

4423 Advanced Macroeconometrics 1 - Assignment 1

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We have just included the output in this assignment. The entire code can be found on <https://github.com/therealLucasPaul/AdvMacroeconometrics>.

Excercise 1: FRED-MD

Download the current version of the FRED-MD database and load it into R (or another statistical software of your choice). Note that the second line in the CSV-file denotes the suggested transformation, you have to remove it.

##	sasdate	RPI	W875RX1	DPCERA3M086SBEA	CMRMTSPLx	RETAILx
## 2	1/1/1959	2442.158	2293.2	17.272	292266.4	18235.77
## 3	2/1/1959	2451.778	2301.5	17.452	294424.7	18369.56
## 4	3/1/1959	2467.594	2318.5	17.617	293418.7	18523.06
## 5	4/1/1959	2483.671	2334.9	17.553	299322.8	18534.47
## 6	5/1/1959	2498.026	2350.4	17.765	301364.3	18679.66
## 7	6/1/1959	2505.788	2357.4	17.831	301348.8	18849.75

Subquestion (a)

Create a function that takes a vector containing observations of a time series as input and returns a dataframe with the following transformed series in its columns as output: - the original time series in its raw form; - the log-transformed time series; - month-on-month growth rates in percent; - year-on-year growth rates in percent; - the first lag of the year-on-year growth rates of the time series

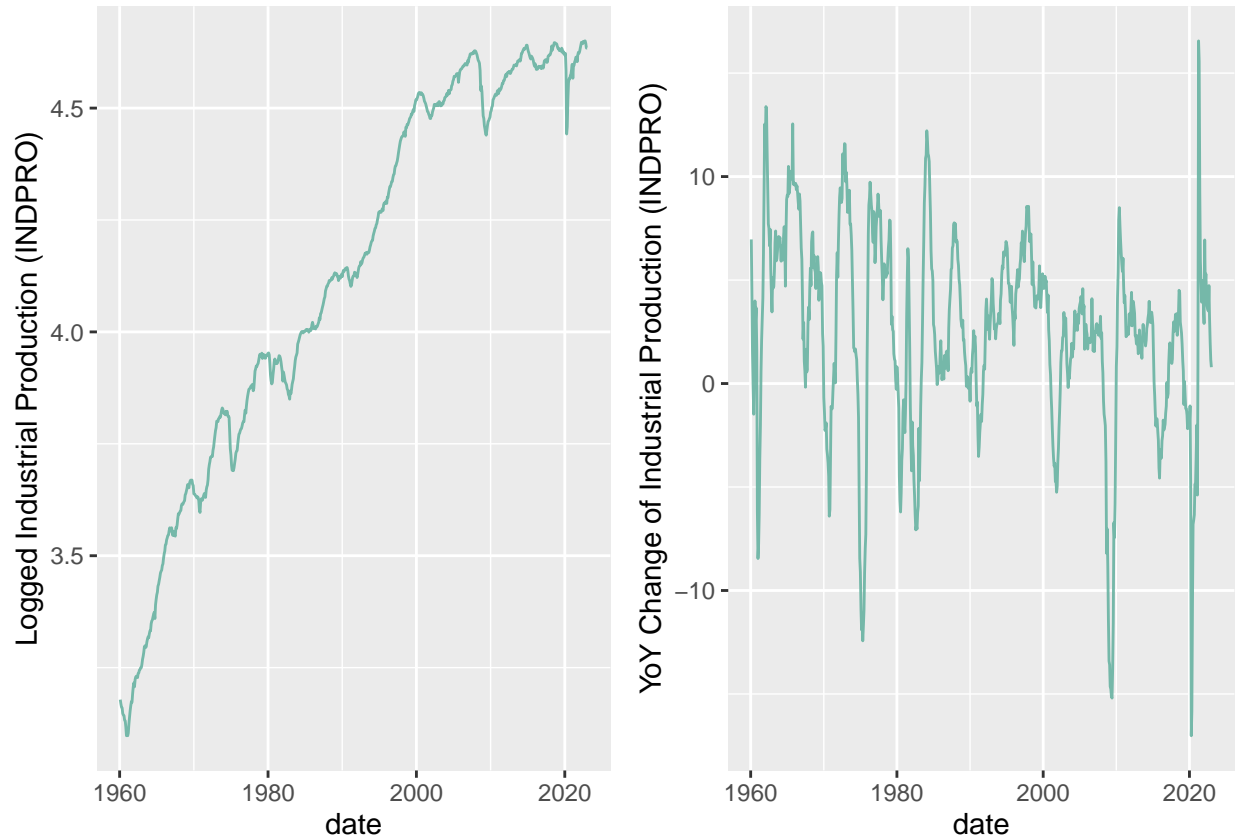
```
ts_transform <- function(x) {  
  output <- data.frame(matrix(NA,      # Create empty data frame  
                             nrow = NROW(x),  
                             ncol = 0))  
  
  output$raw <- x  
  output$log <- log(x)  
  output$mom <- ((x-lag(x))/lag(x))*100  
  output$yoy <- ((x-lag(x, 12))/lag(x, 12))*100  
  output$yoy_1stlag <- lag((x-lag(x, 12))/lag(x, 12))*100  
  return(output)  
}
```

Subquestion (b)

Use the created function to create a dataframe with the various transformation for US industrial production (mnemonic INDPRO), plot the logged time series and the yearly changes produced by the function. Briefly describe the properties of the time series.

##	date	raw	log	mom	yoy	yoy_1stlag
----	------	-----	-----	-----	-----	------------

##	1	1959-01-01	22.0151	3.091729	NA	NA	NA
##	2	1959-02-01	22.4463	3.111126	1.9586556	NA	NA
##	3	1959-03-01	22.7696	3.125426	1.4403265	NA	NA
##	4	1959-04-01	23.2547	3.146507	2.1304722	NA	NA
##	5	1959-05-01	23.6050	3.161459	1.5063622	NA	NA
##	6	1959-06-01	23.6319	3.162597	0.1139589	NA	NA

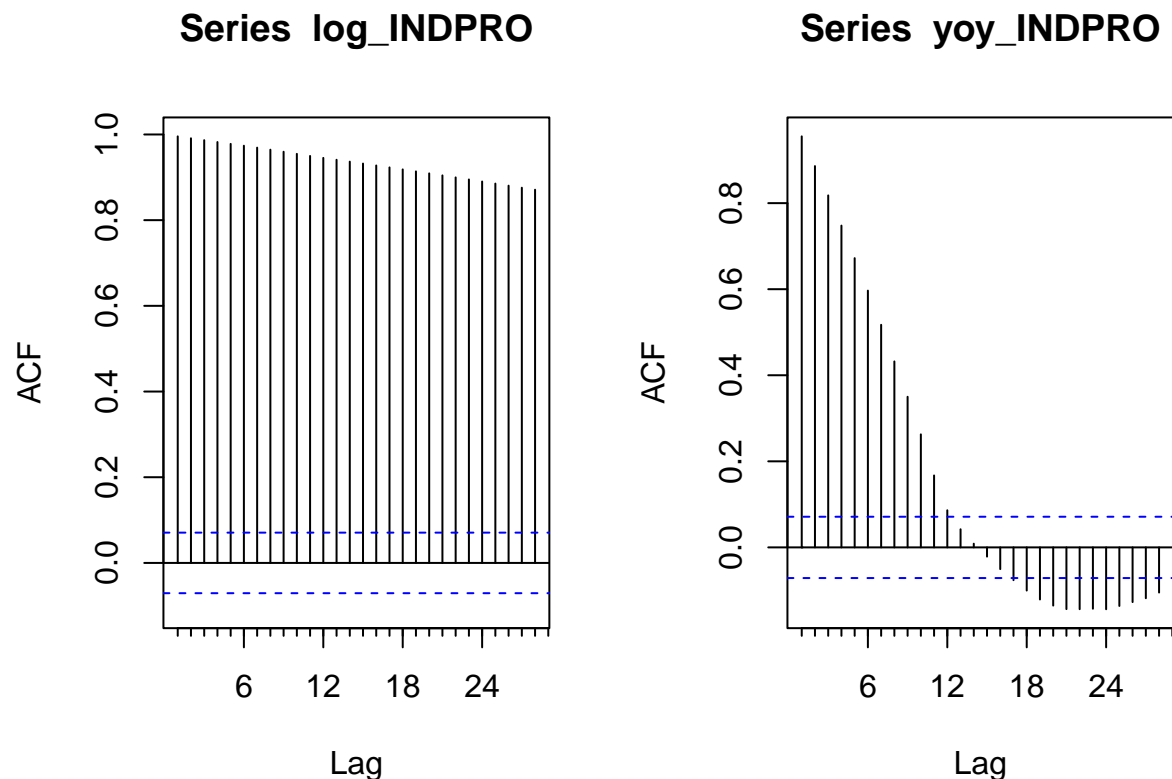


The series of the logged production follows an upward trend showing the increase in the data over time. There are no cyclical or seasonal components. For instance, there are only a few observable downward shifts in the series as the subprime crisis around 2007, and the covid crisis around 2020. The time series does not seem to possess constant first and second moments. Finally, the time series show a slight curvature indicating a decreasing growth in the data over time. By analyzing the graph, the time series does not appear to be stationary.

The time series of the yearly growth rate is experiencing significant shifts over time, and although the variance is significant it seems stable. Besides, no upward, or downward trend can be observed, i.e., the series seems to evolve around a constant mean. It also seems that negative yearly growth rates are followed by negative growth rates (the same can be said for positive yearly growth rates), the data appears to be cyclical. The times series looks graphically stationary.

Subquestion (c)

Using suitable functions from the stats and urca package, assess the properties of both logged industrial production and its yearly growth rate. Plot the autocorrelation function and perform Dickey-Fuller tests to test for a unit root (note the different specifications, i.e. including a drift or a trend), interpret the results.



The ACF plot of the logged production shows a substantial autocorrelation over the entire period which only decays at a very slow-paced overtime. Thus, as in the analysis of the plotted time series, there is strong evidence against the stationarity.

The ACF plot of the yearly growth rate of industrial production has a substantial positive autocorrelation until lag 12 which decreased rapidly. The autocorrelation between lags 12 and 18 is not substantial. Finally, there is an alternation with the autocorrelation which is negative and slightly above the substantial level from lag 18. Thus, the time series looks stationary.

```
##
## #####
## # Augmented Dickey-Fuller Test Unit Root Test #
## #####
##
## Test regression none
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -12.3097  -0.5880   0.0529   0.7056  15.5830
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## z.lag.1 -0.035909    0.009356  -3.838 0.000134 ***
```

```

## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.405 on 755 degrees of freedom
## Multiple R-squared:  0.01914,    Adjusted R-squared:  0.01784
## F-statistic: 14.73 on 1 and 755 DF,  p-value: 0.0001344
##
##
## Value of test-statistic is: -3.838
##
## Critical values for test statistics:
##      1pct  5pct 10pct
## tau1 -2.58 -1.95 -1.62
##
## #####
## # Augmented Dickey-Fuller Test Unit Root Test #
## #####
##
## Test regression none
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.143587 -0.003563  0.000648  0.004666  0.058851
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## z.lag.1  4.514e-04   8.747e-05   5.161 3.13e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.01002 on 767 degrees of freedom
## Multiple R-squared:  0.03356,    Adjusted R-squared:  0.0323
## F-statistic: 26.64 on 1 and 767 DF,  p-value: 3.132e-07
##
##
## Value of test-statistic is: 5.161
##
## Critical values for test statistics:
##      1pct  5pct 10pct
## tau1 -2.58 -1.95 -1.62
##
## #####
## # Augmented Dickey-Fuller Test Unit Root Test #
## #####
##
## Test regression drift
##
##
## Call:

```

```

## lm(formula = z.diff ~ z.lag.1 + 1)
##
## Residuals:
##      Min        1Q      Median        3Q       Max
## -0.142265 -0.003909  0.000693  0.004596  0.059784
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.0128789  0.0032689   3.940  8.9e-05 ***
## z.lag.1      -0.0026467  0.0007911  -3.345  0.000861 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.009922 on 766 degrees of freedom
## Multiple R-squared:  0.0144, Adjusted R-squared:  0.01311
## F-statistic: 11.19 on 1 and 766 DF, p-value: 0.0008614
##
##
## Value of test-statistic is: -3.3455 21.3309
##
## Critical values for test statistics:
##      1pct  5pct 10pct
## tau2 -3.43 -2.86 -2.57
## phi1  6.43  4.59  3.78
##
## #####
## # Augmented Dickey-Fuller Test Unit Root Test #
## #####
##
## Test regression trend
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + tt)
##
## Residuals:
##      Min        1Q      Median        3Q       Max
## -0.142730 -0.003882  0.000696  0.004660  0.059091
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.870e-02  1.047e-02   1.786  0.0746 .
## z.lag.1      -4.412e-03  3.120e-03  -1.414  0.1578
## tt           3.726e-06  6.370e-06   0.585  0.5587
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.009927 on 765 degrees of freedom
## Multiple R-squared:  0.01484, Adjusted R-squared:  0.01227
## F-statistic: 5.762 on 2 and 765 DF, p-value: 0.003282
##
##
## Value of test-statistic is: -1.4141 14.3224 5.7624

```

```
##
## Critical values for test statistics:
##      1pct  5pct 10pct
## tau3 -3.96 -3.41 -3.12
## phi2  6.09  4.68  4.03
## phi3  8.27  6.25  5.34
```

Yoy_prod: The test statistic value is smaller than the critical value ($-3.838 < -2.58$), therefore we can reject the null hypothesis, the time series has no unit root and conclude that the time series is stationary.

Log_prod:\ Test without drift nor trend: We cannot reject that the times series has a unit root as $5.161 > -2.58$. Thus, we cannot find evidence for stationarity.

Test with drift and no trend: The first null hypothesis cannot be rejected as $-3.34 > -3.43$, there is a unit root. The second null hypothesis cannot be rejected either given that $21.33 > 6.43$, thus there is a unit root and no drift. No evidence for stationarity.

Test with both drift and trend: The first null hypothesis (tau3) is not rejected as $-1.41 > -3.96$, a unit root is present. The second null hypothesis (phi3) is rejected given that $5.76 < 6.09$, there is a unit root and there is a trend. The third null hypothesis (phi2) is not rejected $14.32 > 6.09$, a unit root is present and there is no trend nor drift. This is inconsistent with the second null hypothesis.

Subquestion (d)

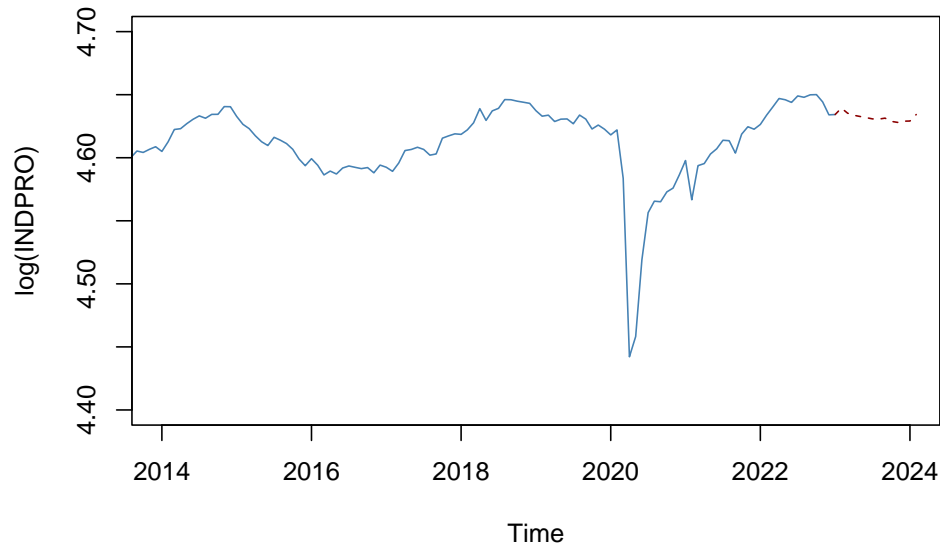
Estimate a suitable AR model (e.g. using the `ar.ols()` function) for the stationary time series (as determined in the previous point). How is the lag order determined by default? Use the estimated model to produce forecasts for the next year and plot them. Interpret their behaviour (i.e. are they converging towards a certain value? What could that be?). Use the produced forecasts to also forecast the change in the original time series.

```
##
## Call:
## ar.ols(x = industrial_prod$log, na.action = na.omit, demean = TRUE,      intercept = TRUE)
##
## Coefficients:
##      1      2      3      4      5      6      7      8
## 1.2637 -0.3294  0.0921  0.0518 -0.0941  0.0529 -0.0165 -0.0789
##      9     10     11     12     13     14     15     16
## 0.0961  0.0492 -0.1650  0.0850 -0.0609  0.0292  0.0281 -0.0108
##     17     18     19     20     21     22     23     24
## 0.0137  0.0036 -0.0460  0.0232 -0.0230  0.0326  0.0277 -0.1539
##     25
## 0.1268
##
## Intercept: 0.001837 (0.0004059)
##
## Order selected 25  sigma^2 estimated as  7.871e-05
##
## Call:
## ar.ols(x = industrial_prod$yoy, na.action = na.omit, demean = FALSE,      intercept = FALSE)
##
## Coefficients:
##      1      2      3      4      5      6      7      8
## 1.2925 -0.3567  0.0895  0.0171 -0.0735  0.0812 -0.0743 -0.0481
##      9     10     11     12     13     14     15     16
## 0.1293  0.0448 -0.1444 -0.6125  0.8058 -0.2258  0.1347 -0.0914
##     17     18     19     20     21     22     23     24
```

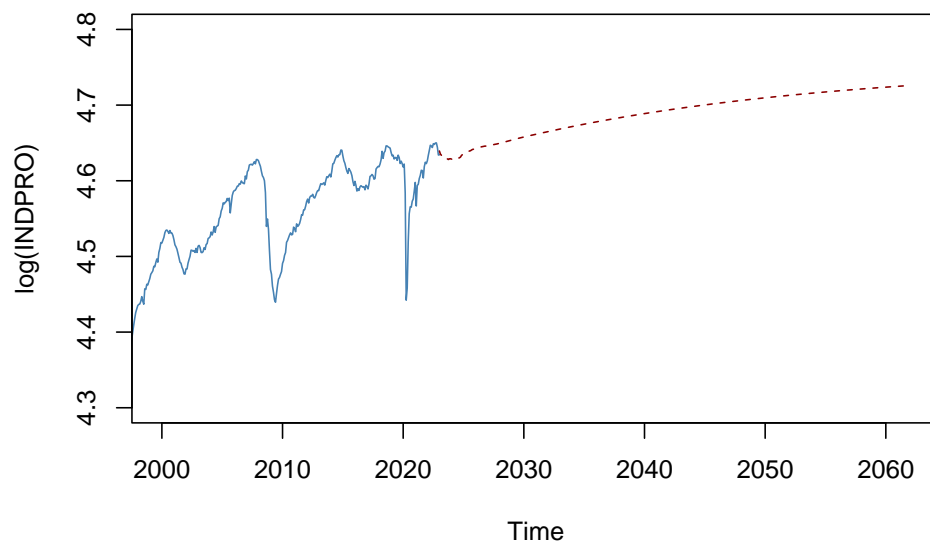
```
## 0.0290 0.0253 -0.1213 0.0522 0.0187 0.1260 -0.0878 -0.5378
##      25      26
## 0.6397 -0.1440
##
## Order selected 26  sigma^2 estimated as 1.042
```

By default the lag order is determined by the AIC information criterion. For the log of INDPRO a lag order of 25 is estimated. The model for the year on year changes is estimated with lag order 26.

12-step ahead forecast for log(INDPRO)



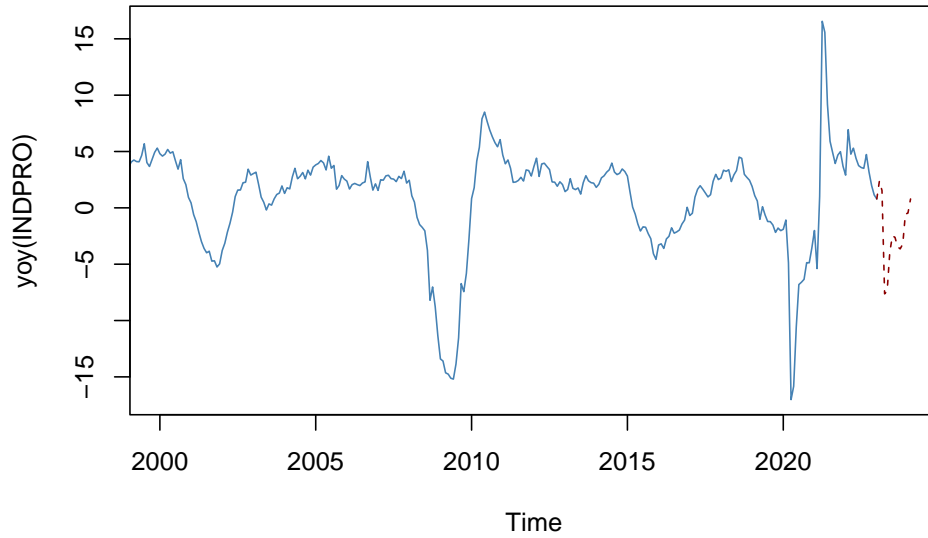
40-year forecast for log(INDPRO)



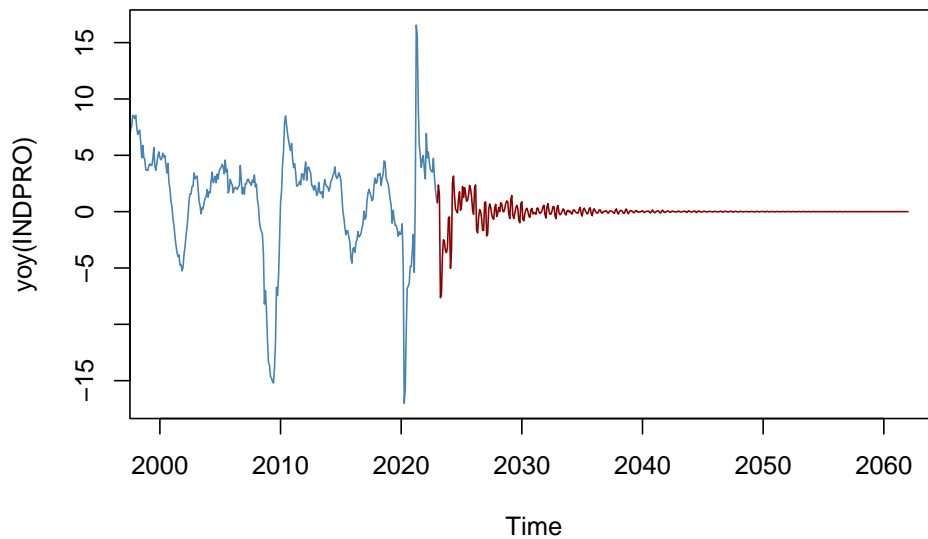
The predicted forecast seems to be stable with no significant shift occurring. When extending the forecasting

period, the data is slightly upward trending and we can observe a divergence effect. It indicates that the value of the log production is expected to increase after every period.

12-step ahead forecast for yoy(INDPRO)

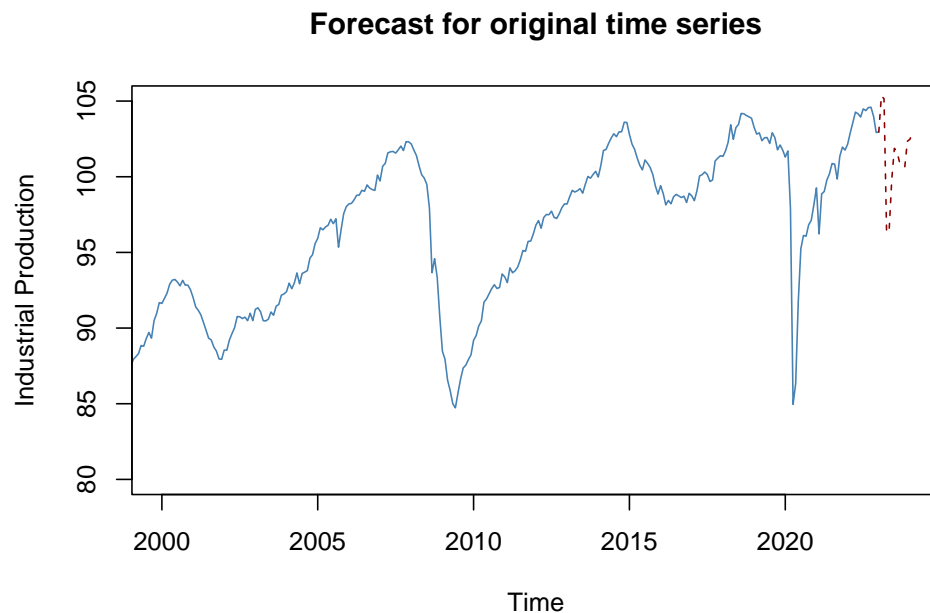


Forecast for yoy(INDPRO)



The forecast of the yearly growth rate shows predicted variation in the short term, however less significant than in the anterior periods. Also, in the long run, the yearly growth rate exhibits a convergence to 0.

```
## [1] 105.33552 105.16440 96.31155 96.49389 99.83880 101.87643 101.63979
## [8] 100.95871 100.78447 100.64529 102.34614 102.47634
```

Subquestion (e) - Bonus question

We start by defining the function.

```
rmse_ar <- function(data, lag, hold_period) {
  #Remove holdout period from the end of the sample
  data_train <- data[1:(length(data) - hold_period)]

  # Estimate the AR model
  ar_model <- ar.ols(data_train, order.max = lag, demean = TRUE, intercept = TRUE)

  # Forecast for the holdout period
  data_test <- data[(length(data) - hold_period + 1):length(data)]
  ar_forecasts <- predict(ar_model, n.ahead = hold_period)

  # Compute the RMSE
  rmse <- sqrt(mean((data_test - ar_forecasts$pred)^2))
  return(rmse)
}
```

```
#RMSE for 50 different lag orders and returning the minimal
rmse <- list()
for (x in 1:50) {
  rmse[[x]] <- rmse_ar(na.omit(industrial_prod$yoy), x, 6)
}
which.min((rmse))
```

```
## [1] 16
```

```
#RMSE for 50 different lag orders and returning the minimal
for (x in 1:50) {
  rmse[[x]] <- rmse_ar(na.omit(industrial_prod$yoy), x, 12)
```

```

}
which.min((rmse))

## [1] 1
#RMSE for 50 different lag orders and returning the minimal
rmse <- list()
for (x in 1:50) {
  rmse[[x]] <- rmse_ar(na.omit(industrial_prod$log), x, 6)
}
which.min((rmse))

## [1] 1
#RMSE for 50 different lag orders and returning the minimal
for (x in 1:50) {
  rmse[[x]] <- rmse_ar(na.omit(industrial_prod$log), x, 12)
}
which.min((rmse))

## [1] 11

```

We run the function for the two time series and compare the RMSE for AR models up to order 50. For a holdout period of 6 months we find that the year on year growth rates are best predicted with an AR(16) model. For a holdout period of 12 months, an AR(1) model produces the lowest RMSE.

For the log(industrial production) the lowest RMSE is produced by an AR(1) model for a 6 month holdout period. Over 12 months an AR(11) model serves as the best predictor.

Remarkably, based on the forecast performance, the optimal lag order is significantly lower than the lag order chosen by the AIC or BIC criterion. The AIC would have selected a model of order 25 (for the logged time series) and 26 (for the year on year growth rates).

Excercise 2 - Killian and Park (2009)

Read Kilian & Park (2009), who discuss the effects of oil price shocks on the US stock market, focus on Sections 2 and 3.1-3.3. Load the provided data by Kilian & Park (2009), which contains a measure of change in oil production, a measure of real economic activity, the real price of oil, and changes in real US dividend growth from 1973M1 to 2016M12.

```
##      GOPC      GRA      RPO      USSR
## 1  11.8773  34.5887 -46.3143 -1.3498
## 2   1.4191  40.0667 -46.6013 -0.3862
## 3   1.1777  42.5462 -45.3973  1.2771
## 4  27.4551  46.6761 -42.1724 -2.4366
## 5 -13.1104  50.6190 -39.8859 -0.2239
## 6  36.2581  51.5436 -39.3027  0.6786
```

Here, *GOPC*, *GRA*, *RPO* and *USSR* refer to *Global Oil Production Change*, *Global Real Activity*, *Real Price of Oil* and *U.S. Stock Returns* respectively. ## Subquestion (a) Using the the packages *vars* in R (or an equivalent one in another language), estimate the VAR described in section 2.2 using the variables in the same order as specified by Kilian and Park (2009).

```
mod1 <- VAR(data, p=24, type="const")
```

Due to the enormity of the VAR consisting of 24 lags and 4 time series, we decided to exclude the output at this point of the assignment.

Subquestion (b)

Using the estimated VAR, compute impulse response functions (take a look at the *irf()* function in *vars*, it uses the same identification scheme as Kilian & Park (2009) propose (recursive ordering based on a Cholesky decomposition of the *vcov*-matrix of the errors) by default. Replicate Figure 1 and the lower panel in figure 3 of Kilian & Park (2009). Interpret the results.

Figure 1

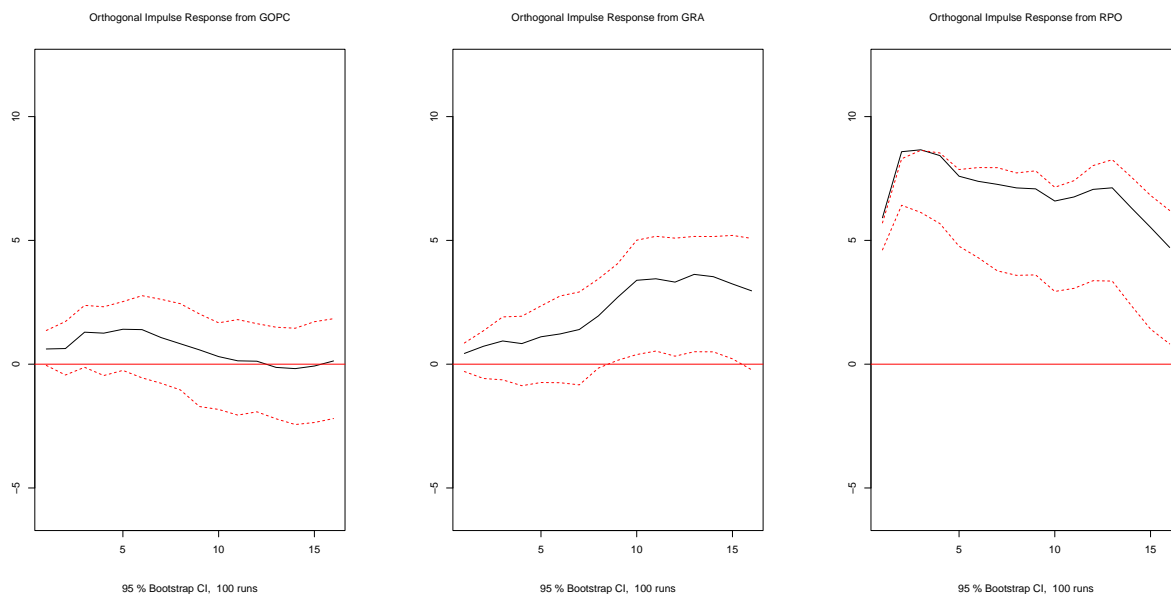
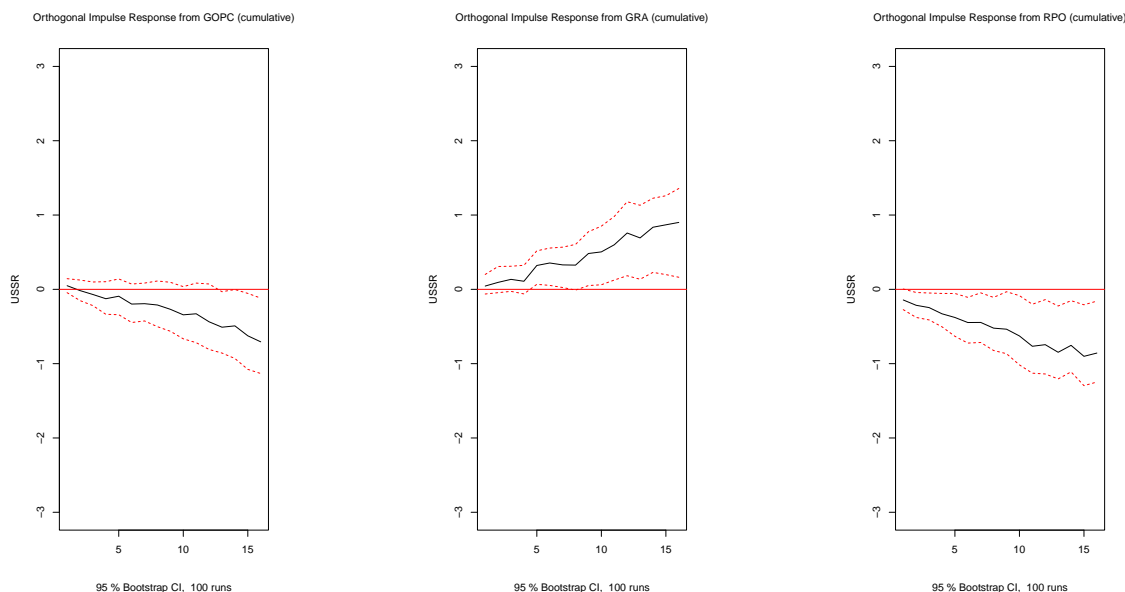


Figure 3



The one standard deviation negative oil supply shock instantaneously increases the oil price and fades to zero after 10 periods. In the paper the confidence intervals were constructed using recursive design wild bootstrap. We use conventional bootstrap standard errors calculated by the vars package in R. When comparing figure 1, the conventional bootstrapped confidence bands are substantially wider. For the confidence bands reported by the vars package, the effect of an aggregate supply shock is not statistically distinguishable from zero in any period. The price of oil gradually increases in response to an aggregate demand shock and is statistically significant ten months after the aggregate demand shock. An unexpected oil-specific demand shock leads to a pronounced increase in the real price of oil immediately and gradually declines. The effect size of a precautionary demand shock remains significantly larger than the other shocks in the following periods. Overall, the figure underscores the notion that oil supply shocks have a comparably minor impact on the real price of oil in comparison to aggregate, and especially oil specific demand shocks.

The lower panel in figure 3 presents the results for the effect on cumulative US real dividends growth rates. A negative oil supply shock decreases real dividend growth rates.

The effect becomes statistically significant after 14 months. In contrast to Figure 1, the effect of unanticipated demand shock differs in its direction to an aggregate demand shock. Unexpected demand shocks significantly decrease dividend growth rates.

Subquestion (c)

Calculate forecast error variance decompositions for the included variables (take a look at the fevd() function in vars). Replicate Table 2 of Kilian and Park (2009). Interpret the results.

```
##      GOPC  GRA  RPO  USSR
## h=1   0.20 0.16 1.69 97.94
## h=2   0.55 0.36 2.09 97.00
## h=3   0.76 0.48 2.12 96.64
## h=12  2.80 6.83 4.53 85.84
## h=Inf 6.63 8.38 7.93 77.06
```

The result of the table is identical to the results in Table 2 by Killian and Park. The effect of shocks in the driving forces of the oil market does not impact significantly the stock return in horizon 1. However, in the long-term horizon it is significant and accounts for the variation of almost 23% in the US real stock return.

The shocks associated with the oil-specific and aggregate demand explain 16.31% of the total long-term variation while in the short-term horizon shocks would only account for 1.85% of the variation. The same is observed for the oil supply shocks where the effect one period later is only 0.2% and grows to explain 6.63% of the variation. The effect is therefore 33 times more important in the later horizon than immediately. The shocks on demand significantly impact more the real stock return than the shocks on the supply.

Subquestion (d)

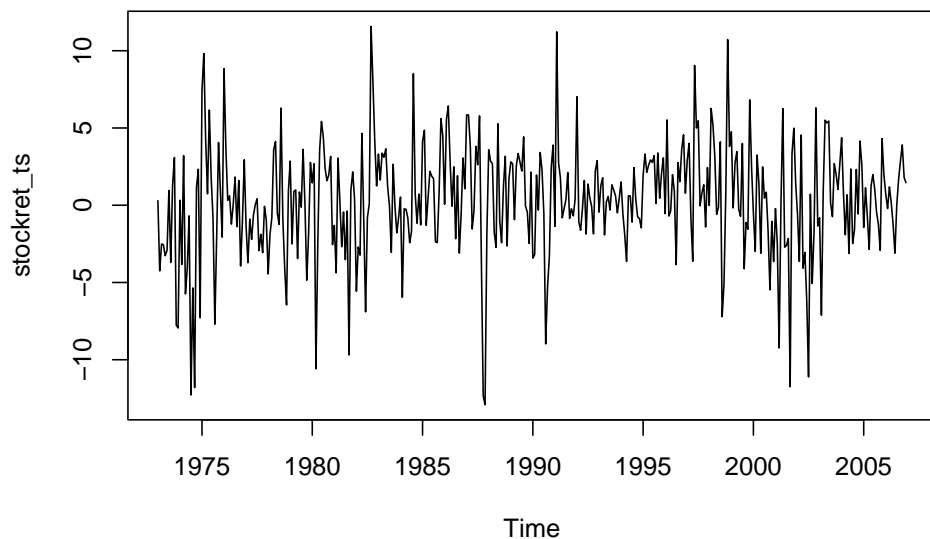
Note that the dataset provided misses US stock market returns (due to the licensing of the underlying time series). Look for alternative data on the US stock market, create a variable similar to the one used by Kilian & Park (2009). Re-estimate the model and replicate Figure 1 again as well as the top panel of Figure 3 and Table 1.5 Interpret the results.

In this exercise we decided to use the S&P 500 returns as well as the CPI data from the FRED database to create monthly real stock returns.

```
## 'data.frame': 770 obs. of 3 variables:
## $ sasdate : chr "1/1/1959" "2/1/1959" "3/1/1959" "4/1/1959" ...
## $ S.P.500 : num 55.6 54.8 56.2 57.1 58 ...
## $ CPIAUCSL: num 29 29 29 29 29 ...

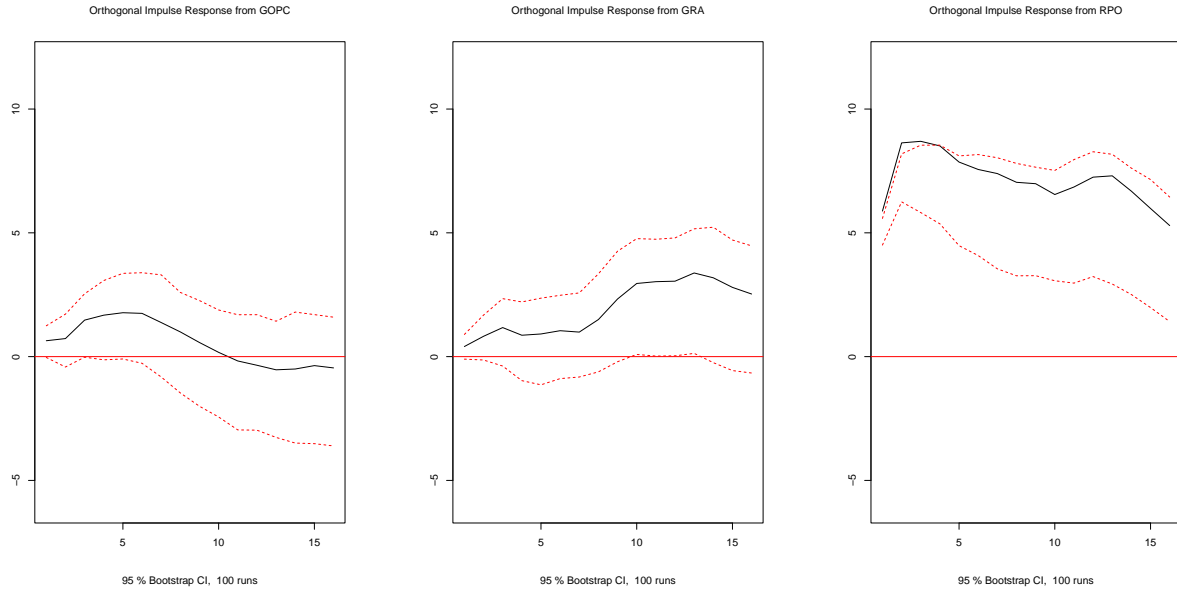
## [1] NA -1.4937564 2.6413340 1.6392707 1.2990903 -1.1037107
## [7] 3.8305679 -0.6720489 -4.1961193 -0.4295228

## Jan Feb Mar Apr May Jun
## 1959 NA -1.493756 2.641334 1.639271 1.299090 -1.103711
```



Using this data, we replicate the VAR given above. Again, the estimated coefficients are given in the appendix.

Figure 1



Top Panel of Figure 3

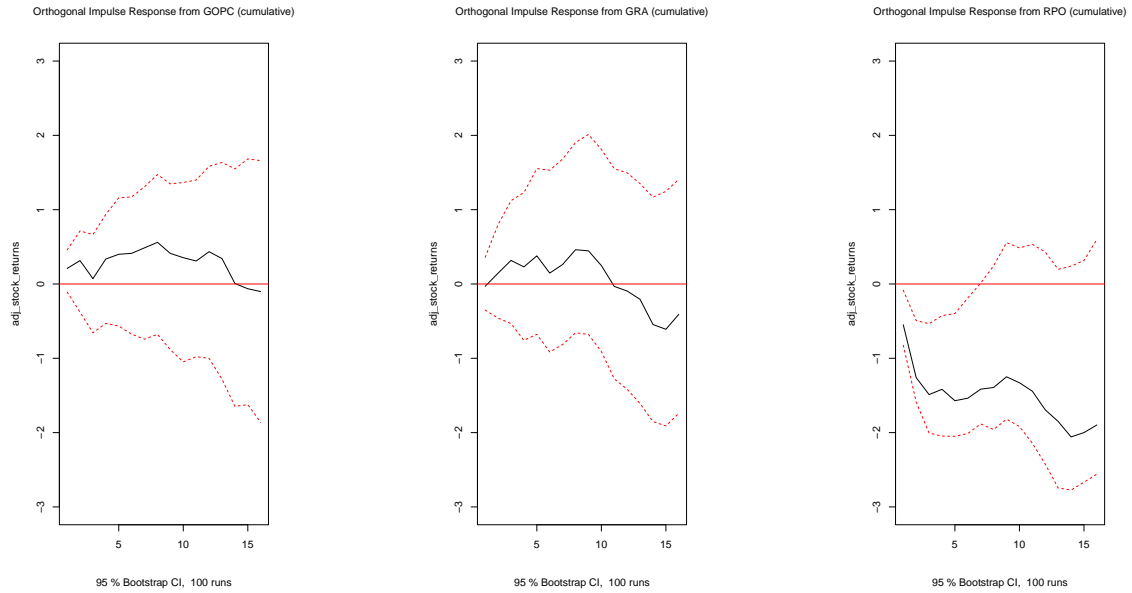


Figure 3 represents cumulative impulse responses, i.e., it is the sum of all impulse responses to either oil supply shocks, aggregate demand shocks, or oil-specific demand shocks over time. We can observe that the cumulative effect of oil supply shock on the stock returns is almost insignificant. It alternates between increased and decreased in the deflated stock returns. Also, it might conduct in an increased value at the initial period, however in the later period the value decreased below the initial one. It seems that an increase in the aggregate demand caused the deflated stock return to rise for several consecutive periods, here 11, and can be considered significant up to period 5 and between periods 7 to 10 approximately. Finally, cumulative impulse responses for shocks to the oil-specific demand cause a significant and sustained decrease in the deflated stock return on the entire period span, it only seems to stop at period 14. The results are once again

similar to the ones in Killian & Park (2009).

Table 1

Similar to before, we replicate table 1 using our data on S&P500 returns.

##	GOPC	GRA	RP0	SP500	Returns
## h=1	0.38	0.01	2.64		96.97
## h=2	0.43	0.25	6.34		92.97
## h=3	0.89	0.48	6.68		91.96
## h=12	1.78	2.35	7.42		88.45
## h=Inf	5.84	6.17	9.04		78.96

There are slight deviations in the data compared to the original document due to the use of a different dataset, however, the impact of each variable has a similar impact in terms of explaining power term of impact on the variation of deflated stock return and the total variation explained by the shocks on the supply and demand of crude oil on deflated stock return is 21% in our table versus 22% by Killian & Park (2009).

The impact on the variation in deflated stock return that can be explained by shock in oil supply, aggregate demand, or oil-specific demand is only 2.64% in the first post-shock period. Thus the three elements have very small explanatory power in terms of variation in deflated stock return in the short term. However, in the long term, the impact of the three variables is 21% thus the shocks in variables driving the oil market have a significant impact on the US deflated stock return. Moreover, we can see that oil-specific demand shocks have the highest impact, and explain 9% of the variation in the long-term, it is followed by the aggregate demand, then the oil supply negative shock. In Killian & Park the oil supply has slightly more explanatory power than the aggregate demand, but they are both almost.