This problem sheet is about computational complexity [1].

- 1. Explain what a decision problem is.
- 2. Explain what the P computational complexity class is, and give an example of a problem in P.
- 3. Explain what a decision problem is.
- 4. Explain what the NP complexity class is.
- 5. Explain the terms conjunctive normal form and disjunctive normal form.
- 6. Convert the following expressions to Conjunctive Normal Form.
 - (a) $a \vee b$
 - (b) $a \wedge b$
 - (c) $((a \land b) \lor (\neg b \land c)) \lor \neg d$
 - (d) $(a \wedge b) \vee (c \wedge d)$
 - (e) $(a \lor b) \land (c \lor d)$
- 7. Convert the following expressions to Disjunctive Normal Form.
 - (a) $a \vee b$
 - (b) $a \wedge b$
 - (c) $((a \land b) \lor (\neg b \land c)) \lor \neg d$
 - (d) $(a \wedge b) \vee (c \wedge d)$
 - (e) $(a \lor b) \land (c \lor d)$
- 8. Determine if there is a setting of the variables in the following expression that makes the evaluation of the expression true.
 - (a) $a \lor b$
 - (b) $a \wedge b$
 - (c) $((a \land b) \lor (\neg b \land c)) \lor \neg d$
 - (d) $(a \wedge b) \vee (c \wedge d)$
 - (e) $(a \lor b) \land (c \lor d)$
- 9. Explain how to prove that a problem is NP-complete.
- $10.\ \,$ Prove that 3-SAT is NP-complete. You may assume that SAT is NP-complete.

References

[1] Michael Sipser. *Introduction to the Theory of Computation*. International Thomson Publishing, 3rd edition, 1996.