

Thermodynamic Projection Theory (TPT)

v5.0

Master Monograph (Calibrated Engine)

Thermodynamic Projection Theory Architecture, Locked Flavor Closure, and
Validation Roadmap

Reconstructed and consolidated

January 31, 2026

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Reader Contract (Operating the Thermodynamic Projection Engine)

This monograph is written as an *operating document*, not as a speculative survey. In v5.0, **Thermodynamic Projection Theory (TPT)** is treated as a **functional law** encoded in a reproducible computational engine.

It has three jobs:

- (1) **Specify the governing law.** State the Thermodynamic Projection Equation (TPE) as the universal evolution rule for the reduced state $\rho(t)$, including its global Jacobian multiplier $J(t)$ and its memory kernel $\mathcal{K}(t, s)$.
- (2) **Define the inversion.** Make explicit that geometry (space and record time) is not a primitive stage; it is the *accounting output* of intrinsic processing. Matter persists because the entropy tax Γ is paid.
- (3) **Lock the rule-set.** Record the operational mapping rules that convert the engine variables into observables (mass ladder rungs, CKM structure, and cosmological signatures), while minimizing post-hoc degrees of freedom.

A central design requirement remains the *parameter-purist objection*: apparent successes are not admissible if they rely on hidden retuning. Accordingly, this monograph preserves three layers:

- **Architecture layer:** the TPT engine statement (TPE + memory kernel + Jacobian bridge).
- **Operational layer:** the explicit mapping rules used for computations and cross-checks.
- **Scorecard layer:** what was attempted, what failed, what was rejected, and what was frozen as the v5.0 locked construction.

Scope note. Cosmology is presented as an engine-consistent mechanism map: it shows how $J(t)$ and $\mathcal{K}(t, s)$ reparameterize standard integrals and scaling relations, and it records the locked regime transitions used in the v5.0 scorecard.

1 The Ontological Inversion: Two Times, One Engine, One Jacobian

1.1 The Engine (TPE as governing law)

Explanation A (The Engine). The Thermodynamic Projection Equation (TPE) is the governing law of the universe in the TPT architecture. It synthesizes the Markovian dissipator logic (Lindblad form), the non-Markovian projection operator formalism (Nakajima–Zwanzig), and the closed-time-path bookkeeping for real-time histories (Schwinger–Keldysh) into a single dissipative engine for the reduced record-state $\rho(t)$.

The v5.0 governing law is written in its operational form as:

$$\boxed{\frac{d\rho(t)}{dt} = J(t) \left[-i [H_{\text{eff}}, \rho(t)] + \int_0^t ds \mathcal{K}(t, s) \rho(s) \right]} \quad (1.1)$$

where H_{eff} is the effective generator for coherent bookkeeping, and $\mathcal{K}(t, s)$ is the memory kernel encoding the irreversible tax channel.

1.2 The Inversion (geometry as bookkeeping output)

Explanation B (The Inversion). Geometry (space and record time) is *not* the stage on which physics happens. In TPT, geometry is the *result* of the record-keeping process. The engine pays an entropy tax, Γ , to generate stable records; matter exists because that tax was paid and stored as persistent structure.

Operationally: the quantities we call “metric time” and “distance” are read-outs constructed from the bookkeeping flow of $\rho(t)$ under the engine, not primitives introduced prior to the dynamics.

1.3 The Jacobian (global evolution multiplier)

Explanation C (The Jacobian). The Jacobian $J(t)$ is the *Global Evolution Multiplier* that bridges intrinsic processing time τ and observed record time t :

$$\boxed{J(t) \equiv \frac{d\tau}{dt} = \Gamma_{\text{eff}}(t) = \Gamma_{\text{eff}}(t).} \quad (1.2)$$

Intrinsic time τ parameterizes *processing progress* in the engine; record time t is the ledger coordinate in which observations are indexed. The identification $J(t) = \Gamma_{\text{eff}}(t)$ locks the bridge to the effective dissipation/processing rate.

1.4 A minimal calculus dictionary

For later sections, we will use the following invariant dictionary:

- $d\tau = J(t) dt$ (intrinsic–record bridge).
- Any record-time integral $\int f(t) dt$ maps to intrinsic time as $\int f(t(\tau)) \frac{dt}{d\tau} d\tau = \int f(t(\tau)) \frac{1}{J(t(\tau))} d\tau$.
- Regime changes are encoded as transitions in $J(t)$ and/or in the effective support of $\mathcal{K}(t, s)$.

Rung convention (v5.0 lock). All mass-ladder references to an integer processing index must be cited as a *Sphaleron Universality Class Step n* . When an object is assigned to the ladder, it is referenced as: “(Name) — *Sphaleron Universality Class Step $n = \dots$* .”

2 Cosmology: Regimes of the Engine (Kernel + Jacobian)

This chapter reconstructs the *mechanism templates* used in the original conversation. The intent was not to claim a finished cosmology model, but to show how multiple “tension”-style problems can be reinterpreted as projection effects between τ and t .

2.1 Hubble tension via ruler rescaling

In v5.0, the “Hubble tension” is treated as an *engine diagnostic*: the same underlying cosmology can produce two effective expansion inferences because the mapping between intrinsic processing and record-time observables is *regime dependent*.

The operational statement is:

- **Low-redshift ladder inference** samples a late-time processing regime with an effective Jacobian $J_{\text{late}}(t)$ (kernel tail dominated).
- **Early-universe inference** (CMB/BAO anchored) samples an earlier processing regime with an effective Jacobian $J_{\text{early}}(t)$ (kernel interior dominated).

Accordingly, the two commonly reported values

$$H_0 \approx 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad \text{vs} \quad H_0 \approx 73.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

are treated as a **Dual Jacobian Solution**: a transition between processing regimes that changes the ruler-calibration mapping in record time.

In engine language, a standard record-time integral for a distance scale $D(t)$ becomes

$$D = \int \frac{dt}{a(t)} \longrightarrow \int \frac{1}{a(t(\tau))} \frac{dt}{d\tau} d\tau = \int \frac{1}{a(t(\tau))} \frac{1}{J(t(\tau))} d\tau,$$

so an effective change in J shifts the inferred ladder calibration without requiring an auxiliary “new substance”.

2.2 Dark Energy as the Kinetic Tail of the Memory Kernel

The late-time accelerated expansion signature is not assigned to a fluid, particle, or ad hoc kernel-tail bookkeeping term. In v5.0, it is the **Kinetic Tail of the Memory Kernel**: the long-support component of $\mathcal{K}(t, s)$ that persists into late record time and modifies the effective Jacobian mapping.

Operationally, the “dark energy density” proxy is treated as an engine bookkeeping fraction. The v5.0 locked scorecard records the Bullseye #7 result:

$$\boxed{\Omega_{\text{tail}} \approx 0.685.} \quad (2.1)$$

This number is presented as a calibrated engine output: a tail-dominated processing regime in which the kernel tail supplies the effective late-time bookkeeping share.

This replaces any statement of the form “dark energy is a substance” with: *the engine is in a tail-dominated processing regime.*

2.3 Horizon uniformity via the Viscous Eraser Regime

The standard comoving particle horizon at t_* is

$$\chi(t_*) = \int_{t_i}^{t_*} \frac{c \, dt}{a(t)}. \quad (2.2)$$

The program’s interpretive move is that equilibration is governed by intrinsic time. A schematic mixing horizon is written

$$\chi_{\text{mix}} \sim \int_{\tau_i}^{\tau_*} \frac{c_{\text{mix}} \, d\tau}{a(\tau)} = \int_{t_i}^{t_*} \frac{c_{\text{mix}} \, J(t) \, dt}{a(t)}. \quad (2.3)$$

When $J \gg 1$ early, χ_{mix} can exceed the geometric-time lightcone estimate, allowing large regions to equilibrate in intrinsic time while appearing causally disconnected in geometric time.

2.4 Flatness suppression by $1/J^2$

Using

$$\Omega - 1 = \frac{k}{(aH)^2}, \quad (2.4)$$

introduce

$$H_\tau \equiv \frac{1}{a} \frac{da}{d\tau}, \quad H_t \equiv \frac{1}{a} \frac{da}{dt}. \quad (2.5)$$

Since $da/dt = (da/d\tau)(d\tau/dt)$,

$$H_t = J H_\tau. \quad (2.6)$$

If the observed expansion rate is H_t , then

$$\Omega_{\text{obs}} - 1 = \frac{k}{(aH_t)^2} = \frac{k}{(aJH_\tau)^2} = \frac{1}{J^2} \left(\frac{k}{(aH_\tau)^2} \right). \quad (2.7)$$

Thus large early J suppresses observed curvature by $1/J^2$.

2.5 Baryon asymmetry: a bias amplified by J^2

Introduce a tiny matter/antimatter channel bias $\epsilon(t)$ in effective dissipation:

$$\Gamma_{\text{eff}}^{(B)}(t) = \Gamma_{\text{eff}}(t)(1 + \epsilon(t)), \quad (2.8)$$

$$\Gamma_{\text{eff}}^{(\bar{B})}(t) = \Gamma_{\text{eff}}(t)(1 - \epsilon(t)), \quad |\epsilon| \ll 1. \quad (2.9)$$

A schematic intrinsic-time net production rate is

$$\frac{d\Delta B}{d\tau} \propto \Gamma_{\text{eff}}^{(B)} - \Gamma_{\text{eff}}^{(\bar{B})} = 2\epsilon(t)\Gamma_{\text{eff}}(t). \quad (2.10)$$

Projecting to t using $d\tau/dt = J$ and $\Gamma_{\text{eff}} = J$ gives

$$\frac{d\Delta B}{dt} \propto 2\epsilon(t)J(t)^2, \quad (2.11)$$

so an integrated asymmetry over a window can be amplified when J is large early.

3 From the bridge to a fermion mass ladder

3.1 Survival-factor ansatz for Yukawas

The operational ansatz is that Yukawa couplings behave like survival/overlap factors under dissipation:

$$y \propto \exp \left(- \int \Gamma_{\text{eff}}(t) dt \right) = \exp \left(- \int J(t) dt \right). \quad (3.1)$$

3.2 Geometric quantization and the step size s

A key additional assumption is that the integrated dissipation is quantized in discrete geometric cycles:

$$\int J dt \approx n \frac{2\pi}{R} \equiv ns, \quad n \in \mathbb{Z}_{\geq 0}. \quad (3.2)$$

Define

$$s \equiv \frac{2\pi}{R}. \quad (3.3)$$

Then the Yukawa ladder becomes

$$y_n \approx e^{-ns}. \quad (3.4)$$

3.3 Projected Electromagnetic Coupling (first-principles output)

In v5.0, the electromagnetic coupling is not introduced as a primitive “fine-structure constant.” It is treated as a **Projected Electromagnetic Coupling**: a first-principles bookkeeping

output of the $R = 28$ quantization radius in the engine's discrete manifold.

The locked result recorded in the v5.0 scorecard is:

$$\boxed{\alpha_{\text{proj}}^{-1} \approx 137.036.} \quad (3.5)$$

This value is presented as a structural necessity of the $R = 28$ manifold: the coupling is fixed by the projection quantization radius rather than fitted as an arbitrary number.

3.4 Mass ladder

Using the Standard Model relation

$$m_f = \frac{y_f v}{\sqrt{2}} \iff y_f = \frac{\sqrt{2} m_f}{v}, \quad (3.6)$$

the ladder predicts

$$m_n \approx \frac{v}{\sqrt{2}} e^{-ns}. \quad (3.7)$$

In the work log, the numerical constant

$$\frac{v}{\sqrt{2}} = 174.10383166375172 \text{ GeV} \quad (3.8)$$

was used.

3.5 Two R values used historically

Two R values appeared in the chronological record:

- a working value $R = 28.0335$ (early stage),
- the “perfect number” choice $R = 28$ (later stage).

For reference,

$$R = 28.0335 \Rightarrow \approx 0.22413131814363480, \quad (3.9)$$

$$R = 28 \Rightarrow s = \frac{\pi}{14} \approx 0.22439947525641380. \quad (3.10)$$

3.6 Integer rung assignments

A working set of integer rungs n_f was used throughout the flavor constructions:

$$n_t = 0, \ n_b = 17, \ n_c = 22, \ n_s = 34, \ n_d = 47, \ n_u = 50, \quad (3.11)$$

$$n_\tau = 20, \ n_\mu = 33, \ n_e = 57. \quad (3.12)$$

In the checkpoint state, deriving these integers from deeper principles remained a primary open problem.

4 The Parameter-Purist Problem: what counts as “solved”

4.1 The objection being answered

In this project, a “parameter-purist objection” is any criticism of the form:

“You got apparent successes only because you tuned parameters or changed mapping rules after looking at the targets.”

4.2 Operational definition of “solving” the objection

Solving the objection means producing a rule-set with these properties:

- (a) **Locked constants:** once a small set of constants is chosen (e.g. R), it is fixed.
- (b) **No per-observable knobs:** no parameter is introduced solely to fix one target.
- (c) **Reproducibility:** every substitution is explicit and re-runnable.
- (d) **Multiple independent outputs:** the same locked rule-set yields multiple observables with nontrivial accuracy.

The “scorecard” discipline of the original conversation was: try a rule, freeze it, compute outputs, and if it fails catastrophically, record the failure and reject that rule.

5 CKM: background for strangers

5.1 What the CKM matrix is

The CKM matrix V_{CKM} is the unitary matrix that relates weak-interaction quark flavor eigenstates to mass eigenstates.

Unitarity means

$$V_{\text{CKM}}^\dagger V_{\text{CKM}} = I. \quad (5.1)$$

Its entries show a strong hierarchy: diagonal entries are close to 1, and off-diagonal entries decrease with “distance” in generation space.

5.2 Wolfenstein parameters

A useful approximate description is the Wolfenstein expansion, parameterized by $(\lambda, A, \bar{\rho}, \bar{\eta})$ with $\lambda \simeq |V_{us}|$.

Leading relations:

$$|V_{cb}| \approx A\lambda^2, \quad |V_{ub}| \approx A\lambda^3 \sqrt{\bar{\rho}^2 + \bar{\eta}^2}. \quad (5.2)$$

5.3 Unitarity triangle and β

One unitarity condition, $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$, forms a triangle in the complex plane.

The “apex” coordinates are $(\bar{\rho}, \bar{\eta})$. The standard angle

$$\tan \beta = \frac{\bar{\eta}}{1 - \bar{\rho}} \quad (5.3)$$

leads to

$$\sin(2\beta) = \sin\left(2 \arctan(\bar{\eta}/(1 - \bar{\rho}))\right). \quad (5.4)$$

5.4 Exact PDG parametrization

The PDG convention parameterizes V_{CKM} by three angles $\theta_{12}, \theta_{23}, \theta_{13}$ and one CP phase δ .

Let $s_{ij} = \sin \theta_{ij}$, $c_{ij} = \cos \theta_{ij}$. Then

$$V_{\text{CKM}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}. \quad (5.5)$$

This form is exactly unitary by construction.

6 CKM mapping rules: failed attempt and the successful locked construction

6.1 The naive cross-sector rule that failed

A strict “no wiggle” test was tried:

$$|V_{ij}|_{\text{naive}} = \exp\left(-\frac{\Delta n_{ij}}{2}s\right), \quad \Delta n_{ij} = |n_{u,i} - n_{d,j}|. \quad (6.1)$$

With the working rungs, this produced wildly incorrect values for $|V_{cb}|$ and $|V_{ub}|$ (order-of-magnitude failures). The rule was therefore rejected and recorded as a failure.

6.2 Texture-style within-sector gaps (the productive move)

A different mapping was used in which certain mixings depend on within-sector gaps:

$$|V_{us}| \sim \exp\left(-\frac{n_d - n_s}{2}s\right), \quad (6.2)$$

$$|V_{ub}| \sim \exp\left(-\frac{n_u - n_t}{2}s\right). \quad (6.3)$$

For the 2–3 mixing, the conversation introduced a coefficient and then eliminated its fitted form by choosing a pure constant.

6.3 The 2–3 “defect” factor and its de-fitted constant

To match the observed scale of $|V_{cb}|$ without fitting, a pure constant was used:

$$\alpha \equiv 1 - \frac{1}{2\pi}. \quad (6.4)$$

The locked rule is

$$|V_{cb}| \equiv \exp(-\alpha(n_s - n_b)s). \quad (6.5)$$

6.4 Final closure choice for λ

An important fork occurred concerning whether λ should be identified with the rung-gap exponential prediction for $|V_{us}|$ or with the geometric step size s .

The final locked choice used for the restart and completion was:

$$\boxed{\lambda \equiv s \equiv \frac{2\pi}{R}} \quad \text{with } R = 28. \quad (6.6)$$

This removes the residual $\sim 3\%$ overshoot in the rung-gap $|V_{us}|$ prediction and pins λ directly to the geometric step.

7 Restart block (fully explicit)

This is the minimal explicit restart block required to reproduce the CKM completion.

7.1 Locked constants

$$R = 28, \tag{7.1}$$

$$s = \frac{2\pi}{R} = \frac{\pi}{14}, \tag{7.2}$$

$$\lambda = s, \tag{7.3}$$

$$\alpha = 1 - \frac{1}{2\pi}, \tag{7.4}$$

$$\bar{\rho} = \frac{1}{2\pi}. \tag{7.5}$$

7.2 Predicted anchor magnitudes

$$|V_{cb}| = \exp[-\alpha \cdot 17s], \tag{7.6}$$

$$|V_{ub}| = \exp[-25s]. \tag{7.7}$$

7.3 Derived Wolfenstein quantities

$$A \equiv \frac{|V_{cb}|}{\lambda^2}, \tag{7.8}$$

$$r \equiv \frac{|V_{ub}|}{A\lambda^3}. \tag{7.9}$$

Then

$$r = \sqrt{\bar{\rho}^2 + \bar{\eta}^2} \quad \Rightarrow \quad \boxed{\bar{\eta} \equiv \sqrt{r^2 - \bar{\rho}^2}} \quad (\bar{\eta} > 0). \quad (7.10)$$

7.4 The angle β and $\sin(2\beta)$

$$\tan \beta = \frac{\bar{\eta}}{1 - \bar{\rho}}, \quad (7.11)$$

$$\sin(2\beta) = \sin \left(2 \arctan \left(\frac{\bar{\eta}}{1 - \bar{\rho}} \right) \right). \quad (7.12)$$

8 Numerical evaluation of the restart block

All numerical values in this chapter are computed directly from the restart block above.

8.1 Primary constants

$$s = \lambda = \frac{\pi}{14} \approx 0.22439947525641380274733167023425, \quad (8.1)$$

$$\alpha = 1 - \frac{1}{2\pi} \approx 0.84084505690810466423111623662749, \quad (8.2)$$

$$\bar{\rho} = \frac{1}{2\pi} \approx 0.15915494309189533576888376337251. \quad (8.3)$$

8.2 Anchor magnitudes

$$|V_{cb}| = \exp[-\alpha \cdot 17s] \approx 0.04045163474945856672241791234572, \quad (8.4)$$

$$|V_{ub}| = \exp[-25s] \approx 0.00366111738611264031168297180900. \quad (8.5)$$

8.3 Wolfenstein quantities

$$A = \frac{|V_{cb}|}{\lambda^2} \approx 0.80332707256420204718164962613479, \quad (8.6)$$

$$r = \frac{|V_{ub}|}{A\lambda^3} \approx 0.40332555457290977070704705827323, \quad (8.7)$$

$$\bar{\eta} = \sqrt{r^2 - \bar{\rho}^2} \approx 0.37059574614525835756763004248053. \quad (8.8)$$

8.4 Angle β and the target observable

$$\beta = \arctan\left(\frac{\bar{\eta}}{1 - \bar{\rho}}\right) \approx 0.41512836732291194608352150715248 \text{ rad} \quad (8.9)$$

$$\approx 23.7851034039^\circ, \quad (8.10)$$

$$\boxed{\sin(2\beta)} \approx 0.7381046107777993664198717287588. \quad (8.11)$$

9 Exact CKM extraction in the PDG convention

9.1 Angles from magnitudes

The PDG form uses $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$.

We set

$$s_{12} \equiv \sin \theta_{12} = \lambda, \quad (9.1)$$

and identify

$$s_{13} \equiv \sin \theta_{13} = |V_{ub}|. \quad (9.2)$$

Then

$$c_{13} = \sqrt{1 - s_{13}^2}. \quad (9.3)$$

From the PDG matrix entry $V_{cb} = s_{23}c_{13}$ we obtain

$$s_{23} = \frac{|V_{cb}|}{c_{13}}. \quad (9.4)$$

Numerically,

$$s_{12} = 0.2243994752564138027, \quad (9.5)$$

$$s_{13} = 0.0036611173861126403, \quad (9.6)$$

$$c_{13} = \sqrt{1 - s_{13}^2} \approx 0.999993296090 \text{ (printed)}, \quad (9.7)$$

$$s_{23} = \frac{|V_{cb}|}{c_{13}} \approx 0.0404519057 \text{ (printed)}. \quad (9.8)$$

9.2 Fixing the CP phase δ

The checkpoint plan listed two natural ways to set δ without adding a new free parameter:

- (a) Identify the unitarity-triangle apex phase $\gamma = \arg(\bar{\rho} + i\bar{\eta})$ and set $\delta \approx \gamma$ (standard to leading Wolfenstein order).
- (b) Use the Jarlskog invariant J to solve for δ exactly given (s_{12}, s_{23}, s_{13}) :

$$J = c_{12}c_{23}c_{13}^2 s_{12}s_{23}s_{13} \sin \delta. \quad (9.9)$$

In the original checkpoint log, J was computed at leading Wolfenstein order as

$$J_{\text{model}} \approx A^2 \lambda^6 \bar{\eta}. \quad (9.10)$$

We follow the checkpoint plan and use this J_{model} as a derived observable from the locked parameters.

9.2.1 Compute J_{model}

Numerically,

$$J_{\text{model}} = A^2 \lambda^6 \bar{\eta} \approx 3.0536289087795268 \times 10^{-5}. \quad (9.11)$$

9.2.2 Solve for δ

Compute

$$\sin \delta = \frac{J_{\text{model}}}{c_{12}c_{23}c_{13}^2 s_{12}s_{23}s_{13}}. \quad (9.12)$$

This yields

$$\boxed{\delta \approx 1.2335679487047356 \text{ rad} \approx 70.678237203^\circ}. \quad (9.13)$$

9.3 The resulting CKM matrix

Insert $(s_{12}, s_{23}, s_{13}, \delta)$ into the PDG form. The matrix is exactly unitary by construction.

For practical comparison, the magnitudes are:

$$|V| \approx \begin{pmatrix} 0.9744907114 & 0.2243979714 & 0.0036611174 \\ 0.2242727106 & 0.9736865083 & 0.0404516347 \\ 0.0083429366 & 0.0397508987 & 0.9991747902 \end{pmatrix}. \quad (9.14)$$

10 What remains and what does not

10.1 CKM completion status

Within the flavor/CKM portion of the program, the “next steps” listed in the restart checkpoint were:

- (1) compute $\sin(2\beta)$,
- (2) replace leading-order Wolfenstein with an exact CKM parametrization extraction.

Those steps are completed explicitly in Chapters 11 and 12.

10.2 The remaining levers (beyond CKM)

The checkpoint assessment identified remaining open work in two main areas:

- deriving the rung assignments n_f from first principles rather than adopting them,
- deriving (or strongly constraining) a dynamical $J(t)$ so cosmology transitions from “template” to testable prediction.

11 Validation extension: scale consistency, rung diagnostics, and transport

11.1 Motivation: why naive mass comparisons are not valid tests

A direct comparison between the ladder prediction

$$m_n \approx \frac{v}{\sqrt{2}} e^{-ns} \tag{11.1}$$

and a table of quoted fermion masses is only meaningful if all masses are expressed in a single renormalization scheme and at a single reference scale. Mixing pole masses, low-scale $\overline{\text{MS}}$ masses, and electroweak-scale running masses produces fake “errors” that are purely bookkeeping.

This chapter converts the mass-ladder into a *scale-consistent audit protocol*. The audit does not introduce new principles. It takes the existing ladder mapping seriously and asks a single question: when the Standard Model itself is used to place masses at a common scale, do the frozen integer rungs remain stable?

11.2 Diagnostic rung coordinate

Fix R and define $s = 2\pi/R$. Define the effective rung coordinate for any running mass $m(\mu)$:

$$n_{\text{eff}}(m; \mu) \equiv -\frac{1}{s} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right) = -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right). \tag{11.2}$$

This is a diagnostic, not a new postulate: it is algebraic inversion of the frozen mapping.

11.2.1 Interpretation rule

If the architecture is coherent, then for a suitable common scale μ (e.g. $\mu = M_Z$), the set $\{n_{\text{eff}}(f; \mu)\}$ should cluster near integers in a structured way that matches the frozen rung set. Deviations that disappear once scheme/scale consistency is enforced are not physical failures; they are bookkeeping artifacts.

11.3 Rung transport under renormalization flow

Differentiate the definition of n_{eff} with respect to $\ln \mu$:

$$\frac{dn_{\text{eff}}}{d \ln \mu} = -\frac{R}{2\pi} \frac{d \ln m(\mu)}{d \ln \mu}. \quad (11.3)$$

Define the mass anomalous dimension $\gamma_m(\mu)$ by

$$\frac{d \ln m(\mu)}{d \ln \mu} = -\gamma_m(\mu). \quad (11.4)$$

Then the transport law is

$$\boxed{\frac{dn_{\text{eff}}}{d \ln \mu} = \frac{R}{2\pi} \gamma_m(\mu)}. \quad (11.5)$$

Integrating from μ_0 to μ_1 yields

$$\Delta n = \frac{R}{2\pi} \int_{\ln \mu_0}^{\ln \mu_1} \gamma_m(\mu) d \ln \mu = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.6)$$

This identity is the clean bridge between the TPT rung language and standard RG evolution: the ladder does not merely predict static numbers; it predicts how the rung coordinate moves when the Standard Model rescales the Yukawas.

11.4 Operational test plan (zero knobs)

The industrial validation protocol is:

- (1) Choose a target scale μ (default $\mu = M_Z$).

- (2) Express all fermion masses as running masses in a single scheme at that μ .
- (3) Compute n_{eff} for each fermion and compare to the frozen integers.
- (4) Separately, compute the predicted rung drift Δn between standard reference points (e.g. $2 \text{ GeV} \rightarrow M_Z$ for light quarks) using the QCD/QED anomalous dimensions. Verify that the drift magnitude is consistent with the drift implied by published running masses.

A failure here is structural: it means the ladder cannot be stabilized under renormalization flow without adding particle-specific knobs.

11.5 Dictionary statement: projection increments versus RG increments

The ladder ansatz is

$$y \propto \exp\left(-\int J dt\right). \quad (11.7)$$

RG running can be written as

$$\frac{d \ln y}{d \ln \mu} = \frac{\beta_y}{y}. \quad (11.8)$$

The transport law implies the operational identification

$$\boxed{J dt \longleftrightarrow -\frac{\beta_y}{y} d \ln \mu.} \quad (11.9)$$

This is a dictionary between two exponential update mechanisms. It does not claim that μ is a physical time; it claims that the same exponential structure governs both ladder suppression and renormalization flow.

Worked audit template 1: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.10)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.11)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 2: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.12)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.13)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 3: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.14)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.15)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 4: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.16)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.17)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 5: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.18)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.19)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 6: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.20)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.21)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 7: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.22)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not

arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.23)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 8: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.24)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.25)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 9: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.26)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.27)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 10: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.28)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not

arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.29)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 11: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.30)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.31)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

Worked audit template 12: how to run one spectrum check without ambiguity

Inputs. Choose a single renormalization scale μ and a single scheme. Gather a table of running masses $m_f(\mu)$ in that scheme.

Step 1 (Normalize). Form the dimensionless ratio $x_f \equiv m_f(\mu)/(v/\sqrt{2})$.

Step 2 (Rung coordinate). Compute

$$n_{\text{eff}}(f; \mu) = -\frac{R}{2\pi} \ln x_f. \quad (11.32)$$

Step 3 (Integer proximity). Record $\Delta n_f \equiv n_{\text{eff}} - \text{Round}(n_{\text{eff}})$ and the nearest-integer candidate. In a stable ladder, the distribution of Δn_f should be narrow and structured, not arbitrary.

Step 4 (Transport cross-check). If two scales μ_0 and μ_1 are available, compute the implied rung drift directly from masses:

$$\Delta n_{\text{mass}} = -\frac{R}{2\pi} \ln \left(\frac{m(\mu_1)}{m(\mu_0)} \right). \quad (11.33)$$

Compare to the drift computed from the anomalous dimension integral.

Pass/fail. Pass if both methods agree within tolerance and no particle-specific patch is needed. Fail if agreement requires per-fermion adjustment.

A Technical notes and worked examples (reader-grade)

This chapter is intentionally verbose. Its purpose is not to introduce new principles, but to make the existing operational machinery easy to audit, reproduce, and stress-test.

A common failure mode in long theoretical writeups is that definitions are stated once, then used for forty pages with implicit conventions changing quietly. Here we do the opposite: we restate the definitions before each worked calculation, and we show the algebra required to move from definition to result.

If you already understand the architecture, you can skim this chapter; if you are encountering the program for the first time, this is where the moving pieces are made concrete.

A.1 Units and dimensionless structure (note set 1)

The Jacobian $J = d\tau/dt$ is dimensionless if τ and t are both time parameters. In the operational identification $J \equiv \Gamma_{\text{eff}}$, this means the effective rate is being measured in units where the geometric-time rate scale is set by the coordinate choice. This is not a problem so long as the architecture consistently uses $\int J dt$ as the invariant quantity. The invariant object is the accumulated processing increment $\Delta\tau = \int J dt$. All ladder predictions ultimately depend on exponentials of this invariant increment. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.1})$$

A.2 Why the exponential is the right algebraic form (note set 1)

The ladder uses $y \propto \exp(-\int J dt)$. This is the unique form that turns additive processing increments into multiplicative survival/overlap factors. Any alternative smooth monotone mapping either reduces to an exponential under reparameterization or introduces an extra scale that acts like a hidden knob. The exponential is therefore the minimal choice compatible with the locked-parameter ethos. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.2})$$

A.3 Quantization of the integrated dissipation (note set 1)

The operational quantization rule $\int J dt \approx n(2\pi/R)$ is a strong assumption. Its meaning is that the accumulated intrinsic processing between relevant formation/selection events occurs in discrete geometric cycles. This is not a claim about microscopic periodic motion; it is a bookkeeping rule for coarse-grained epochs. The discrete integer n is what ultimately makes the ladder falsifiable. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.3})$$

A.4 From Yukawa to mass: why $v/\sqrt{2}$ appears (note set 1)

In the Standard Model, fermion masses in the Higgs phase satisfy $m_f = y_f v/\sqrt{2}$. The ladder therefore naturally predicts the dimensionless Yukawas; multiplying by $v/\sqrt{2}$ maps the prediction to the mass scale. This point matters because it makes the ladder testable in any scheme where $y_f(\mu)$ is defined. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.4})$$

A.5 Effective rung coordinate as a diagnostic (note set 1)

The definition $n_{\text{eff}} = -(R/2\pi) \ln(m/(v/\sqrt{2}))$ converts a running mass into a coordinate in rung space. This is a diagnostic, not a new assumption: it is simply the inversion of the ladder formula. If the ladder is correct, then n_{eff} should sit near an integer in a scheme-consistent analysis. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.5})$$

A.6 Rung drift under renormalization (note set 1)

Because masses run, the rung coordinate runs. Differentiating n_{eff} yields $dn_{\text{eff}}/d\ln\mu = (R/2\pi)\gamma_m(\mu)$. This makes the validation program crisp: the RG anomalous dimension is a known function in the Standard Model, so the architecture must be compatible with it without introducing new knobs. In other words: rung drift is not a nuisance; it is a prediction channel. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio,

state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

$$n_{\text{eff}}(\mu) \equiv -\frac{R}{2\pi} \ln\left(\frac{m(\mu)}{v/\sqrt{2}}\right), \quad \Delta n = -\frac{R}{2\pi} \ln\left(\frac{m(\mu_1)}{m(\mu_0)}\right). \quad (\text{A.6})$$

A.7 Worked example: converting a mass ratio to rung drift (note set 1)

Suppose a running mass changes by a factor $q = m(\mu_1)/m(\mu_0)$. Then $\Delta n = -(R/2\pi) \ln q$. With $R = 28$, the prefactor is $R/2\pi \approx 4.458$. A modest factor-of-two change in mass corresponds to $\Delta n \approx 4.458 \ln 2 \approx 3.09$ rungs. This explains why scale control is mandatory before rung integers are compared. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.8 Why CKM is a stronger test than a single mass (note set 1)

A single mass can always be declared ‘close enough’ to some integer rung if you are allowed to shift scale, scheme, or rounding. The CKM closure instead ties multiple independent quantities together through a small locked constant set. Once R is fixed and the anchors $|V_{ub}|, |V_{cb}|$ are defined, the unitarity triangle and $\sin(2\beta)$ are forced. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.9 Why the PDG extraction matters (note set 1)

The Wolfenstein expansion is approximate. By converting the engine anchors into the exact PDG angles $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$, the program produces an exactly unitary CKM matrix with no hidden normalization drift. This is a structural integrity check: it prevents accidental inconsistencies from being confused with physics. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.10 Failure modes to watch for in future extensions (note set 1)

(i) Introducing per-particle correction factors. (ii) Re-defining rung assignments after seeing targets. (iii) Mixing pole masses and running masses in the same table. (iv) Using different R values in different sectors. The validation program is designed to forbid these by construction. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.11 Units and dimensionless structure (note set 2)

The Jacobian $J = d\tau/dt$ is dimensionless if τ and t are both time parameters. In the operational identification $J \equiv \Gamma_{\text{eff}}$, this means the effective rate is being measured in units where the geometric-time rate scale is set by the coordinate choice. This is not a problem so long as the architecture consistently uses $\int J dt$ as the invariant quantity. The invariant object is the accumulated processing increment $\Delta\tau = \int J dt$. All ladder predictions ultimately depend on exponentials of this invariant increment. Operationally, every time an ambiguity

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A.12 Why the exponential is the right algebraic form (note set 2)

The ladder uses $y \propto \exp(-\int J dt)$. This is the unique form that turns additive processing increments into multiplicative survival/overlap factors. Any alternative smooth monotone mapping either reduces to an exponential under reparameterization or introduces an extra scale that acts like a hidden knob. The exponential is therefore the minimal choice compatible with the locked-parameter ethos. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.13 Quantization of the integrated dissipation (note set 2)

The operational quantization rule $\int J dt \approx n(2\pi/R)$ is a strong assumption. Its meaning is that the accumulated intrinsic processing between relevant formation/selection events occurs in discrete geometric cycles. This is not a claim about microscopic periodic motion; it is a bookkeeping rule for coarse-grained epochs. The discrete integer n is what ultimately makes the ladder falsifiable. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.14 From Yukawa to mass: why $v/\sqrt{2}$ appears (note set 2)

In the Standard Model, fermion masses in the Higgs phase satisfy $m_f = y_f v/\sqrt{2}$. The ladder therefore naturally predicts the dimensionless Yukawas; multiplying by $v/\sqrt{2}$ maps the prediction to the mass scale. This point matters because it makes the ladder testable in any scheme where $y_f(\mu)$ is defined. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.15 Effective rung coordinate as a diagnostic (note set 2)

The definition $n_{\text{eff}} = -(R/2\pi) \ln(m/(v/\sqrt{2}))$ converts a running mass into a coordinate in rung space. This is a diagnostic, not a new assumption: it is simply the inversion of the ladder formula. If the ladder is correct, then n_{eff} should sit near an integer in a scheme-consistent analysis. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.16 Rung drift under renormalization (note set 2)

Because masses run, the rung coordinate runs. Differentiating n_{eff} yields $dn_{\text{eff}}/d\ln\mu = (R/2\pi)\gamma_m(\mu)$. This makes the validation program crisp: the RG anomalous dimension is a known function in the Standard Model, so the architecture must be compatible with it without introducing new knobs. In other words: rung drift is not a nuisance; it is a prediction channel. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.17 Worked example: converting a mass ratio to rung drift (note set 2)

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A.19 Why the PDG extraction matters (note set 2)

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A.20 Failure modes to watch for in future extensions (note set 2)

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A.21 Units and dimensionless structure (note set 3)

The Jacobian $J = d\tau/dt$ is dimensionless if τ and t are both time parameters. In the operational identification $J \equiv \Gamma_{\text{eff}}$, this means the effective rate is being measured in units where the geometric-time rate scale is set by the coordinate choice. This is not a problem so long as the architecture consistently uses $\int J dt$ as the invariant quantity. The invariant object is the accumulated processing increment $\Delta\tau = \int J dt$. All ladder predictions ultimately depend on exponentials of this invariant increment. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.22 Why the exponential is the right algebraic form (note set 3)

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A.23 Quantization of the integrated dissipation (note set 3)

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A.24 From Yukawa to mass: why $v/\sqrt{2}$ appears (note set 3)

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A.25 Effective rung coordinate as a diagnostic (note set 3)

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A.26 Rung drift under renormalization (note set 3)

Because masses run, the rung coordinate runs. Differentiating n_{eff} yields $dn_{\text{eff}}/d\ln\mu = (R/2\pi)\gamma_m(\mu)$. This makes the validation program crisp: the RG anomalous dimension is a known function in the Standard Model, so the architecture must be compatible with it without introducing new knobs. In other words: rung drift is not a nuisance; it is a prediction channel. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.27 Worked example: converting a mass ratio to rung drift (note set 3)

Suppose a running mass changes by a factor $q = m(\mu_1)/m(\mu_0)$. Then $\Delta n = -(R/2\pi)\ln q$. With $R = 28$, the prefactor is $R/2\pi \approx 4.458$. A modest factor-of-two change in mass corresponds to $\Delta n \approx 4.458 \ln 2 \approx 3.09$ rungs. This explains why scale control is mandatory before rung integers are compared. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.28 Why CKM is a stronger test than a single mass (note set 3)

A single mass can always be declared ‘close enough’ to some integer rung if you are allowed to shift scale, scheme, or rounding. The CKM closure instead ties multiple independent quantities together through a small locked constant set. Once R is fixed and the anchors $|V_{ub}|, |V_{cb}|$ are defined, the unitarity triangle and $\sin(2\beta)$ are forced. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.39 Why the PDG extraction matters (note set 4)

The Wolfenstein expansion is approximate. By converting the engine anchors into the exact PDG angles $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$, the program produces an exactly unitary CKM matrix with no hidden normalization drift. This is a structural integrity check: it prevents accidental inconsistencies from being confused with physics. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.40 Failure modes to watch for in future extensions (note set 4)

(i) Introducing per-particle correction factors. (ii) Re-defining rung assignments after seeing targets. (iii) Mixing pole masses and running masses in the same table. (iv) Using different R values in different sectors. The validation program is designed to forbid these by construction. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed

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A.41 Units and dimensionless structure (note set 5)

The Jacobian $J = d\tau/dt$ is dimensionless if τ and t are both time parameters. In the operational identification $J \equiv \Gamma_{\text{eff}}$, this means the effective rate is being measured in units where the geometric-time rate scale is set by the coordinate choice. This is not a problem so long as the architecture consistently uses $\int J dt$ as the invariant quantity. The invariant object is the accumulated processing increment $\Delta\tau = \int J dt$. All ladder predictions ultimately depend on exponentials of this invariant increment. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.42 Why the exponential is the right algebraic form (note set 5)

The ladder uses $y \propto \exp(-\int J dt)$. This is the unique form that turns additive processing increments into multiplicative survival/overlap factors. Any alternative smooth monotone mapping either reduces to an exponential under reparameterization or introduces an extra scale that acts like a hidden knob. The exponential is therefore the minimal choice compatible with the locked-parameter ethos. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.43 Quantization of the integrated dissipation (note set 5)

The operational quantization rule $\int J dt \approx n(2\pi/R)$ is a strong assumption. Its meaning is that the accumulated intrinsic processing between relevant formation/selection events occurs in discrete geometric cycles. This is not a claim about microscopic periodic motion; it is a bookkeeping rule for coarse-grained epochs. The discrete integer n is what ultimately makes the ladder falsifiable. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.44 From Yukawa to mass: why $v/\sqrt{2}$ appears (note set 5)

In the Standard Model, fermion masses in the Higgs phase satisfy $m_f = y_f v/\sqrt{2}$. The ladder therefore naturally predicts the dimensionless Yukawas; multiplying by $v/\sqrt{2}$ maps the prediction to the mass scale. This point matters because it makes the ladder testable in any scheme where $y_f(\mu)$ is defined. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.45 Effective rung coordinate as a diagnostic (note set 5)

The definition $n_{\text{eff}} = -(R/2\pi) \ln(m/(v/\sqrt{2}))$ converts a running mass into a coordinate in rung space. This is a diagnostic, not a new assumption: it is simply the inversion of the

ladder formula. If the ladder is correct, then n_{eff} should sit near an integer in a scheme-consistent analysis. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.46 Rung drift under renormalization (note set 5)

Because masses run, the rung coordinate runs. Differentiating n_{eff} yields $dn_{\text{eff}}/d\ln\mu = (R/2\pi)\gamma_m(\mu)$. This makes the validation program crisp: the RG anomalous dimension is a known function in the Standard Model, so the architecture must be compatible with it without introducing new knobs. In other words: rung drift is not a nuisance; it is a prediction channel. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.47 Worked example: converting a mass ratio to rung drift (note set 5)

Suppose a running mass changes by a factor $q = m(\mu_1)/m(\mu_0)$. Then $\Delta n = -(R/2\pi) \ln q$. With $R = 28$, the prefactor is $R/2\pi \approx 4.458$. A modest factor-of-two change in mass corresponds to $\Delta n \approx 4.458 \ln 2 \approx 3.09$ rungs. This explains why scale control is mandatory before rung integers are compared. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.48 Why CKM is a stronger test than a single mass (note set 5)

A single mass can always be declared ‘close enough’ to some integer rung if you are allowed to shift scale, scheme, or rounding. The CKM closure instead ties multiple independent quantities together through a small locked constant set. Once R is fixed and the anchors $|V_{ub}|, |V_{cb}|$ are defined, the unitarity triangle and $\sin(2\beta)$ are forced. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.49 Why the PDG extraction matters (note set 5)

The Wolfenstein expansion is approximate. By converting the engine anchors into the exact PDG angles $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$, the program produces an exactly unitary CKM matrix with no hidden normalization drift. This is a structural integrity check: it prevents accidental inconsistencies from being confused with physics. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.50 Failure modes to watch for in future extensions (note set 5)

(i) Introducing per-particle correction factors. (ii) Re-defining rung assignments after seeing targets. (iii) Mixing pole masses and running masses in the same table. (iv) Using different R values in different sectors. The validation program is designed to forbid these by construction. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed

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A.51 Units and dimensionless structure (note set 6)

The Jacobian $J = d\tau/dt$ is dimensionless if τ and t are both time parameters. In the operational identification $J \equiv \Gamma_{\text{eff}}$, this means the effective rate is being measured in units where the geometric-time rate scale is set by the coordinate choice. This is not a problem so long as the architecture consistently uses $\int J dt$ as the invariant quantity. The invariant object is the accumulated processing increment $\Delta\tau = \int J dt$. All ladder predictions ultimately depend on exponentials of this invariant increment. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.52 Why the exponential is the right algebraic form (note set 6)

The ladder uses $y \propto \exp(-\int J dt)$. This is the unique form that turns additive processing increments into multiplicative survival/overlap factors. Any alternative smooth monotone mapping either reduces to an exponential under reparameterization or introduces an extra scale that acts like a hidden knob. The exponential is therefore the minimal choice compatible with the locked-parameter ethos. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.53 Quantization of the integrated dissipation (note set 6)

The operational quantization rule $\int J dt \approx n(2\pi/R)$ is a strong assumption. Its meaning is that the accumulated intrinsic processing between relevant formation/selection events occurs in discrete geometric cycles. This is not a claim about microscopic periodic motion; it is a bookkeeping rule for coarse-grained epochs. The discrete integer n is what ultimately makes the ladder falsifiable. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.54 From Yukawa to mass: why $v/\sqrt{2}$ appears (note set 6)

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A.55 Effective rung coordinate as a diagnostic (note set 6)

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A.56 Rung drift under renormalization (note set 6)

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A.57 Worked example: converting a mass ratio to rung drift (note set 6)

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A.58 Why CKM is a stronger test than a single mass (note set 6)

A single mass can always be declared ‘close enough’ to some integer rung if you are allowed to shift scale, scheme, or rounding. The CKM closure instead ties multiple independent quantities together through a small locked constant set. Once R is fixed and the anchors $|V_{ub}|, |V_{cb}|$ are defined, the unitarity triangle and $\sin(2\beta)$ are forced. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.59 Why the PDG extraction matters (note set 6)

The Wolfenstein expansion is approximate. By converting the engine anchors into the exact PDG angles $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$, the program produces an exactly unitary CKM matrix with no hidden normalization drift. This is a structural integrity check: it prevents accidental inconsistencies from being confused with physics. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed to remain implicit if it can affect a printed number. This is not stylistic; it is required for auditability.

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A.60 Failure modes to watch for in future extensions (note set 6)

(i) Introducing per-particle correction factors. (ii) Re-defining rung assignments after seeing targets. (iii) Mixing pole masses and running masses in the same table. (iv) Using different R values in different sectors. The validation program is designed to forbid these by construction. Operationally, every time an ambiguity appears, the rule is: reduce it to a dimensionless ratio, state the chosen convention explicitly, and record it in the scorecard. Nothing is allowed

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B Technical Notes and Worked Examples (for audit and onboarding)

This chapter is deliberately verbose. It exists to make the architecture legible to a new reader without requiring prior familiarity with the project history. Nothing here introduces new metaphysical principles; it is algebra, bookkeeping, and explicit worked manipulation of the already-locked objects $\tau, t, J(t), R, s$, and the rung map.

B.1 Dimensional bookkeeping

The Jacobian $J(t) = d\tau/dt$ is dimensionless if τ and t are measured in the same units; operationally we treat J as a rate *in the exponent* and therefore as a dimensionless integrand after choosing consistent units. The step size $s = 2\pi/R$ is dimensionless. The rung n is an integer by definition.

B.2 Worked note 1: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.1})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.2})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.3})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.4})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.5})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.3 Worked note 2: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.6})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.7})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.8})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.9})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.10})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.4 Worked note 3: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.11})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.12})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.13})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.14})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.15})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.5 Worked note 4: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.16})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.17})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.18})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.19})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.20})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.6 Worked note 5: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.21})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.22})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.23})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.24})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.25})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.7 Worked note 6: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.26})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.27})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.28})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.29})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.30})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.8 Worked note 7: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.31})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.32})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.33})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.34})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.35})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.9 Worked note 8: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.36})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.37})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.38})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.39})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.40})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.10 Worked note 9: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.41})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.42})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.43})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.44})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.45})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.11 Worked note 10: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.46})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.47})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.48})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.49})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.50})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.12 Worked note 11: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.51})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.52})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.53})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.54})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.55})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.13 Worked note 12: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.56})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.57})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.58})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.59})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.60})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.14 Worked note 13: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.61})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.62})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.63})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.64})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.65})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.15 Worked note 14: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.66})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.67})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.68})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.69})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.70})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.16 Worked note 15: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.71})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.72})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.73})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.74})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.75})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.17 Worked note 16: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.76})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.77})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.78})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.79})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.80})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.18 Worked note 17: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.81})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.82})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.83})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.84})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.85})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.19 Worked note 18: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.86})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.87})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.88})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.89})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.90})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.20 Worked note 19: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.91})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.92})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.93})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.94})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.95})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.21 Worked note 20: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.96})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.97})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.98})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.99})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.100})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.22 Worked note 21: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.101})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.102})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.103})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.104})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.105})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.23 Worked note 22: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.106})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.107})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.108})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.109})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.110})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.24 Worked note 23: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.111})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.112})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.113})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.114})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.115})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.25 Worked note 24: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.116})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.117})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.118})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.119})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.120})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.26 Worked note 25: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.121})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.122})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.123})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.124})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.125})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.27 Worked note 26: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.126})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.127})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.128})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.129})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.130})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.28 Worked note 27: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.131})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.132})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.133})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.134})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.135})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.29 Worked note 28: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.136})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.137})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.138})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.139})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.140})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.30 Worked note 29: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.141})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.142})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.143})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.144})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.145})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.31 Worked note 30: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.146})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.147})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.148})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.149})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.150})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.32 Worked note 31: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.151})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.152})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.153})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.154})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.155})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.33 Worked note 32: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.156})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.157})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.158})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.159})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.160})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.34 Worked note 33: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.161})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.162})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.163})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.164})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.165})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.35 Worked note 34: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.166})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.167})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.168})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.169})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.170})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.36 Worked note 35: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.171})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.172})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.173})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.174})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.175})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.37 Worked note 36: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.176})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.177})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.178})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.179})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.180})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.38 Worked note 37: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.181})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.182})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.183})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2})y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.184})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.185})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.39 Worked note 38: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.186})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.187})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.188})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.189})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.190})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.40 Worked note 39: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.191})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.192})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.193})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.194})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.195})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the observed alignment at one scale is not a robust structural feature.

B.41 Worked note 40: A concrete algebraic check

Goal. Demonstrate a concrete manipulation that appears repeatedly in the project.

Setup. Start from the survival-factor ansatz

$$y \propto \exp\left(-\int J(t) dt\right). \quad (\text{B.196})$$

If the integral is quantized as $\int J dt \approx ns$, then

$$y_n \approx e^{-ns}. \quad (\text{B.197})$$

Check. Taking logs removes the exponential and isolates the additive structure:

$$-\ln y_n \approx ns. \quad (\text{B.198})$$

This is the structural reason the program cares about rungs: it converts a multiplicative hierarchy into an additive integer coordinate.

Connection to masses. Using $m = (v/\sqrt{2}) y$ yields

$$-\ln\left(\frac{m}{v/\sqrt{2}}\right) \approx ns. \quad (\text{B.199})$$

Dividing by s gives the diagnostic coordinate

$$n_{\text{eff}} = -\frac{1}{s} \ln\left(\frac{m}{v/\sqrt{2}}\right), \quad (\text{B.200})$$

which is the object compared against the frozen integer set.

Failure mode. If n_{eff} is not stable under consistent running to a common scale μ , then the

observed alignment at one scale is not a robust structural feature.

B.42 Reproducibility protocol (no hidden steps)

To reproduce every printed CKM number:

- (1) Set $R = 28$ and compute $s = 2\pi/R = \pi/14$.
- (2) Set $\lambda = s$, $\alpha = 1 - 1/(2\pi)$, and $\bar{\rho} = 1/(2\pi)$.
- (3) Compute $|V_{cb}| = \exp[-\alpha \cdot 17s]$ and $|V_{ub}| = \exp[-25s]$.
- (4) Compute $A = |V_{cb}|/\lambda^2$ and $r = |V_{ub}|/(A\lambda^3)$.
- (5) Compute $\bar{\eta} = \sqrt{r^2 - \bar{\rho}^2}$.
- (6) Compute $\beta = \arctan(\bar{\eta}/(1 - \bar{\rho}))$ and report $\sin(2\beta)$.
- (7) Compute $s_{12} = \lambda$, $s_{13} = |V_{ub}|$, $c_{13} = \sqrt{1 - s_{13}^2}$, and $s_{23} = |V_{cb}|/c_{13}$.
- (8) Compute $J_{\text{model}} = A^2\lambda^6\bar{\eta}$ and solve for δ using

$$J_{\text{model}} = c_{12}c_{23}c_{13}^2s_{12}s_{23}s_{13}\sin\delta.$$

- (9) Insert $(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$ into the PDG CKM matrix.

This protocol is intentionally redundant; it exists to ensure there is no ambiguity about what is assumed, what is defined, and what is computed.

Appendix A: Symbol table

Symbol	Meaning
τ	intrinsic/processing time
t	geometric/observed time
$J(t)$	Jacobian $d\tau/dt$, also $\Gamma_{\text{eff}}(t)$
$\Gamma_{\text{eff}}(t)$	effective dissipation/processing rate
R	geometric constant setting $s = 2\pi/R$
s	step size $2\pi/R$
n	integer Sphaleron Universality Class Step index
y	Yukawa coupling (treated as survival factor)
v	Higgs vev
V_{CKM}	CKM matrix
λ	Wolfenstein parameter (locked to s)
α	defect factor $1 - 1/(2\pi)$
$A, \bar{\rho}, \bar{\eta}$	Wolfenstein parameters
β	unitarity-triangle angle
δ	PDG CP phase
γ_m	mass anomalous dimension

Appendix B: Frozen rung set

$$n_t = 0, \quad n_b = 17, \quad n_c = 22, \quad n_s = 34, \quad n_d = 47, \quad n_u = 50, \quad (\text{B.201})$$

$$n_\tau = 20, \quad n_\mu = 33, \quad n_e = 57. \quad (\text{B.202})$$