
- 5. Write a procedure **noatoms** that takes a list and returns the number of atoms it contains.
- 6. Here is a Scheme procedure that never finishes its job:

Explain why it doesn't give any result[1].

- 7. Write a function called range that takes an integer n and returns a list containing the atoms $1, 2, 3, \ldots, n$.
- 8. Write a function called reversel that takes a list and returns it reversed.
- 9. If we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3, 5, 6 and 9. The sum of these multiples is 23. Write a procedure to find the sum of all the multiples of 3 or 5 below 1000 [2].
- 10. Write a procedure called flatten that takes as its argument a list, possibly including sublists, but whose ultimate building blocks are atoms. It should return a sentence containing all the atoms of the list, in the order in which they appear in the original:

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```
> (flatten '(((a b) c (d e)) (f g) ((((h))) (i j) k)))
(a b c d e f g h i j k)
```

11. Each new term in the Fibonacci sequence is generated by adding the previous two terms. By starting with 1 and 2, the first 10 terms will be:

```
1, 2, 3, 5, 8, 13, 21, 34, 55, 89, \dots
```

By considering the terms in the Fibonacci sequence whose values do not exceed four million, find the sum of the even-valued terms [2].

12. Write a procedure to-binary:

```
> (to-binary 9)
1001
> (to-binary 23)
10111
```

13. Write Heap's algorithm for generating permutations in Scheme.

References

- [1] Brian Harvey and Matt Wright, Simply Scheme: Introducing Computer Science, MIT, 1999.
- [2] Project Euler, Project Euler, 2016.