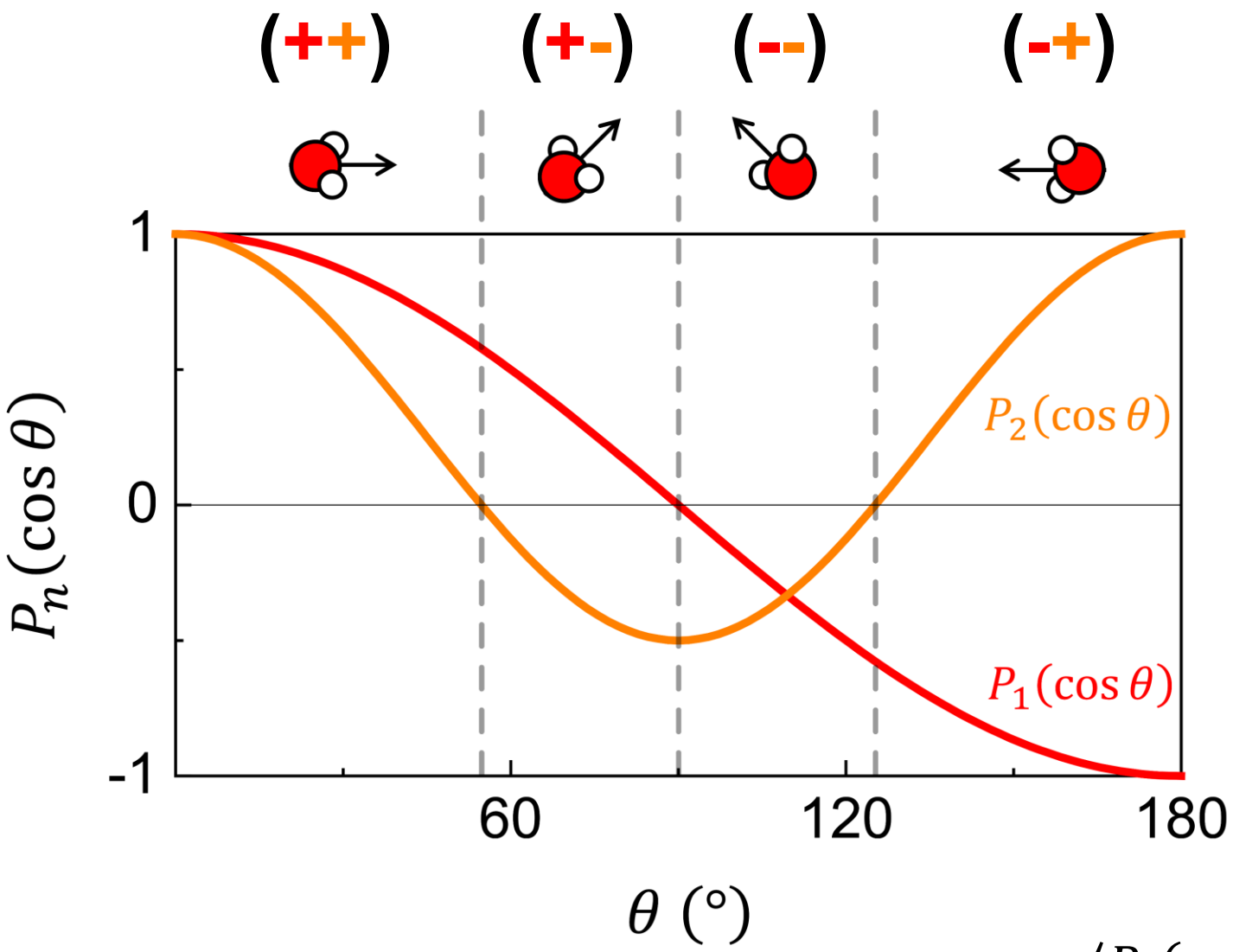
SI Result 1 (a): Legendre Polynomial



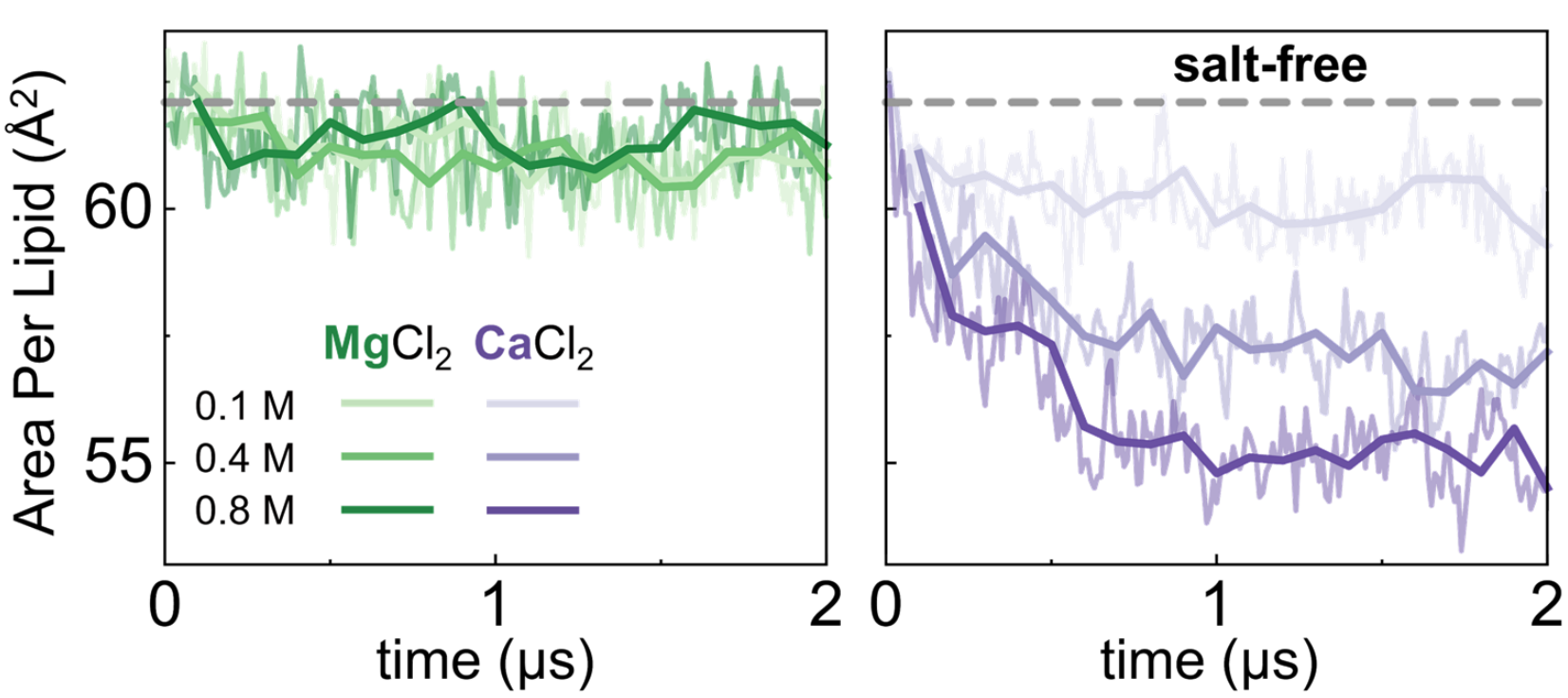
See **Fig. 2 (d)** and **Fig. 2 (e)**

$$P_1(\cos\theta) = \cos\theta$$

$$P_2(\cos\theta) = (3\cos^2\theta - 1)/2$$

$$\langle P_n(\cos\theta)\rangle(z) = \int_0^{\pi} d\theta \sin\theta\, P_n(\cos\theta) p(\theta, z)$$

SI Result 1 (b): Area per lipid

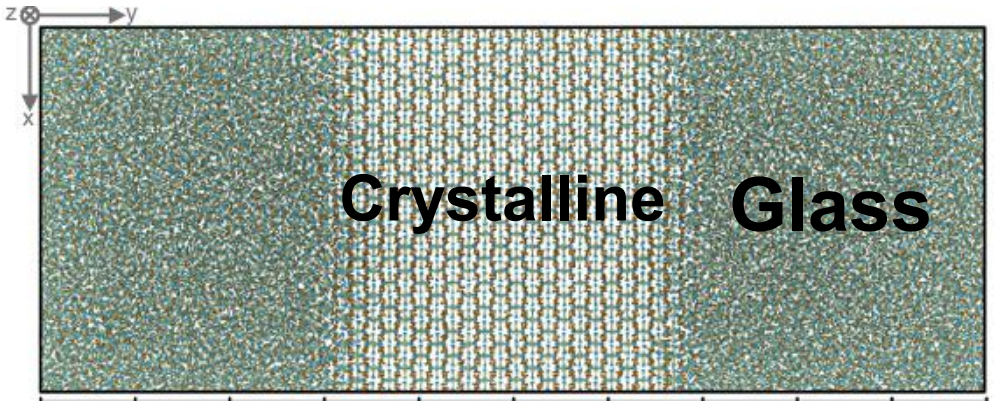


- **Mg^{2+}** cannot induce membrane condensation due to its **hydration shell** **[7]**.
- **Ca^{2+}** reduces repulsion between headgroups, inducing **membrane condensation** **[7]**.
- As Conc. of **$CaCl_2$** increases, portion of interfacial water (**IW**) of **$CaCl_2$** decreases.

(See $\rho_{H_2O}(z)$ in **Fig. 2 (f)**)

SI Result 1 (c): Lateral Displacement Distribution

Li_3PS_4



nature communications

Article

https://doi.org/10.1038/s41467-025-56322-x

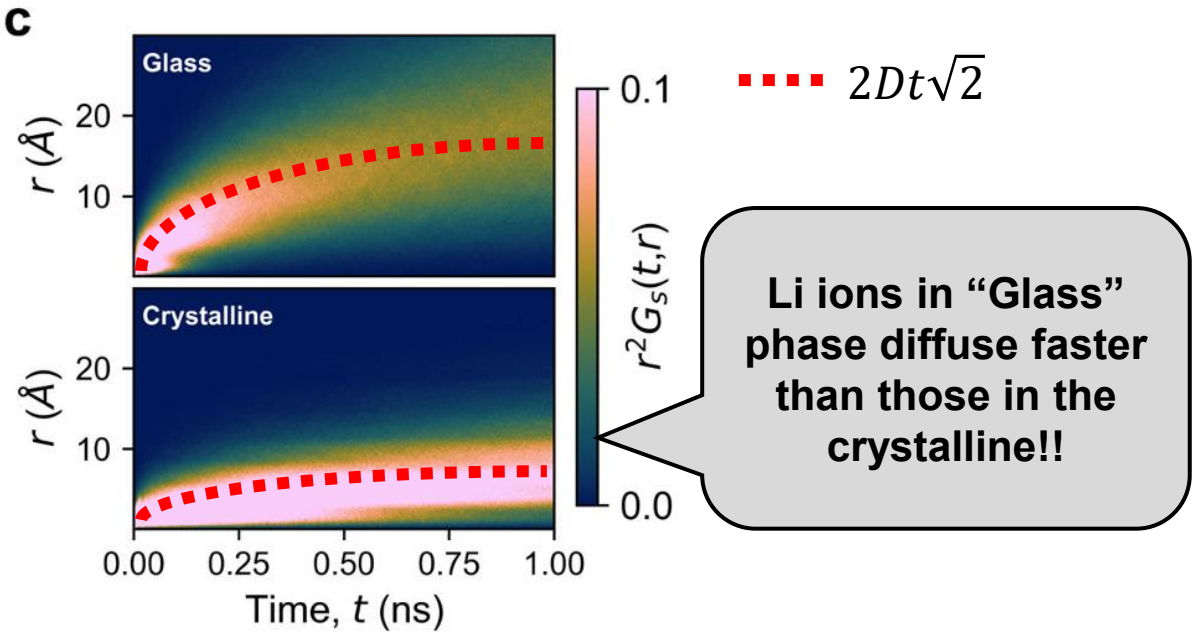
Disorder-induced enhancement of lithium-ion transport in solid-state electrolytes

Received: 11 January 2024

Accepted: 14 January 2025

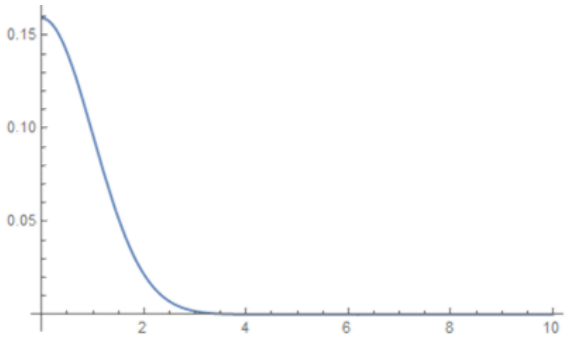
Published online: 26 January 2025

Zhimin Chen[1], Tao Du[1,2] ✉, N. M. Anoop Krishnan[3], Yuanzheng Yue[1] & Morten M. Smedskjaer[1] ✉



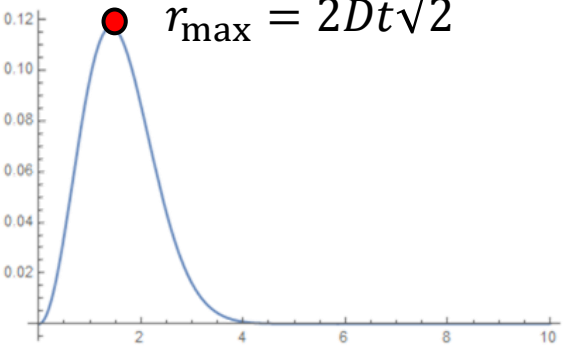
Li ions in "Glass" phase diffuse faster than those in the crystalline!!

$$G_s(\boldsymbol{r},t) = (4\pi Dt)^{-3/2} e^{-r^2/4Dt}$$



$$r^2 G_s(\boldsymbol{r},t)$$

$$r_{\max} = 2Dt\sqrt{2}$$



SI Result 1 (c): Lateral Displacement Distribution

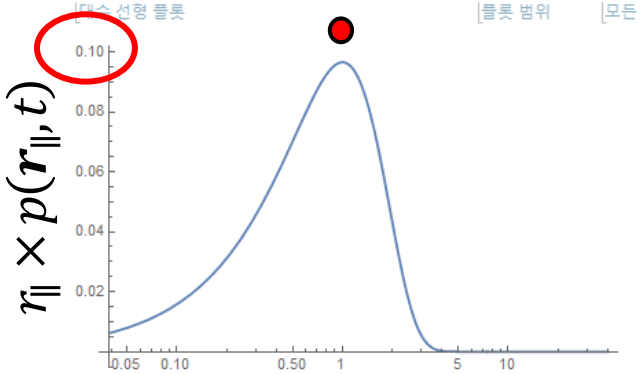
$$G_s(\boldsymbol{r}_\parallel, t) \cong \sum_n f_n G_{\mathcal{N}}\left(\boldsymbol{r}_\parallel, t | D_\parallel^{(n)}\right) \qquad \sum_n f_n = 1$$

$$G_{\mathcal{N}}(\boldsymbol{r}_\parallel, t | D_\parallel) \equiv (4\pi D_\parallel t)^{-1} e^{-r_\parallel^2 / 4 D_\parallel t}$$

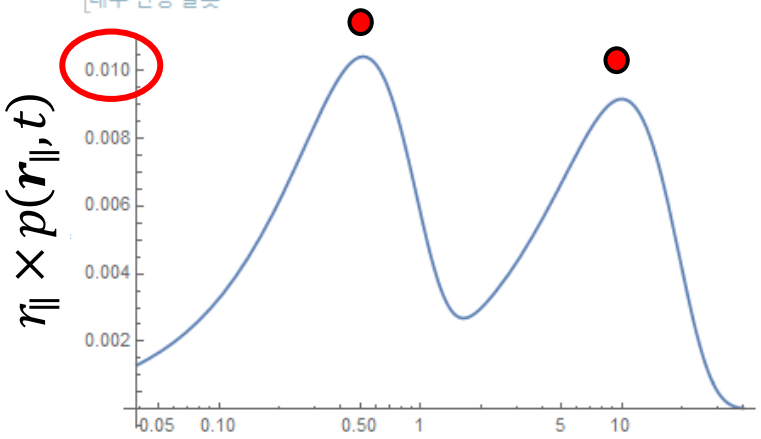
$$r_\parallel \times G_{\mathcal{N}}(\boldsymbol{r}_\parallel, t | D_\parallel) \rightarrow \text{ maximum at } r_\parallel = \sigma = \sqrt{2 D_\parallel t}$$

```
In[2]:= P[x_, σ_] := (2 π σ²)^-1 Exp[-x² / (2 σ²)]
                                  지수 함수
```

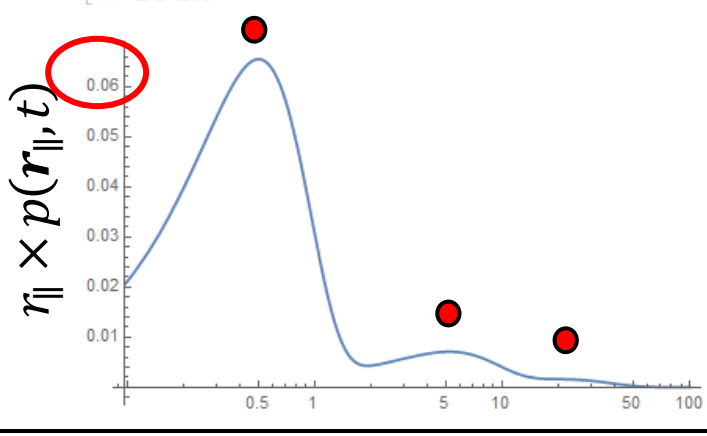
```
In[30]:= LogLinearPlot[x (P[x, 1]), {x, 0, 40}, PlotRange → All]
          대수 선형 플롯                          플롯 범위   모든
```




```
In[26]:= LogLinearPlot[x (0.05 P[x, 0.5] + 0.95 P[x, 10]), {x, 0, 40}, PlotRange → All]
          대수 선형 플롯                                                  플롯 범위   모든
```




```
In[29]:= LogLinearPlot[x (1/3 P[x, 0.5] + 1/3 P[x, 5] + 1/3 P[x, 20]), {x, 0, 100}, PlotRange → All]
          대수 선형 플롯                                                  플롯 범위   모든
```

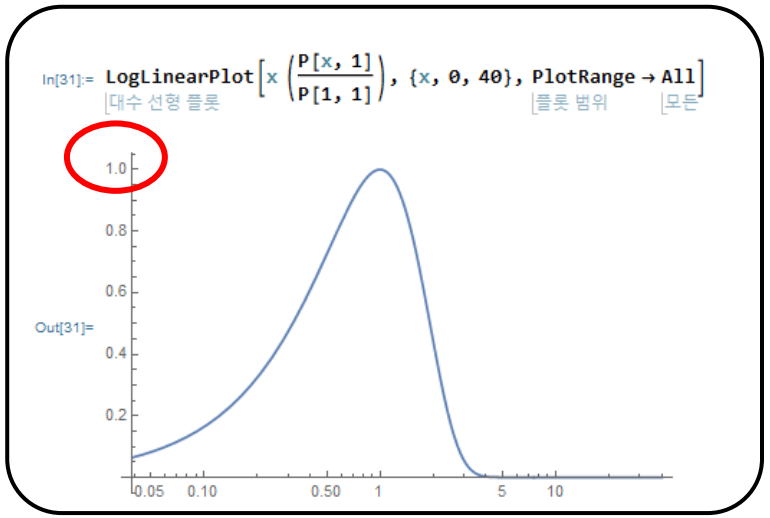


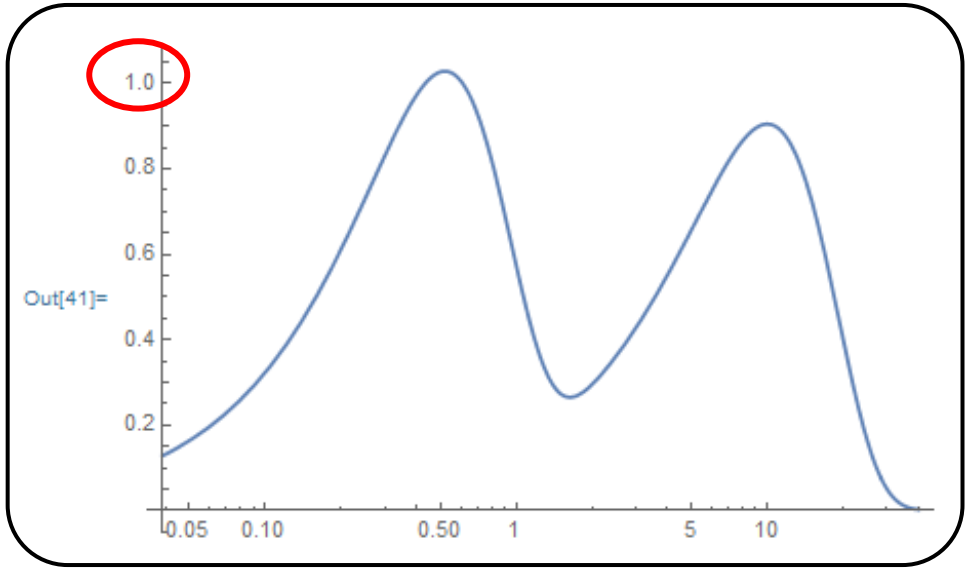
SI Result 1 (c): Lateral Displacement Distribution

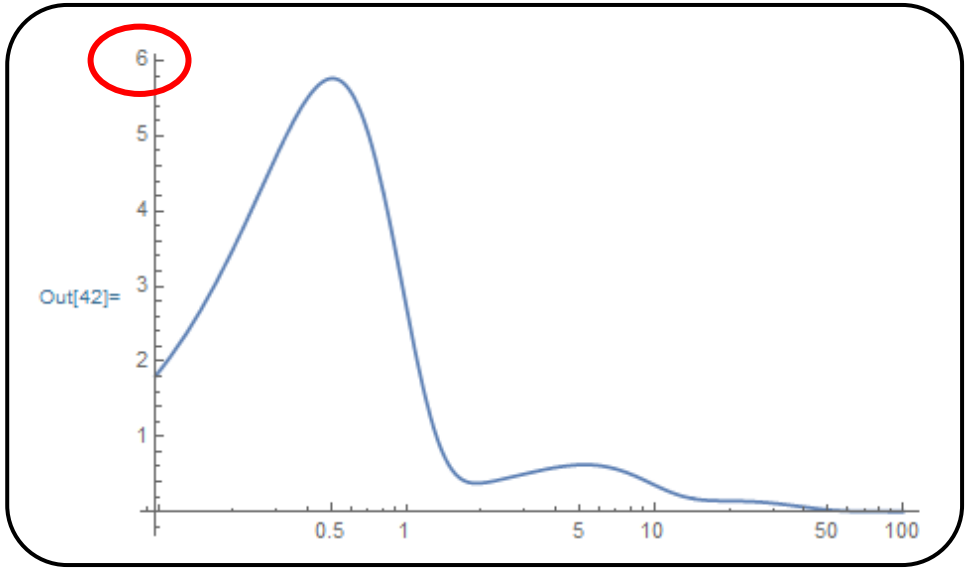
$$G_s(\boldsymbol{r}_\parallel, t) \cong \sum_n f_n G_{\mathcal{N}}\left(\boldsymbol{r}_\parallel, t | D_\parallel^{(n)}\right) \qquad \sum_n f_n = 1$$

$$G_{\mathcal{N}}(\boldsymbol{r}_\parallel, t | D_\parallel) \equiv (4\pi D_\parallel t)^{-1} e^{-r_\parallel^2 / 4 D_\parallel t}$$

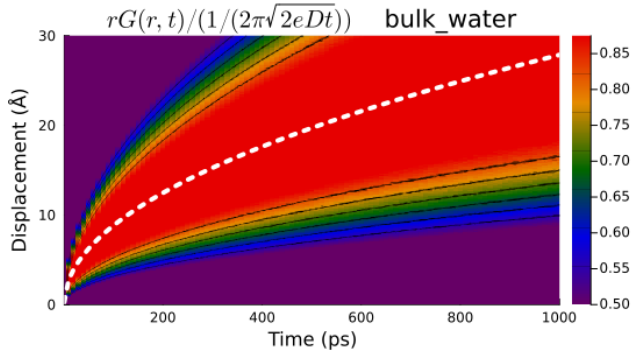
$$f(\boldsymbol{r}_\parallel, t) \equiv \left. \frac{r_\parallel G_s(\boldsymbol{r}_\parallel, t)}{\sigma\, p_{\mathcal{N}}(\sigma, t|\sigma)} \right|_{\sigma = \sqrt{2\langle D_\parallel \rangle t}}$$

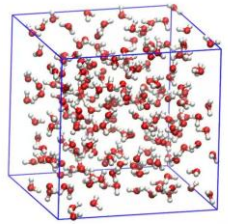


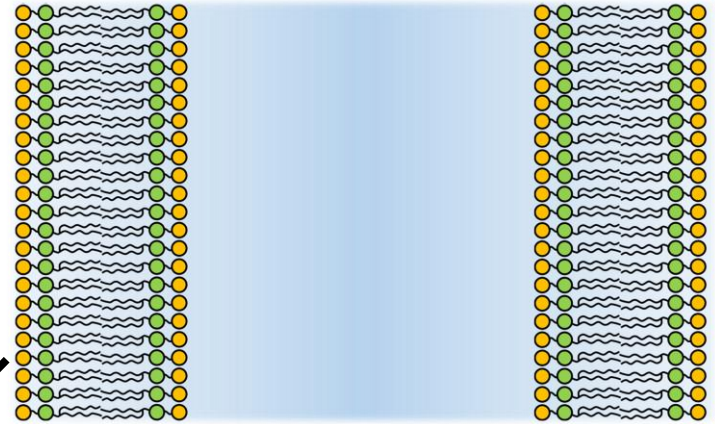


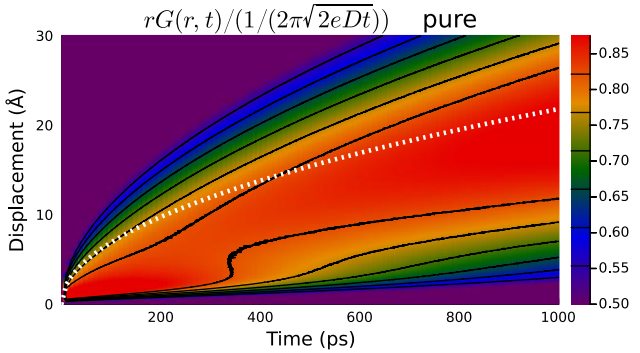


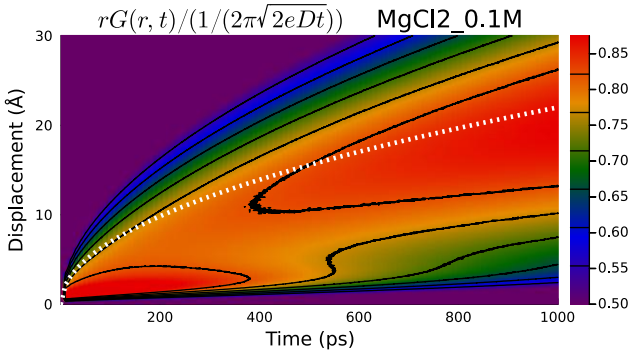
SI Result 1 (c): Lateral Displacement Distribution

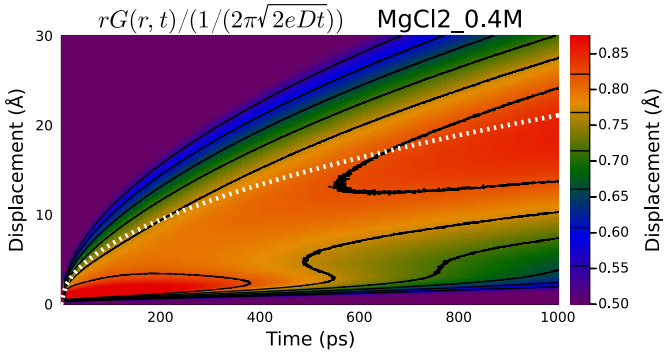


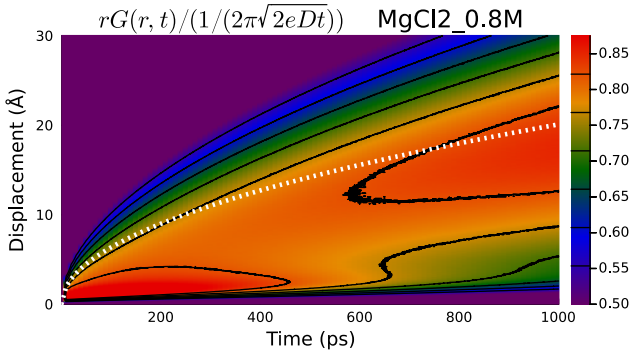


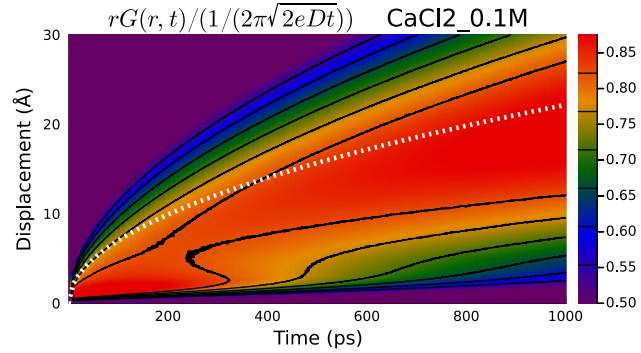


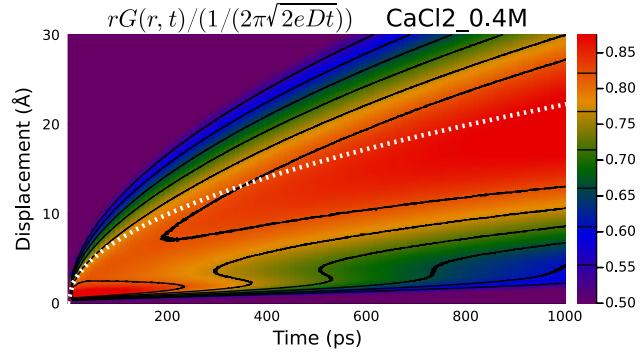


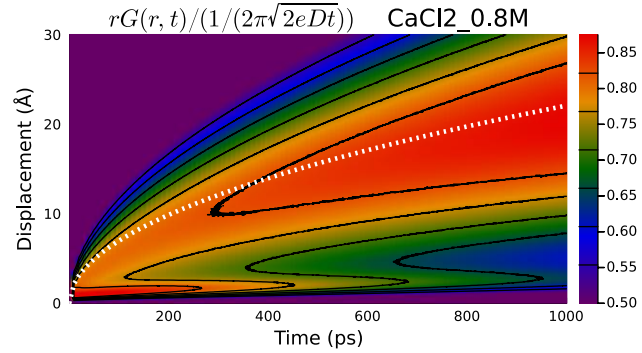


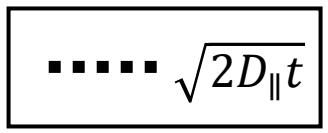




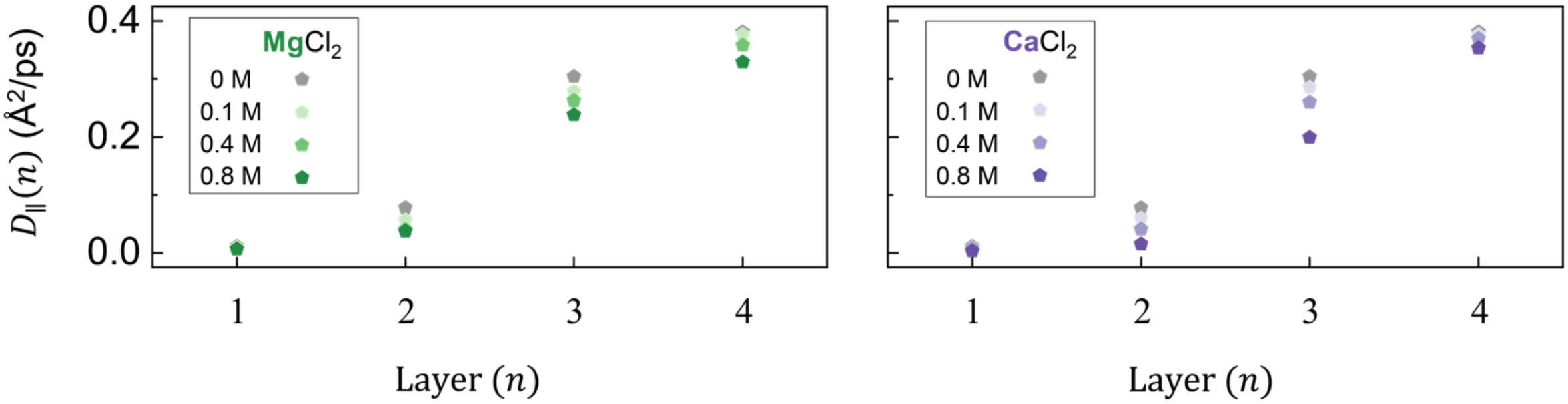








SI Result 1 (d): Region dependent lateral diffusion coefficient

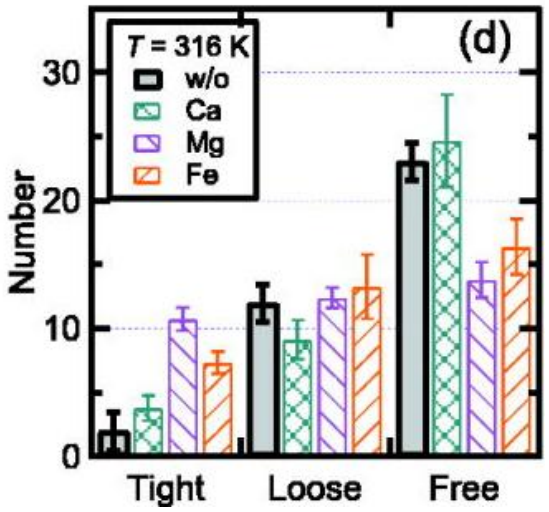


$D_{\parallel}(n)$: determined by umbrella sampling (1 μs-long)

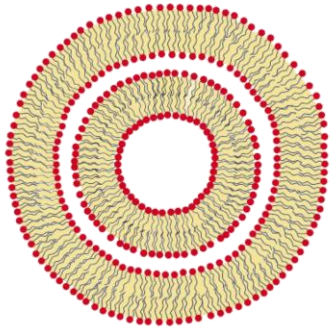
$\mathrm{Layer}(n)$: defined by the nodes of $\langle P_2(\cos\theta)\rangle(z)$ in the salt-free case. (see **Fig. 2 (e)**)

SI Result 1 (e): Experimental result

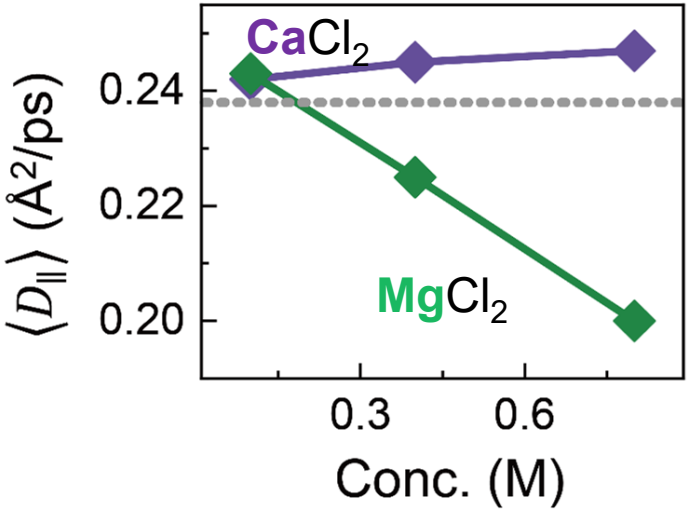
Fig. 3

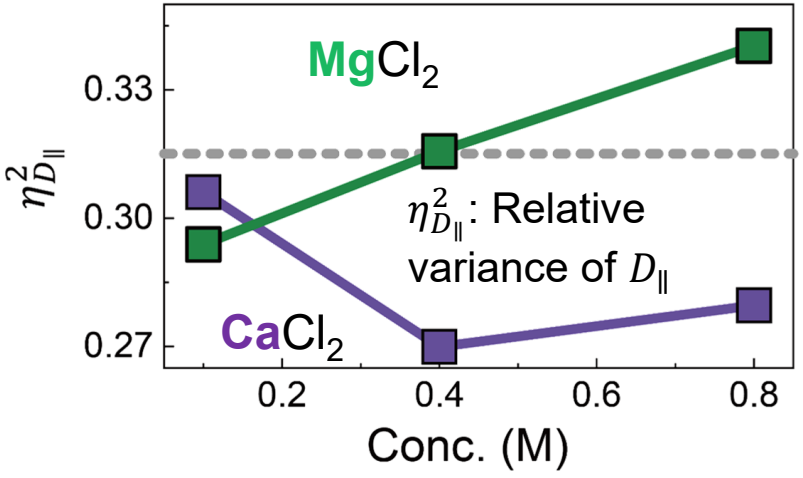


[Experiment]
DMPC
37 H_2O/lipid molecule.
0.45 M conc.



Multilamellar lipid vesicle





Quasi-elastic neutron scattering study of the effects of metal cations on the hydration water between phospholipid bilayers

Cite as: Appl. Phys. Lett. **116**, 133701 (2020); doi: 10.1063/1.5144012
Submitted: 31 December 2019 · Accepted: 26 February 2020 ·
Published Online: 30 March 2020

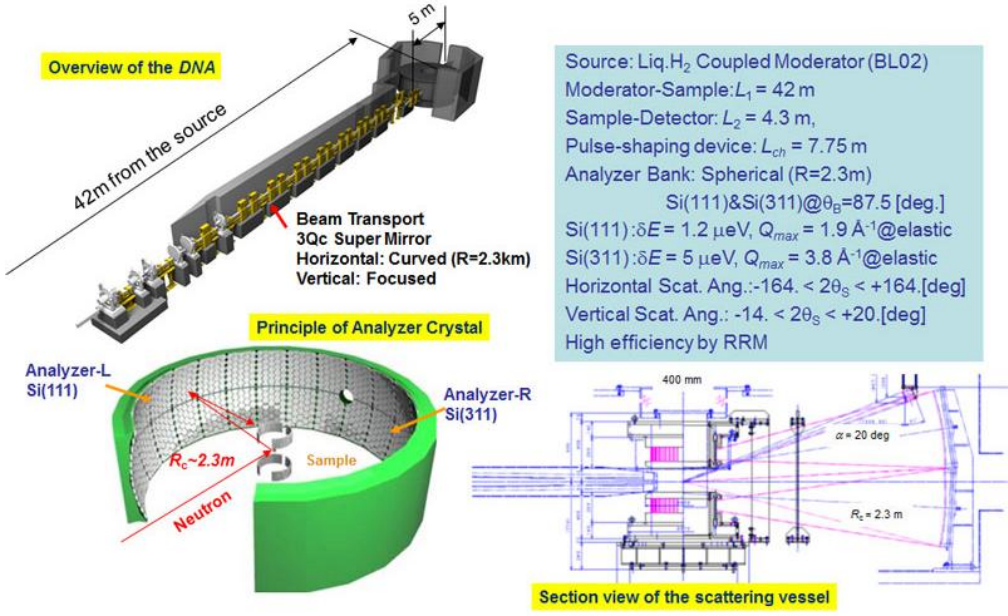
View Online Export Citation CrossMark

H. Seto[1,a] and T. Yamada[2,b]

AFFILIATIONS

[1]Institute of Materials Structure Science/J-PARC Center, High Energy Accelerator Research Organization, Tokai 319-1106, Japan
[2]Neutron Science and Technology Center, Comprehensive Research Organization for Science and Society, Tokai 319-1106, Japan

[a]Author to whom correspondence should be addressed: hideki.seto@kek.jp
[b]Electronic mail: t_yamada@cross.or.jp



J-PARC MLF BL02 DNA: Dynamic Spectrometer