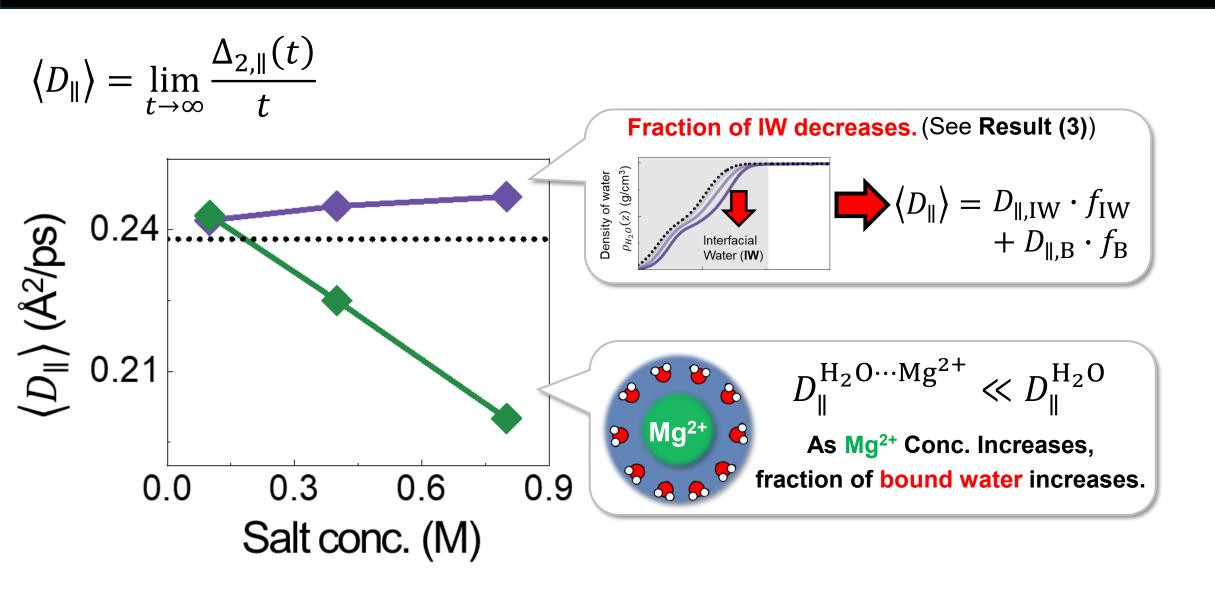
SI Result 1. Mean Diffusion Coefficient

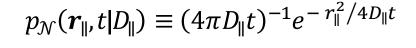


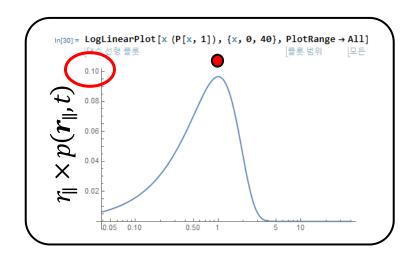
SI Result 2. Lateral Displacement Distribution

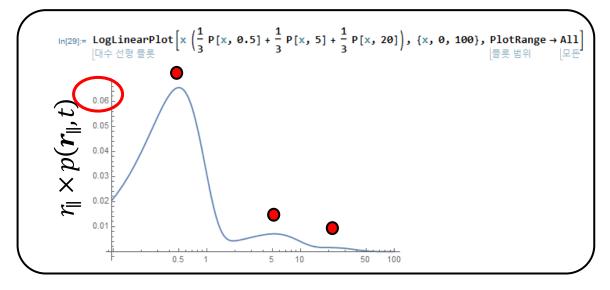
$$p(\mathbf{r}_{\parallel},t) \cong \sum_{n} f_{n} p_{\mathcal{N}} \left(\mathbf{r}_{\parallel},t|D_{\parallel}^{(n)}\right) \qquad \sum_{n} f_{n} = 1$$

$$r_{\parallel} \times p_{\mathcal{N}}(\boldsymbol{r}_{\parallel}, t|D_{\parallel}) \rightarrow \text{maximum at } r_{\parallel} = \sigma = \sqrt{2D_{\parallel}t}$$

$$In[2] = P[x_{_}, \sigma_{_}] := (2 \pi \sigma^2)^{-1} \exp[-x^2/(2 \sigma^2)]$$



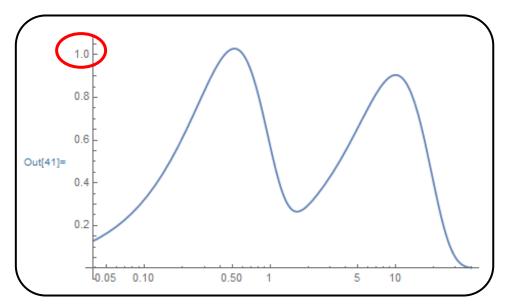




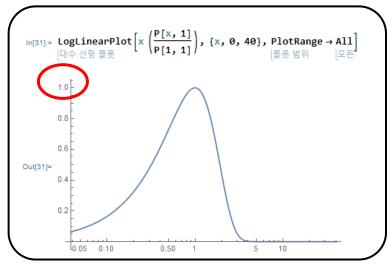
SI Result 2. Lateral Displacement Distribution

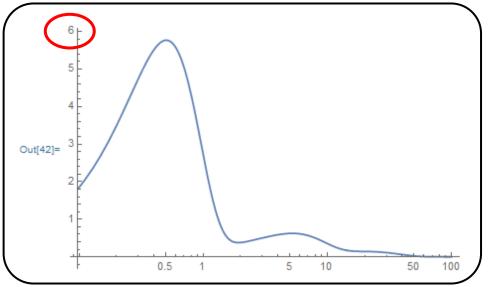
$$p(\mathbf{r}_{\parallel},t) \cong \sum_{n} f_{n} p_{\mathcal{N}} \left(\mathbf{r}_{\parallel},t|D_{\parallel}^{(n)}\right) \qquad \sum_{n} f_{n} = 1$$

$$f(\mathbf{r}_{\parallel},t) \equiv \frac{r_{\parallel}p(\mathbf{r}_{\parallel},t)}{\sigma p_{\mathcal{N}}(\sigma,t|\sigma)}\Big|_{\sigma=\sqrt{2\langle D_{\parallel}\rangle t}}$$

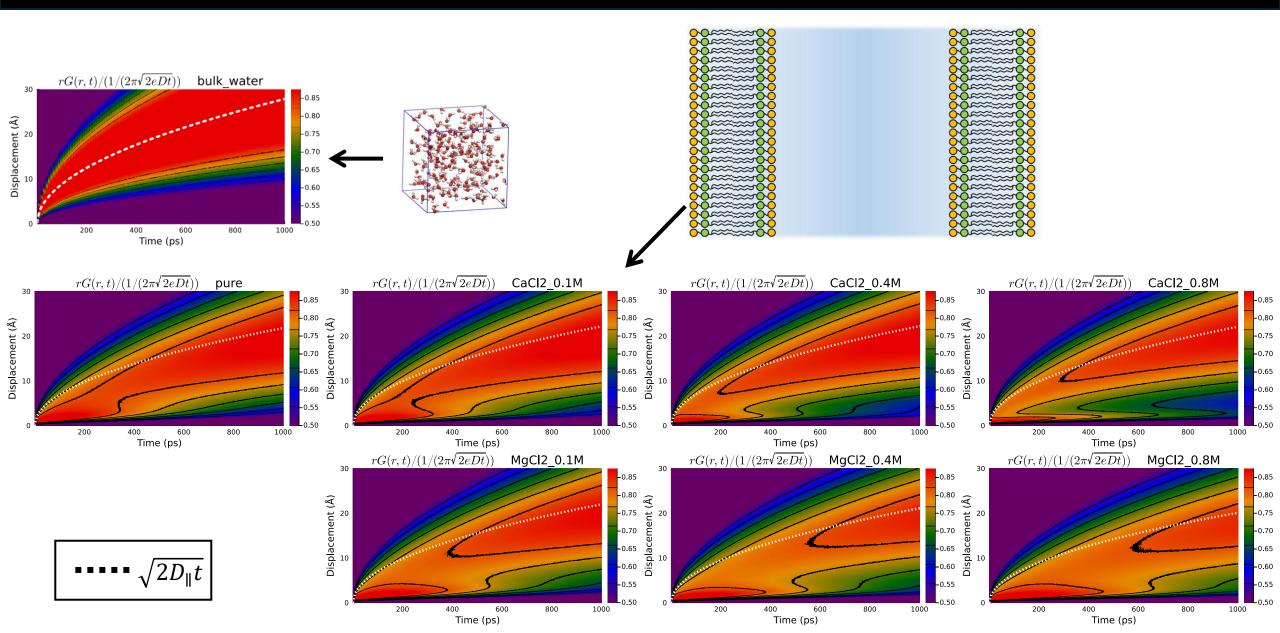


$$p_{\mathcal{N}}(\mathbf{r}_{\parallel}, t|D_{\parallel}) \equiv (4\pi D_{\parallel}t)^{-1}e^{-r_{\parallel}^2/4D_{\parallel}t}$$





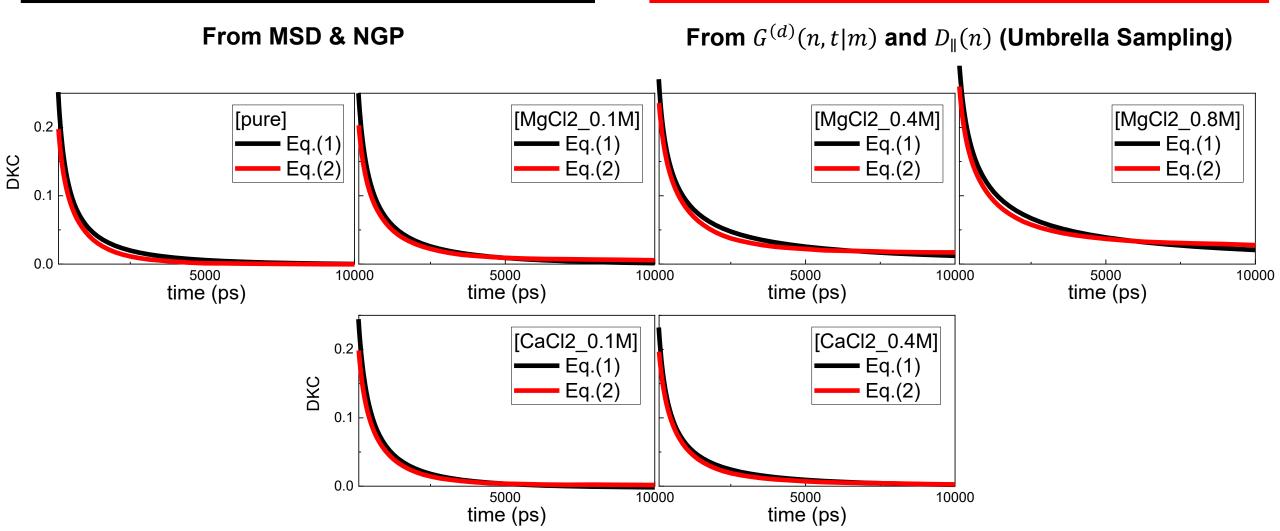
SI Result 2. Lateral Displacement Distribution



SI Result 4. Diffusion Kernel Correlation

$$C_{\mathcal{D}_{\parallel}}(t) = \int d\mathbf{\Gamma} \int d\mathbf{\Gamma}_{0} \frac{\delta \widehat{\mathcal{D}}_{\parallel}(\mathbf{\Gamma}, s)}{\left\langle \widehat{\mathcal{D}}_{\parallel}(s) \right\rangle} \, \widehat{G}(\Gamma, s | \Gamma_{0}) \frac{\delta \widehat{\mathcal{D}}_{\parallel}(\mathbf{\Gamma}_{0}, s)}{\left\langle \widehat{\mathcal{D}}_{\parallel}(s) \right\rangle} P_{st}(\mathbf{\Gamma}_{0}) \, (1)$$

$$C_{\mathcal{D}_{\parallel}}(t) \cong \eta_{D_{\parallel}}^{2} \phi_{D_{\parallel}}(t) = \sum_{n} \sum_{m} \frac{\delta D_{\parallel}(n)}{\langle D_{\parallel} \rangle} G^{(d)}(n, t | m) \frac{\delta D_{\parallel}(m)}{\langle D_{\parallel} \rangle} P_{st}(m) \tag{2}$$



SI Result 5. Experimental result

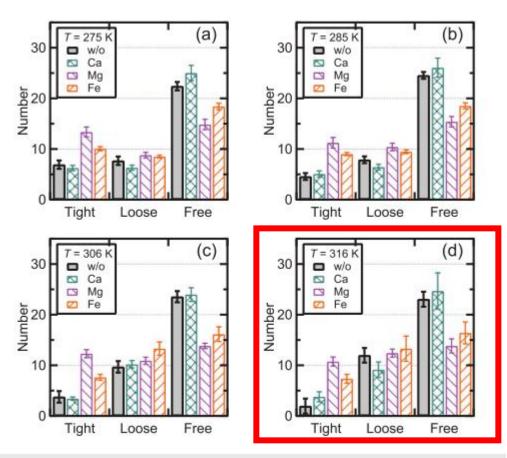
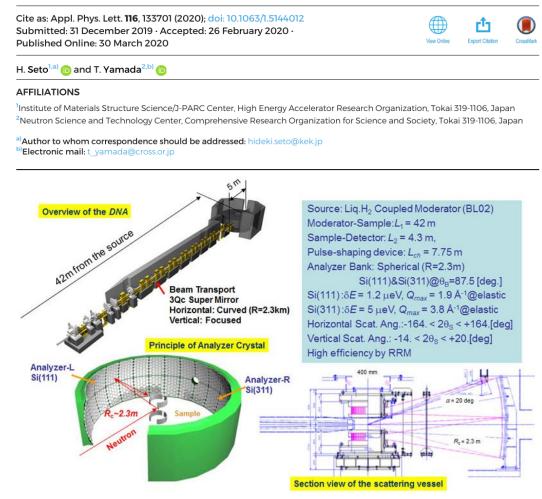


FIG. 3. Temperature dependence of the numbers of free water molecules, loosely bound water molecules, and tightly bound water molecules for $d67DMPC-37H_2O$ (gray), $d67DMPC-37H_2O-0.25CaCl_2$ (green), $d67DMPC-37H_2O-0.25MgCl_2$ (purple), and $d67DMPC-37H_2O-0.25FeCl_2$ (orange).

Quasi-elastic neutron scattering study of the effects of metal cations on the hydration water between phospholipid bilayers



J-PARC MLF BL02 DNA: Dynamic Spectrometer

SI Result 6. PDF of cation, anion

