Quant. Comp. HW - 2

Steven MacCoun

Oct. 18, 2005

1 Simon's Problem

2 Modular Exponentiation

```
Here was my python code:
```

3 RSA Misuse

I first tried to solve this as strictly a math problem, but had little success, in large part because I thought that the gcd(e1, e2) was somehow irrelevant to the problem. However, I noticed that normally the exponents are the same value when performing RSA, so I scoured google to see if there was

some well known attack where you have a common modulus with different attacks. Turns out that it is fairly well documented, and Simmons wrote a paper on it a while back.

The basic idea is: Since

$$qcd(e_1, e_2) = 1$$

, then

$$\exists u, v \ s.t. \ e_1 * u + e_2 * v = 1$$

You can use this to fact to find M:

$$(M^{e_1} mod n)^u (M^{e_2} mod n)^v = M^{e_1*u + e_2*v} mod n = M mod n$$

4 Prime factorization

Problem: Consider n=121932632103337941464563328643500519

(a) How many bits is n?

print len(str(121932632103337941464563328643500519))

Output:

36

(b) Find if n is prime with program that runs in less than one second.

```
d = n - 1
         s = 0
        while d % 2 == 0:
                  d >>= 1
                  s += 1
         #Run several miller_rabin passes
         for repeat in xrange(20):
                   a = randint(2, n-1)
                   if not miller_rabin_pass(a, s, d, n):
                             return False
         return True
print miller_rabin(n)
   (b)
   (c)
   (d)
   (e)
```