

RA Set Operations

- RA Set Operations
- Union
- Intersection
- Difference

❖ RA Set Operations

Relational algebra defines three set operations

- **union** ... $R \cup S$... (Query₁) **UNION** (Query₂)
- **intersection** ... $R \cap S$... (Query₁) **INTERSECT** (Query₂)
- **difference** ... $R - S$... (Query₁) **EXCEPT** (Query₂)

All relations involved must have the same schema (union-compatible)

All operations give a **set of results** (i.e. no duplicates)

To get *bag* semantics, use **UNION ALL**, etc.

❖ Union

Union combines two compatible relations into a single relation via set union of sets of tuples.

$$r_1 \cup r_2 = \{t \mid t \in r_1 \vee t \in r_2\}, \text{ where } r_1(R), r_2(R)$$

Result size: $|r_1 \cup r_2| \leq |r_1| + |r_2|$ Result schema: R

Algorithmic view:

```
result = r1
```

```
for each tuple  $t$  in relation  $r_2$ 
```

```
    result = result  $\cup$  { $t$ }
```

❖ Intersection

Intersection combines two compatible relations into a single relation via set intersection of sets of tuples.

$$r_1 \cap r_2 = \{t \mid t \in r_1 \wedge t \in r_2\}, \text{ where } r_1(R), r_2(R)$$

Result size: $|r_1 \cap r_2| \leq \min(|r_1|, |r_2|)$ Result schema: R

Algorithmic view:

```
result = {}  
for each tuple  $t$  in relation  $r_1$   
    if ( $t \in r_2$ ) {  $result = result \cup \{t\}$  }
```

❖ Intersection (cont)

Examples of union and intersection:

$T = \text{Sel}[B=1](R)$

A	B	C	D
a	1	x	4
e	1	y	4

$U = \text{Sel}[C=x](R)$

A	B	C	D
a	1	x	4
d	8	x	5

$T \text{ union } U$

A	B	C	D
a	1	x	4
d	8	x	5
e	1	y	4

$T \text{ intersect } U$

A	B	C	D
a	1	x	4

❖ Intersection (cont)

Querying with relational algebra (set operations)...

- Bars where either John or Gernot drinks

```
JohnBars = Proj[bar](Sel[drinker=John](Frequents))  
GernotBars = Proj[bar](Sel[drinker=Gernot](Frequents))
```

```
Result = JohnBars union GernotBars
```

- Bars where both John and Gernot drink

```
Result = JohnBars intersect GernotBars
```

❖ Difference

Difference finds the set of tuples that exist in one relation but do not occur in a second compatible relation.

$$r_1 - r_2 = \{ t \mid t \in r_1 \wedge t \notin r_2 \}, \text{ where } r_1(R), r_2(R)$$

Uses same notion of relation compatibility as union.

Note: tuples in r_2 but not r_1 do not appear in the result

- i.e. set difference \neq complement of set intersection

Algorithmic view:

```
result = {}
for each tuple t in relation r1
    if (!(t ∈ r2)) { result = result ∪ {t} }
```

❖ Difference (cont)

Examples of difference:

$T = \text{Sel}[B=1](R)$

A	B	C	D
a	1	x	4
e	1	y	4

$U = \text{Sel}[C=x](R)$

A	B	C	D
a	1	x	4
d	8	x	5

$T - U$

A	B	C	D
e	1	y	4

$U - T$

A	B	C	D
d	8	x	5

Clearly, difference is not symmetric.

❖ Difference (cont)

Querying with relational algebra (difference) ...

- Bars where John drinks and Gernot doesn't

```
JohnBars = Proj[bar](Sel[drinker=John](Frequents))  
GernotBars = Proj[bar](Sel[drinker=Gernot](Frequents))
```

```
Result = JohnBars - GernotBars
```

- Bars that sell VB but not New

```
VBBars = Proj[bar](Sel[beer=VB](Sells))  
NewBars = Proj[bar](Sel[beer=New](Sells))
```

```
Result = VBBars - NewBars
```

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