Relational Algebra

- Relational Algebra
- Notation
- Describing RA Operations
- Example Database #1
- Example Database #2
- Rename
- Selection
- Projection

COMP3311 20T3 ♦ Relational Algebra ♦ [0/16]

>>

>

## Relational Algebra

11/26/2020

### Relational algebra (RA) can be viewed as ...

- mathematical system for manipulating relations, or
- data manipulation language (DML) for the relational model

### Relational algebra consists of:

- operands: relations, or variables representing relations
- operators that map relations to relations
- rules for combining operands/operators into expressions
- rules for evaluating such expressions

### Why is it important?

- because it forms the basis for DBMS implementation
- relational algebra ops are like the machine code for DBMSs

COMP3311 20T3 ♦ Relational Algebra ♦ [1/16]

<< \ \ >>

## Relational Algebra (cont)

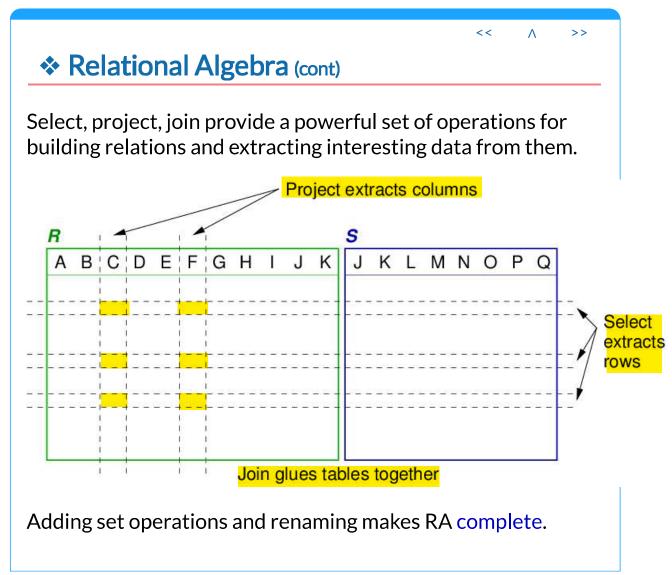
### **Core** relational algebra operations:

- rename: change names of relations/attributes
- selection: choosing a subset of tuples/rows
- projection: choosing a subset of attributes/columns
- union, intersection, difference: combining relations
- product, join: combining relations

#### Common extensions include:

• aggregation, projection++, division

COMP3311 20T3 ♦ Relational Algebra ♦ [2/16]



COMP3311 20T3 ♦ Relational Algebra ♦ [3/16]

## Notation

Standard treatments of relational algebra use Greek symbols.

We use the following notation (because it is easier to reproduce):

Operation Standard Our

Notation Notation

Selection  $\sigma_{expr}(Rel)$  Sel[expr](Rel)

Projection  $\pi_{A,B,C}(Rel)$  Proj[A,B,C](Rel)

Join  $Rel_1 \bowtie_{expr} Rel_2$   $Rel_1$   $Rel_2$   $Rel_2$ 

Rename  $\rho_{schema}Rel$  Rename[schema](Rel)

For other operations (e.g. set operations) we adopt the standard notation. Except when typing in a text file, where \* = intersection, + = union

COMP3311 20T3 ♦ Relational Algebra ♦ [4/16]

<< / / >>

## Describing RA Operations

### We define the semantics of RA operations using

- "conditional set" expressions e.g. { X | condition on X }
- tuple notations:
  - $\circ$  t[AB] (extracts attributes A and B from tuple t)
  - (x,y,z) (enumerated tuples; specify attribute values)
- quantifiers, set operations, boolean operators

#### For each operation, we also describe it operationally:

- give an algorithm to compute the result, tuple-by-tuple
- the algorithm is not generally how it will be computed in practice

COMP3311 20T3 ♦ Relational Algebra ♦ [5/16]

## Describing RA Operations (cont)

All RA operators return a result of type relation.

For convenience, we can name a result and use it later.

E.g.

```
Temp = R op_1 S op_2 T

Res = Temp op_3 Z

-- which is equivalent to

Res = (R op_1 S op_2 T) op_3 Z
```

Each "intermediate result" has a well-defined schema.

COMP3311 20T3 ♦ Relational Algebra ♦ [6/16]

# Example Database #1

R

Α	В	С	D
а	1	х	4
b	2	у	5
С	4	z	4
d	8	Х	5
е	1	у	4
f	2	х	5

S

D	E	F
1	а	х
2	b	у
3	С	х
4	а	у
5	b	х

COMP3311 20T3 ♦ Relational Algebra ♦ [7/16]

## Example Database #2

## Beers(name,manf)

(VB, Carlton) (New, Tooheys) (Porter, Maltshovel)

...

#### Beers(name,addr,licence)

(CBH, Coogee,433122) (Royal, Randwick, 632987) (Regent, Kingsford,112112

#### Frequents(drinker,bar)

(John, CBH) (Gernot, CBH) (Gernot, Regent)

...

#### Likes(drinker, beer)

(Andrew, New) (Gernot, Porter) (John, Pale Ale)

...

#### Beers(name,addr,phone)

(John, Alexandria, 93111139 (Gernot, Newtown, 92422429) (Andrew, Glebe, 90411049)

...

#### Sells(beer,bar,price)

(CBH, New, 2.50) (CBH, VB, 1.99 Royal, Porter, 3.00

6.53

COMP3311 20T3 ♦ Relational Algebra ♦ [8/16]

~~ /\

### Rename

Rename provides "schema mapping".

If expression E returns a relation  $R(A_1, A_2, ... A_n)$ , then

Rename[ $S(B_1, B_2, ... B_n)$ ](E)

gives a relation called *S* 

- containing the same set of tuples as E
- but with the name of each attribute changed from  $A_i$  to  $B_i$

Rename is like the identity function on the *contents* of a relation

The only thing that Rename changes is the schema.

COMP3311 20T3 ♦ Relational Algebra ♦ [9/16]

<< / / >>

### Rename (cont)

Rename can be viewed as a "technical" apparatus of RA.

We can also use implicit rename/project in sequences of RA operations, e.g.

```
R(a,b,c), S(c,d)
            Res = Rename[Res(b,c,d)](Project[b,c](Sel[a>5](R)) Join S)
dirty one-liner
            -- VS
            Tmp1 = Select[a>5](R)
            Tmp2 = Project[b,c](Tmp1)
            Tmp3 = Rename[Tmp3(cc,d)](S)
                                                explicit renaming
            Tmp4 = Tmp2 Join[c=cc] Tmp3
            Res = Rename[Res(b,c,d)](Tmp4)
            -- VS
            Tmp1(b,c) = Select[a>5](R)
                                                   I like this one the most!
implicit renaming
            Tmp2(cc,d) = S
on the LHS
            Res(b,c,d) = Tmp1 Join[c=cc] Tmp2
assignment
```

In SQL, we achieve a similar effect by defining a set of views

COMP3311 20T3 ♦ Relational Algebra ♦ [10/16]



Selection returns a subset of the tuples in a relation r(R) that satisfy a specified condition C.

$$\sigma_C(r) = Sel[C](r) = \{t \mid t \in r \land C(t)\}$$

Cis a boolean expression on attributes in R.

Result size:  $|\sigma_C(r)| \le |r|$ 

Result schema: same as the schema of r (i.e. R)

Algorithmic view:

```
result = {}
for each tuple t in relation r
  if (C(t)) { result = result U {t} }
```

COMP3311 20T3 ♦ Relational Algebra ♦ [11/16]

<< / / >>

# ❖ Selection (cont)

### Examples of selection:

R

Α	В	С	D	
а	1	х	4	
b	2	у	5	
С	4	z	4	
d	8	х	5	
е	1	у	4	
f	2	х	5	

Α	В	С	D

Sel[B=1](R)

Α	В	С	D
а	1	х	4
е	1	у	4

Sel[B>=D](R)

Α	В	С	D
С	4	z	4
d	8	х	5

Sel[A=b or A=c](R)

-	<u> </u>		
Α	В	С	D
b	2	у	5
С	4	z	4

COMP3311 20T3 ♦ Relational Algebra ♦ [12/16]

## Selection (cont)

Querying with relational algebra (selection) ...

• Details of all bars in The Rocks

```
Result = Sel[addr=The Rocks](Bars)
```

Beers made by Sierra Nevada

```
SNBeers = Sel[manf=Sierra Nevada](Beers)
Result = Rename[beer](Proj[name](SNBeers))
```

COMP3311 20T3 ♦ Relational Algebra ♦ [13/16]



Projection returns a set of tuples containing a subset of the attributes in the original relation.

$$\pi_{X}(r) = \frac{Proj[X](r)}{r} = \{ t[X] \mid t \in r \}, \text{ where } r(R) \}$$

X specifies a subset of the attributes of R.

Note that removing key attributes can produce duplicates.

In RA, duplicates are removed from the result set.
(In RDBMS's, duplicates are retained (i.e. they use bags, not sets))

Result size:  $|\Pi_X(r)| \le |r|$  Result schema: R'(X)

Algorithmic view:

```
result = {}
for each tuple t in relation r
result = result U {t[X]}
```

COMP3311 20T3 ♦ Relational Algebra ♦ [14/16]

# Projection (cont)

## Examples of projection:

Α	В	С	D
а	1	х	4
b	2	у	5
С	4	z	4
d	8	х	5
е	1	у	4
f	2	х	5

Proj[A,B,C](R)

Α	В	С
а	1	х
b	2	у
С	4	z
d	8	х
е	1	у
f	2	х

Proj[B,D](R)

Veril (	30 Tests 5400
В	D
1	4
2	5
4	4
8	5

Proj[D](R)

D
4
5

COMP3311 20T3 ♦ Relational Algebra ♦ [15/16]

Projection (cont)

Querying with relational algebra (projection)...

Names of all beers

Names of drinkers who live in Newtown

```
Result = Proj[name](Sel[addr=Newtown](Drinkers))
```

• What are all of the breweries?

```
Result(brewer) = Proj[manf](Beers)
```

COMP3311 20T3 ♦ Relational Algebra ♦ [16/16]

Produced: 6 Nov 2020