ACM 常用算法模板

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1 数据结构

1.1 并查集

```
struct dsu {
1
2
      int n;
3
      vector<int> fa;
4
      dsu(int _n) : n(_n) {
5
          fa.resize(n + 1);
6
          iota(fa.begin(), fa.end(), 0);
7
      }
8
      int find(int x) { return x == fa[x] ? x : fa[x] = find(fa[x]); }
9
      int merge(int x, int y) {
10
          int fax = find(x), fay = find(y);
11
          if (fax == fay) return 0;  // 一个集合
          return fa[find(x)] = find(y); // 合并到哪个集合了
12
13
      }
14 };
```

1.2 树状数组

一维

```
template <class T>
 1
2
   struct Fenwick_tree {
3
       Fenwick_tree(int n) : n(n), tree(n + 1, 0) {}
4
       T query(int 1, int r) {
5
           auto query = [&](int pos) {
6
                T res = 0;
7
                while (pos) {
8
                    res += tree[pos];
9
                    pos -= lowbit(pos);
10
                }
11
                return res;
12
           };
13
           return query(r) - query(l - 1);
14
15
       void update(int pos, T num) {
16
           while (pos <= n) {</pre>
17
                tree[pos] += num;
18
                pos += lowbit(pos);
19
           }
20
       }
  private:
21
22
       int n;
23
       vector<T> tree;
24 };
```

二维

```
1 template <class T>
2 struct Fenwick_tree_2 {
```

```
3
       Fenwick_tree_2(int n, int m) : n(n), m(m), tree(n + 1, vector<T>(m + 1)) {}
4
       T query(int l1, int r1, int l2, int r2) {
5
           auto query = [&](int 1, int r) {
6
               T res = 0;
7
               for (int i = 1; i; i -= lowbit(i))
                    for (int j = r; j; j -= lowbit(j)) res += tree[i][j];
8
9
10
           };
11
           return query(12, r2) - query(12, r1 - 1) - query(11 - 1, r2) +
12
                  query(11 - 1, r1 - 1);
13
       void update(int x, int y, T num) {
14
15
           for (int i = x; i <= n; i += lowbit(i))</pre>
16
               for (int j = y; j <= m; j += lowbit(j)) tree[i][j] += num;</pre>
17
       }
18
  private:
19
       int n, m;
20
       vector<vector<T>> tree;
21 };
```

三维

```
template <class T>
 1
2
  struct Fenwick_tree_3 {
3
       Fenwick_tree_3(int n, int m, int k)
 4
           : n(n),
5
             m(m),
6
             k(k),
7
             tree(n + 1, vector<vector<T>>(m + 1, vector<T>(k + 1))) {}
8
       T query(int a, int b, int c, int d, int e, int f) {
9
           auto query = [&](int x, int y, int z) {
10
               T res = 0;
11
               for (int i = x; i; i -= lowbit(i))
12
                   for (int j = y; j; j -= lowbit(j))
13
                        for (int p = z; p; p -= lowbit(p)) res += tree[i][j][p];
14
               return res;
15
           };
16
           T res = query(d, e, f);
           res -= query(a - 1, e, f) + query(d, b - 1, f) + query(d, e, c - 1);
17
           res += query(a - 1, b - 1, f) + query(a - 1, e, c - 1) +
18
19
                  query(d, b - 1, c - 1);
           res -= query(a - 1, b - 1, c - 1);
20
21
           return res;
22
       }
23
       void update(int x, int y, int z, T num) {
24
           for (int i = x; i <= n; i += lowbit(i))</pre>
25
               for (int j = y; j <= m; j += lowbit(j))</pre>
                   for (int p = z; p <= k; p += lowbit(p)) tree[i][j][p] += num;</pre>
26
27
       }
28
  private:
29
       int n, m, k;
30
       vector<vector<T>>> tree;
31 };
```

1.3 线段树

```
template <class Data, class Num>
2
  struct Segment_Tree {
3
       inline void update(int 1, int r, Num x) { update(1, 1, r, x); }
4
       inline Data query(int 1, int r) { return query(1, 1, r); }
5
       Segment_Tree(vector<Data>& a) {
6
           n = a.size();
7
           tree.assign(n * 4 + 1, {});
8
           build(a, 1, 1, n);
9
       }
10
  private:
11
       int n;
12
       struct Tree {
13
           int 1, r;
14
           Data data;
15
       };
16
       vector<Tree> tree;
17
       inline void pushup(int pos) {
18
           tree[pos].data = tree[pos << 1].data + tree[pos << 1 | 1].data;</pre>
19
       }
20
       inline void pushdown(int pos) {
21
           tree[pos << 1].data = tree[pos << 1].data + tree[pos].data.lazytag;</pre>
22
           tree[pos << 1 | 1].data =
23
               tree[pos << 1 | 1].data + tree[pos].data.lazytag;</pre>
24
           tree[pos].data.lazytag = Num::zero();
25
26
       void build(vector<Data>& a, int pos, int 1, int r) {
27
           tree[pos].l = 1;
28
           tree[pos].r = r;
29
           if (1 == r) {
30
               tree[pos].data = a[l - 1];
31
               return;
32
           }
           int mid = (tree[pos].l + tree[pos].r) >> 1;
33
           build(a, pos << 1, 1, mid);</pre>
34
35
           build(a, pos << 1 | 1, mid + 1, r);
36
           pushup(pos);
37
       }
       void update(int pos, int& 1, int& r, Num& x) {
38
39
           if (1 > tree[pos].r || r < tree[pos].1) return;</pre>
40
           if (1 <= tree[pos].1 && tree[pos].r <= r) {</pre>
               tree[pos].data = tree[pos].data + x;
41
42
               return;
43
44
           pushdown(pos);
45
           update(pos << 1, 1, r, x);
46
           update(pos << 1 | 1, 1, r, x);
47
           pushup(pos);
```

```
48
49
       Data query(int pos, int& 1, int& r) {
50
           if (1 > tree[pos].r || r < tree[pos].l) return Data::zero();</pre>
           if (1 <= tree[pos].1 && tree[pos].r <= r) return tree[pos].data;</pre>
51
52
           pushdown(pos);
53
           return query(pos << 1, 1, r) + query(pos << 1 | 1, 1, r);
54
       }
55
  };
56
  struct Num {
57
       11 add;
58
       inline static Num zero() { return {0}; }
59
       inline Num operator+(Num b) { return {add + b.add}; }
60 };
61
  struct Data {
62
      ll sum, len;
63
       Num lazytag;
64
       inline static Data zero() { return {0, 0, Num::zero()}; }
65
       inline Data operator+(Num b) {
66
           return {sum + len * b.add, len, lazytag + b};
67
68
       inline Data operator+(Data b) {
69
           return {sum + b.sum, len + b.len, Num::zero()};
70
       }
71
  };
```

1.4 可持久化线段树

```
constexpr int MAXN = 200000;
  vector<int> root(MAXN << 5);</pre>
3
  struct Persistent_seg {
4
       int n;
5
       struct Data {
6
           int ls, rs;
 7
           int val;
8
       };
9
       vector<Data> tree;
10
       Persistent_seg(int n, vector<int>& a) : n(n) { root[0] = build(1, n, a); }
11
       int build(int 1, int r, vector<int>& a) {
12
           if (1 == r) {
13
               tree.push_back({0, 0, a[1]});
14
               return tree.size() - 1;
15
           }
16
           int mid = 1 + r \gg 1;
17
           int ls = build(l, mid, a), rs = build(mid + 1, r, a);
           tree.push_back({ls, rs, tree[ls].val + tree[rs].val});
18
19
           return tree.size() - 1;
20
21
       int update(int rt, const int& idx, const int& val, int l, int r) {
22
           if (1 == r) {
23
               tree.push_back({0, 0, tree[rt].val + val});
24
               return tree.size() - 1;
```

```
25
26
           int mid = 1 + r >> 1, ls = tree[rt].ls, rs = tree[rt].rs;
27
           if (idx <= mid) ls = update(ls, idx, val, l, mid);</pre>
           else rs = update(rs, idx, val, mid + 1, r);
28
29
           tree.push_back({ls, rs, tree[ls].val + tree[rs].val});
30
           return tree.size() - 1;
31
       }
32
       int query(int rt1, int rt2, int k, int l, int r) {
33
           if (1 == r) return 1;
           int mid = 1 + r \gg 1;
34
35
           int lcnt = tree[tree[rt2].ls].val - tree[tree[rt1].ls].val;
           if (k <= lcnt) return query(tree[rt1].ls, tree[rt2].ls, k, l, mid);</pre>
36
37
           else return query(tree[rt1].rs, tree[rt2].rs, k - lcnt, mid + 1, r);
38
       }
39 };
```

1.5 st 表

```
auto lg = []() {
       array<int, 10000001> lg;
3
       lg[1] = 0;
4
       for (int i = 2; i \leftarrow 10000000; i++) lg[i] = lg[i >> 1] + 1;
5
       return lg;
6
  }();
7
   template <typename T>
8
   struct st {
9
       int n;
10
       vector<vector<T>> a;
11
       st(vector<T>& _a) : n(_a.size()) {
12
           a.assign(lg[n] + 1, vector<int>(n));
           for (int i = 0; i < n; i++) a[0][i] = _a[i];</pre>
13
14
           for (int j = 1; j <= lg[n]; j++)</pre>
15
                for (int i = 0; i + (1 << j) - 1 < n; i++)
16
                    a[j][i] = max(a[j - 1][i], a[j - 1][i + (1 << (j - 1))]);
17
18
       T query(int 1, int r) {
19
           int k = lg[r - l + 1];
20
           return max(a[k][1], a[k][r - (1 << k) + 1]);</pre>
21
       }
22 };
```

2 图论

存图

```
1
  struct Graph {
2
       int n;
3
       struct Edge {
           int to, w;
 4
5
       };
 6
       vector<vector<Edge>> graph;
7
       Graph(int _n) {
           n = _n;
8
9
           graph.assign(n + 1, vector<Edge>());
10
11
       void add(int u, int v, int w) { graph[u].push_back({v, w}); }
12 };
```

2.1 最短路

dijkstra

```
void dij(Graph& graph, vector<int>& dis, int t) {
2
       vector<int> visit(graph.n + 1, 0);
3
       priority_queue<pair<int, int>> que;
 4
       dis[t] = 0;
5
       que.emplace(0, t);
6
       while (!que.empty()) {
7
           int u = que.top().second;
8
           que.pop();
9
           if (visit[u]) continue;
10
           visit[u] = 1;
11
           for (auto& [to, w] : graph.graph[u]) {
12
               if (dis[to] > dis[u] + w) {
13
                   dis[to] = dis[u] + w;
14
                   que.emplace(-dis[to], to);
15
               }
16
           }
17
       }
18 }
```

2.2 树上问题

2.2.1 最近公公祖先

倍增法

```
vector<int> dep;
vector<array<int, 21>> fa;
dep.assign(n + 1, 0);
fa.assign(n + 1, array<int, 21>{});
void binary_jump(int root) {
  function<void(int)> dfs = [&](int t) {
```

```
7
           dep[t] = dep[fa[t][0]] + 1;
8
           for (auto& [to] : graph[t]) {
9
               if (to == fa[t][0]) continue;
10
               fa[to][0] = t;
               dfs(to);
11
12
           }
13
       };
       dfs(root);
14
15
       for (int j = 1; j <= 20; j++)
16
           for (int i = 1; i <= n; i++) fa[i][j] = fa[fa[i][j - 1]][j - 1];</pre>
17
  int lca(int x, int y) {
18
19
       if (dep[x] < dep[y]) swap(x, y);</pre>
       for (int i = 20; i >= 0; i--)
20
21
           if (dep[fa[x][i]] >= dep[y]) x = fa[x][i];
       if (x == y) return x;
22
23
       for (int i = 20; i >= 0; i--) {
           if (fa[x][i] != fa[y][i]) {
24
25
               x = fa[x][i];
26
               y = fa[y][i];
27
           }
28
29
       return fa[x][0];
30 }
```

树剖

```
int lca(int x, int y) {
    while (top[x] != top[y]) {
        if (dep[top[x]] < dep[top[y]]) swap(x, y);
        x = fa[top[x]];
    }
    if (dep[x] < dep[y]) swap(x, y);
    return y;
}</pre>
```

2.2.2 树链剖分

```
1 vector<int> fa, siz, dep, son, dfn, rnk, top;
2 fa.assign(n + 1, 0);
3 | siz.assign(n + 1, 0);
 4 dep.assign(n + 1, 0);
5
  son.assign(n + 1, 0);
6 dfn.assign(n + 1, 0);
7
  rnk.assign(n + 1, 0);
8
  top.assign(n + 1, 0);
9
  void hld(int root) {
10
       function<void(int)> dfs1 = [&](int t) {
           dep[t] = dep[fa[t]] + 1;
11
12
           siz[t] = 1;
13
           for (auto& [to, w] : graph[t]) {
14
               if (to == fa[t]) continue;
```

```
15
                fa[to] = t;
16
                dfs1(to);
17
                if (siz[son[t]] < siz[to]) son[t] = to;</pre>
                siz[t] += siz[to];
18
19
           }
20
       };
       dfs1(root);
21
22
       int dfn_tail = 0;
23
       for (int i = 1; i <= n; i++) top[i] = i;</pre>
       function<void(int)> dfs2 = [&](int t) {
24
25
           dfn[t] = ++dfn_tail;
           rnk[dfn_tail] = t;
26
27
           if (!son[t]) return;
28
           top[son[t]] = top[t];
29
           dfs2(son[t]);
           for (auto& [to, w] : graph[t]) {
30
31
                if (to == fa[t] || to == son[t]) continue;
32
33
           }
34
       };
35
       dfs2(root);
36
```

2.3 强连通分量

```
void tarjan(Graph& g1, Graph& g2) {
2
       int dfn_tail = 0, cnt = 0;
3
       vector\langle int \rangle dfn(g1.n + 1, 0), low(g1.n + 1, 0), exist(g1.n + 1, 0),
4
           belong(g1.n + 1, 0);
5
       stack<int> sta;
6
       function<void(int)> dfs = [&](int t) {
7
           dfn[t] = low[t] = ++dfn_tail;
8
           sta.push(t);
9
           exist[t] = 1;
10
           for (auto& [to] : g1.graph[t])
11
                if (!dfn[to]) {
12
                    dfs(to);
13
                    low[t] = min(low[t], low[to]);
                } else if (exist[to]) low[t] = min(low[t], dfn[to]);
14
15
           if (dfn[t] == low[t]) {
16
                cnt++;
17
                while (int temp = sta.top()) {
                    belong[temp] = cnt;
18
19
                    exist[temp] = 0;
20
                    sta.pop();
21
                    if (temp == t) break;
22
                }
23
           }
24
       };
25
       for (int i = 1; i <= g1.n; i++)</pre>
26
           if (!dfn[i]) dfs(i);
```

2.4 拓扑排序

```
void toposort(Graph& g, vector<int>& dis) {
2
      vector<int> in(g.n + 1, 0);
3
      for (int i = 1; i <= g.n; i++)
4
           for (auto& [to] : g.graph[i]) in[to]++;
5
      queue<int> que;
6
      for (int i = 1; i <= g.n; i++)
7
           if (!in[i]) {
8
               que.push(i);
9
               dis[i] = g.w[i]; // dp
10
11
      while (!que.empty()) {
12
           int u = que.front();
13
           que.pop();
14
           for (auto& [to] : g.graph[u]) {
15
               in[to]--;
16
               dis[to] = max(dis[to], dis[u] + g.w[to]); // dp
17
               if (!in[to]) que.push(to);
18
           }
19
      }
20 }
```

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3 字符串

3.1 kmp

```
auto kmp(string& s) {
1
2
       vector next(s.size(), -1);
3
       for (int i = 1, j = -1; i < s.size(); i++) {</pre>
4
           while (j \ge 0 \&\& s[i] != s[j + 1]) j = next[j];
5
           if (s[i] == s[j + 1]) j++;
6
           next[i] = j;
7
       }
8
       // next 意为长度
9
       for (auto& i : next) i++;
10
       return next;
11
```

3.2 哈希

```
1 constexpr int N = 2e6;
2 constexpr 11 mod[2] = {20000000011, 2000000033}, base[2] = {20011, 20033};
3
  vector<array<11, 2>> pow_base(N);
5
  pow_base[0][0] = pow_base[0][1] = 1;
  for (int i = 1; i < N; i++) {</pre>
6
       pow_base[i][0] = pow_base[i - 1][0] * base[0] % mod[0];
7
       pow_base[i][1] = pow_base[i - 1][1] * base[1] % mod[1];
8
9
10
  struct Hash {
11
12
       int size;
13
       vector<array<11, 2>> hash;
14
       Hash() {}
15
       Hash(const string& s) {
           size = s.size();
16
17
           hash.resize(size);
18
           hash[0][0] = hash[0][1] = s[0];
19
           for (int i = 1; i < size; i++) {</pre>
               hash[i][0] = (hash[i - 1][0] * base[0] + s[i]) % mod[0];
20
21
               hash[i][1] = (hash[i - 1][1] * base[1] + s[i]) % mod[1];
           }
22
23
       }
24
       array<11, 2> operator[](const array<int, 2>& range) const {
25
           int 1 = range[0], r = range[1];
           if (1 == 0) return hash[r];
26
27
           auto single_hash = [&](bool flag) {
28
               return (hash[r][flag] -
29
                        hash[l - 1][flag] * pow_base[r - l + 1][flag] % mod[flag] +
30
                        mod[flag]) %
31
                       mod[flag];
32
           };
33
           return {single_hash(0), single_hash(1)};
```

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```
34 }; 35 |
```

3.3 manacher

```
void manacher(const string& _s, vector<int>& r) {
2
       string s(_s.size() * 2 + 1, '$');
3
       for (int i = 0; i < _s.size(); i++) s[2 * i + 1] = _s[i];
4
       r.resize(_s.size() * 2 + 1);
5
       for (int i = 0, maxr = 0, mid = 0; i < s.size(); i++) {</pre>
6
           if (i < maxr) r[i] = min(r[mid * 2 - i], maxr - i);</pre>
7
           while (i - r[i] - 1 >= 0 \&\& i + r[i] + 1 < s.size() \&\&
8
                  s[i - r[i] - 1] == s[i + r[i] + 1])
9
               ++r[i];
10
           if (i + r[i] > maxr) maxr = i + r[i], mid = i;
11
      }
12 }
```

4 数学

4.1 扩展欧几里得

```
\begin{split} x &= x + k * dx, y = y - k * dy \\ \text{若要求 } x &> 0, \ k > -\frac{x}{dx} \Rightarrow k \geq \left\lceil \frac{-x+1}{dx} \right\rceil \\ \text{若要求 } x &\geq 0, \ k > -\frac{x}{dx} \Rightarrow k \geq \left\lceil -\frac{x}{dx} \right\rceil \\ \text{若要求 } y &> 0, \ k < \frac{y}{dy} \Rightarrow k \leq \left\lfloor \frac{y-1}{dy} \right\rfloor \\ \text{若要求 } y &\geq 0, \ k < \frac{y}{dy} \Rightarrow k \leq \left\lceil \frac{y}{dy} \right\rceil \end{split}
```

```
int __exgcd(int a, int b, int& x, int& y) {
2
      if (!b) {
3
           x = 1;
4
           y = 0;
5
           return a;
6
       }
7
       int d = __exgcd(b, a % b, x, y);
8
       int t = x;
9
       x = y;
       y = t - (a / b) * y;
10
11
       return d;
12
  array<int, 2> exgcd(int a, int b, int c) {
13
       int x, y;
14
15
       int gcd_a_b = __exgcd(a, b, x, y);
16
       if (c % gcd_a_b) return {INT_MAX, INT_MAX};
17
       x *= c / gcd_a_b;
18
       y *= c / gcd_a_b;
19
       int dx = b / gcd_a_b;
20
       int dy = a / gcd_a_b;
21
       // x = x + k* dx y = y - k* dy
       // 调整为 x >=0 的最小解
22
       int k = ceil(-1.0 * x / dx);
23
       x += k * dx;
24
25
       y -= k * dy;
26
       return {x, y};
27 }
```

4.2 线性筛法

```
1
  auto [min_prime, prime] = []() {
2
      constexpr int N = 10000000;
3
      vector<int> min_prime(N + 1, 0), prime;
4
      for (int i = 2; i <= N; i++) {
5
           if (min_prime[i] == 0) {
6
               min_prime[i] = i;
7
               prime.push_back(i);
8
9
           for (auto& j : prime) {
10
               if (j > min_prime[i] || j > N / i) break;
11
               min_prime[j * i] = j;
```

4.3 分解质因数

```
auto num_prime(int num) {
2
       vector<array<int, 2>> res;
3
       for (auto& i : prime) {
4
           if (i > num / i) break;
5
           if (num % i == 0) {
6
               res.push_back({i, 0});
7
               while (num % i == 0) {
8
                    num /= i;
9
                    res.back()[1]++;
10
               }
           }
11
12
13
       if (num > 1) res.push_back({num, 1});
14
       return res;
15 }
```

4.4 组合数

```
1 array<modint, N + 1> fac, ifac;
  fac[0] = ifac[0] = 1;
3
  for (int i = 1; i <= N; i++) {
       fac[i] = fac[i - 1] * i;
 4
5
       ifac[i] = fac[i].inv();
6
  }
7
  modint C(int n, int m) {
8
       if (n < m) return 0;</pre>
9
       if (m == 0) return 1;
       if (n <= mod) return fac[n] * ifac[m] * ifac[n - m];</pre>
10
11
       // n >= mod 时需要这个
12
       return C(n % mod, m % mod) * C(n / mod, m / mod);
13 }
```

4.5 数论分块

```
求解形如 \sum_{i=1}^n f(i)g(\lfloor \frac{n}{i} \rfloor) 的合式 s(n) = \sum_{i=1}^n f(i)
```

```
modint sqrt_decomposition(int n) {
    auto s = [&](int x) { return x; };
    auto g = [&](int x) { return x; };
    int l = 1;
    modint res = 0;
    while (1 <= n) {</pre>
```

```
int r = n / (n / 1);
res = res + (ll)(s(r) - s(l - 1)) * g(n / 1);

l = r + 1;

return res;
}
```

4.6 盒子与球

n 个球, m 个盒

球同	盒同	可空	公式
✓	✓	✓	$f_{n,m} = f_{n-1,m-1} + f_{n-m,m}$
✓	✓	×	$f_{n-m,m}$
×	✓	✓	$\sum_{i=1}^{m} g_{n,i}$
×	✓	×	$g_{n,m} = g_{n-1,m-1} + m * g_{n-1,m}$
✓	×	✓	C_{n+m-1}^{m-1}
✓	×	×	C_{n-1}^{m-1}
×	×	✓	m^n
×	×	×	$m!*g_{n,m}$

4.7 线性基

```
// 线性基
1
2
  struct basis {
3
      array<unsigned 11, 64> p{};
4
5
      // 将×插入此线性基中
6
      void insert(unsigned ll x) {
7
          for (int i = 63; i >= 0; i--) {
8
               if ((x >> i) & 1) {
9
                  if (p[i]) x ^= p[i];
10
                   else {
11
                       p[i] = x;
                       break;
12
13
                   }
14
               }
15
          }
      }
16
17
18
      // 将另一个线性基插入此线性基中
      void insert(basis other) {
19
20
          for (int i = 0; i <= 63; i++) {</pre>
21
               if (!other.p[i]) continue;
22
               insert(other.p[i]);
23
```

```
24
       }
25
26
      // 最大异或值
27
      unsigned ll max_basis() {
28
           unsigned 11 res = 0;
29
           for (int i = 63; i >= 0; i--)
30
               if ((res ^ p[i]) > res) res ^= p[i];
31
           return res;
32
      }
33 };
```

4.8 矩阵快速幂

```
constexpr 11 mod = 2147493647;
2
   struct Mat {
3
       int n, m;
4
       vector<vector<ll>>> mat;
5
       Mat(int n, int m) : n(n), m(n), mat(n, vector<ll>(m, 0)) {}
6
       Mat(vector<vector<1l>> mat) : n(mat.size()), m(mat[0].size()), mat(mat) {}
7
       Mat operator*(const Mat& other) {
8
            assert(m == other.n);
9
            Mat res(n, other.m);
10
            for (int i = 0; i < res.n; i++)</pre>
11
                for (int j = 0; j < res.m; j++)</pre>
12
                     for (int k = 0; k < m; k++)
13
                          res.mat[i][j] =
                              (\texttt{res.mat[i][j]} + \texttt{mat[i][k]} * \texttt{other.mat[k][j]} \% \; \texttt{mod)} \; \%
14
15
16
            return res;
17
       }
18
  };
19
  Mat ksm(Mat a, ll b) {
20
       assert(a.n == a.m);
21
       Mat res(a.n, a.m);
22
       for (int i = 0; i < res.n; i++) res.mat[i][i] = 1;</pre>
23
       while (b) {
24
            if (b & 1) res = res * a;
25
            b >>= 1;
26
            a = a * a;
27
       }
28
       return res;
29 }
```

```
1 double eps = 1e-8;
  const double PI = acos(-1);
3 using T = 11;
 4
5
  template <typename T>
6
  int cmp(T a, T b) {
       return a != b ? a < b ? -1 : 1 : 0;
7
8
9
  int cmp(double a, double b) {
10
11
       double c = a - b;
12
       if (abs(c) < eps) return 0;</pre>
13
       return c < 0 ? -1 : 1;
14 }
15
16 // 向量
17
  struct vec {
18
      T x, y;
19
       vec(T_x = 0, T_y = 0) : x(_x), y(_y) {}
20
21
22
       double length() const { return sqrt(x * x + y * y); }
23
24
       // 与×轴正方向的夹角
25
       double angle() const {
26
           double angle = atan2(y, x);
           if (angle < 0) angle += 2 * PI;</pre>
27
28
           return angle;
29
       }
30
31
       // 逆时针旋转
32
       vec &rotate(const double &theta) {
33
           double tmp = x;
34
           x = x * cos(theta) - y * sin(theta);
35
           y = y * cos(theta) + tmp * sin(theta);
           return *this;
36
37
       }
38
       bool operator==(const vec &other) const {
39
40
           return !cmp(x, other.x) && !cmp(y, other.y);
41
       }
42
       bool operator<(const vec &other) const {</pre>
43
           int tmp = cmp(angle(), other.angle());
44
           if (tmp) return tmp == -1 ? 0 : 1;
45
           tmp = cmp(x, other.x);
46
           return tmp == -1 ? 0 : 1;
47
       }
48
49
       vec operator+(const vec &other) const { return {x + other.x, y + other.y}; }
50
       vec operator-() const { return {-x, -y}; }
```

```
51
       vec operator-(const vec &other) const { return -other + (*this); }
52
       vec operator*(const T &other) const { return {x * other, y * other}; }
53
       vec operator/(const T &other) const { return {x / other, y / other}; }
       T operator*(const vec &other) const { return x * other.x + y * other.y; }
54
55
56
       // 叉积 结果大于0, a到b为逆时针, 小于0, a到b顺时针,
57
       // 等于0共线,可能同向或反向,结果绝对值表示 a b 形成的平行四边行的面积
58
       T operator^(const vec &other) const { return x * other.y - y * other.x; }
59
60
       friend istream &operator>>(istream &input, vec &data) {
61
           input >> data.x >> data.y;
62
           return input;
63
       }
64
       friend ostream &operator<<(ostream &output, const vec &data) {</pre>
65
           output << fixed << setprecision(6);</pre>
           output << data.x << " " << data.y;</pre>
66
67
           return output;
68
       }
69 };
70
71 T cross(const vec &a, const vec &b, const vec &c) { return (a - c) ^ (b - c); }
72
73 // 两点间的距离
74
   T distance(const vec &a, const vec &b) {
75
       return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
76
77
78
   // 两向量夹角
79 double angle(const vec &a, const vec &b) {
80
       double theta = abs(a.angle() - b.angle());
81
       if (theta > PI) theta = 2 * PI - theta;
82
       return theta;
83 }
84
85
   // 判断点是否在凸包内
86
   bool in polygon(const vec &a, vector<vec> &p) {
87
       int n = p.size();
88
       if (n == 1) return a == p[0];
89
       if (cross(a, p[1], p[0]) > 0 || cross(p.back(), a, p[0]) > 0) return 0;
90
       auto cmp = [&p](vec &x, const vec &y) { return ((x - p[0]) ^ y) >= 0; };
91
       int i = lower_bound(p.begin() + 2, p.end(), a - p[0], cmp) - p.begin() - 1;
92
       return cross(p[(i + 1) % n], a, p[i]) >= 0;
93 }
94
95
   // 多边形的面积
96
   double polygon area(vector<vec> &p) {
97
       for (int i = 1; i < p.size(); i++) area += p[i - 1] ^ p[i];</pre>
98
99
       area += p.back() ^ p[0];
100
       return abs(area / 2.0);
101
   }
102
```

```
103 // 多边形的周长
104
   double polygon_length(vector<vec> &p) {
       double length = 0;
105
       for (int i = 1; i < p.size(); i++) length += (p[i - 1] - p[i]).length();</pre>
106
107
       length += (p.back() - p[0]).length();
108
       return length;
109
110
   // 以整点为顶点的线段上的整点个数
111
   T count(const vec &a, const vec &b) {
112
113
       vec c = a - b;
114
       return gcd(abs(c.x), abs(c.y)) + 1;
115 }
116
117
   // 以整点为顶点的多边形边上整点个数
118
   T count(vector<vec> &p) {
119
       T cnt = 0;
120
       for (int i = 1; i < p.size(); i++) cnt += count(p[i - 1], p[i]);</pre>
121
       cnt += count(p.back(), p[0]);
122
       return cnt - p.size();
123 }
124
125
   // 凸包直径的两个端点
126
   auto polygon_dia(vector<vec> &p) {
127
       int n = p.size();
128
       array<vec, 2> res{};
129
       if (n == 1) return res;
       if (n == 2) return res = {p[0], p[1]};
130
131
       T mx = 0;
       for (int i = 0, j = 2; i < n; i++) {
132
133
            while (abs(cross(p[i], p[(i + 1) % n], p[j])) <=</pre>
134
                   abs(cross(p[i], p[(i + 1) % n], p[(j + 1) % n]))
135
                j = (j + 1) \% n;
136
            if (T tmp = distance(p[i], p[j]); tmp > mx) {
137
                mx = tmp;
138
                res = {p[i], p[j]};
139
140
            if (T tmp = distance(p[(i + 1) % n], p[j]); tmp > mx) {
141
                mx = tmp;
142
                res = \{p[(i + 1) \% n], p[j]\};
143
            }
144
145
       return res;
146
147
148
   // 凸包
149
   auto convex_hull(vector<vec> &p) {
150
       sort(p.begin(), p.end(), [](vec &a, vec &b) {
151
            int tmp = cmp(a.x, b.x);
152
            if (tmp) return tmp == -1 ? 0 : 1;
            tmp = cmp(a.y, b.y);
153
154
            return tmp == -1 ? 0 : 1;
```

```
155
        });
156
        int n = p.size();
157
        vector sta(n + 1, 0);
        vector v(n, false);
158
159
        int tp = -1;
160
        sta[++tp] = 0;
161
        auto update = [&](int lim, int i) {
            while (tp > lim &&
162
                    ((p[sta[tp]] - p[sta[tp - 1]]) ^ (p[i] - p[sta[tp]])) <= 0)
163
164
                v[sta[tp--]] = 0;
165
            sta[++tp] = i;
166
            v[i] = 1;
167
        };
        for (int i = 1; i < n; i++) update(0, i);</pre>
168
169
        int cnt = tp;
170
        for (int i = n - 1; i >= 0; i--) {
171
            if (v[i]) continue;
172
            update(cnt, i);
173
        }
174
        vector<vec> res(tp);
175
        for (int i = 0; i < tp; i++) res[i] = p[sta[i]];</pre>
176
        return res;
177
178
179
   // 闵可夫斯基和 两个点集的和构成一个凸包
180
   auto minkowski(vector<vec> &a, vector<vec> &b) {
181
        int n = a.size(), m = b.size();
182
        vector<vec> c{a[0] + b[0]};
183
        c.reserve(n + m);
184
        int i = 0, j = 0;
185
        while (i < n && j < m) {</pre>
            vec x = a[(i + 1) \% n] - a[i];
186
187
            vec y = b[(j + 1) \% m] - b[j];
            c.push_back(c.back() + ((x ^ y) >= 0 ? (i++, x) : (j++, y)));
188
189
        }
190
        while (i + 1 < n) {
191
            c.push_back(c.back() + a[(i + 1) % n] - a[i]);
192
            i++;
193
194
        while (j + 1 < m) {
195
            c.push_back(c.back() + b[(j + 1) \% m] - b[j]);
196
            j++;
197
        }
198
        return c;
199 }
200
201 // 直线
202
   struct line {
203
        vec point, direction;
204
        line(const vec &p = vec(), const vec &d = vec()) : point(p), direction(d) {}
205 };
206
```

```
207 // 点到直线距离
208
   double distance(const vec &a, const line &b) {
209
       return abs((b.point - a) ^ (b.point + b.direction - a)) /
              b.direction.length();
210
211
212
213
   // 判断点在直线哪边,大于0在左边,等于0在线上,小于0在右边
214
   T side_line(const vec &a, const line &b) { return b.direction ^ (a - b.point); }
215
216
   // 两直线是否垂直
   bool perpendicular(const line &a, const line &b) {
217
       return !cmp(a.direction * b.direction, 0);
218
219
   }
220
221
   // 点的垂线是否与线段有交点
222
   bool perpendicular(const vec &a, const line &b) {
223
       vec perpen(-b.direction.y, b.direction.x);
224
       bool cross1 = (perpen ^ (b.point - a)) > 0;
225
       bool cross2 = (perpen ^ (b.point + b.direction - a)) > 0;
226
       return cross1 != cross2;
227
228
229
   // 两直线是否平行
230
   bool parallel(const line &a, const line &b) {
231
       return !cmp(a.direction ^ b.direction, 0);
232
233
234
   // 两直线交点
235
   vec intersection(T A, T B, T C, T D, T E, T F) {
       return {(B * F - C * E) / (A * E - B * D),
236
237
               (C * D - A * F) / (A * E - B * D);
238
   }
239
240
   // 两直线交点
241
   vec intersection(const line &a, const line &b) {
242
       return intersection(a.direction.y, -a.direction.x,
243
                           a.direction.x * a.point.y - a.direction.y * a.point.x,
                           b.direction.y, -b.direction.x,
244
245
                           b.direction.x * b.point.y - b.direction.y * b.point.x);
246
247
   struct circle {
248
249
       vec o;
250
       double r;
251
       circle(const vec &_o, T _r) : o(_o), r(_r){};
252
       // 点与圆的关系 -1在圆内, 0在圆上, 1在圆外
253
       int relation(const vec &other) const {
254
           double len = (other - o).length();
255
           return cmp(len, r);
256
       }
257
       double area() { return PI * r * r; }
258 };
```

```
259
260
       圆与直线交点
   auto intersection(const circle &c, const line &l) {
261
262
        double d = distance(c.o, 1);
263
       vector<vec> res;
        double len = 1.direction.length();
264
265
        vec mid = 1.point + 1.direction * ((c.o - 1.point) * 1.direction / len);
        if (!cmp(d, c.r)) res.push_back(mid);
266
        else if (d < c.r) {</pre>
267
268
            d = sqrt(c.r * c.r - d * d) / len;
            res.push_back(mid + 1.direction * d);
269
            res.push_back(mid - 1.direction * d);
270
271
        }
272
        return res;
273
274
275
   // oab三角形与圆相交的面积
   double area(const circle &c, const vec &a, const vec &b) {
276
277
       vec oa = a - c.o, ob = b - c.o;
        T cab = oa ^ ob;
278
279
       if (!cmp(cab, 0)) return 0;
        if (c.relation(a) != 1 && c.relation(b) != 1) return cab / 2.0;
280
281
        vec ba = a - b, bo = -ob;
282
        vec ab = -ba, ao = -oa;
283
        auto r = c.r;
284
        double ang;
285
        double loa = oa.length(), lob = ob.length(), lab = ab.length();
286
        double x =
287
            (ba * bo + sqrt(r * r * lab * lab - (ba ^ bo) * (ba ^ bo))) / lab;
288
        double y =
289
            (ab * ao + sqrt(r * r * lab * lab - (ab ^ ao) * (ab ^ ao))) / lab;
290
        if (cmp(lob, r) == -1 \&\& cmp(loa, r) != -1) {
291
            ang = cab * (1 - x / lab) / (r * loa);
292
            ang = min(max((double)-1, ang), (double)1);
293
            return (asin(ang) * r * r + cab * x / lab) / 2;
294
295
        if (cmp(lob, r) != -1 \&\& cmp(loa, r) == -1) {
296
            ang = cab * (1 - y / lab) / (r * lob);
297
            ang = min(max((double)-1, ang), (double)1);
298
            return (asin(ang) * r * r + cab * y / lab) / 2;
299
        }
300
        if (cmp(abs(cab), r * lab) != -1 || cmp(ab * ao, 0) != 1 ||
301
            cmp(ba * bo, 0) != 1) {
302
            ang = cab / (loa * lob);
303
            ang = min(max((double)-1, ang), (double)1);
304
            double tmp = -asin(ang);
305
            if (cmp(oa * ob, 0) == -1)
306
                if (cmp(cab, 0) == -1) tmp -= PI;
307
                else tmp += PI;
308
            else tmp = -tmp;
309
            return tmp * r * r / 2;
310
```

```
311
       ang = cab * (1 - x / lab) / (r * loa);
312
       ang = min(max((double)-1, ang), (double)1);
313
       double ang2 = cab * (1 - y / lab) / (r * lob);
       ang2 = min(max((double)-1, ang2), (double)1);
314
315
       return ((a\sin(ang) + a\sin(ang2)) * r * r + cab * ((x + y) / lab - 1)) / 2;
316
317
318
   // 多边形与圆相交的面积
319
   double area(vector<vec> &p, circle c) {
320
       double res = 0;
321
       for (int i = 1; i < p.size(); i++) res += area(c, p[i - 1], p[i]);
322
       res += area(c, p.back(), p[0]);
323
       return abs(res);
324
```

5.1 扫描线

```
1 #define ls (pos << 1)
  #define rs (ls | 1)
3 #define mid ((tree[pos].l + tree[pos].r) >> 1)
  struct Rectangle {
5
      11 x_1, y_1, x_r, y_r;
6
  };
7
  11 area(vector<Rectangle>& rec) {
8
       struct Line {
9
           11 x, y_up, y_down;
10
           int pd;
11
       };
       vector<Line> line(rec.size() * 2);
12
13
       vector<ll> y_set(rec.size() * 2);
14
       for (int i = 0; i < rec.size(); i++) {</pre>
15
           y_set[i * 2] = rec[i].y_l;
16
           y_{set[i * 2 + 1] = rec[i].y_r;}
17
           line[i * 2] = {rec[i].x_l, rec[i].y_r, rec[i].y_l, 1};
           line[i * 2 + 1] = {rec[i].x_r, rec[i].y_r, rec[i].y_l, -1};
18
19
20
       sort(y_set.begin(), y_set.end());
21
       y_set.erase(unique(y_set.begin(), y_set.end()), y_set.end());
       sort(line.begin(), line.end(), [](Line a, Line b) { return a.x < b.x; });</pre>
22
23
       struct Data {
24
           int 1, r;
           11 len, cnt, raw_len;
25
26
27
       vector<Data> tree(4 * y_set.size());
28
       function<void(int, int, int)> build = [&](int pos, int 1, int r) {
29
           tree[pos].l = 1;
           tree[pos].r = r;
30
31
           if (1 == r) {
32
               tree[pos].raw_len = y_set[r + 1] - y_set[l];
33
               tree[pos].cnt = tree[pos].len = 0;
34
               return;
```

```
35
36
           build(ls, 1, mid);
37
           build(rs, mid + 1, r);
38
           tree[pos].raw_len = tree[ls].raw_len + tree[rs].raw_len;
39
       };
       function<void(int, int, int, int)> update = [&](int pos, int 1, int r,
40
41
                                                          int num) {
42
           if (1 <= tree[pos].1 && tree[pos].r <= r) {</pre>
43
               tree[pos].cnt += num;
44
               tree[pos].len = tree[pos].cnt ? tree[pos].raw_len
45
                                 : tree[pos].1 == tree[pos].r
                                     ? 0
46
47
                                     : tree[ls].len + tree[rs].len;
48
               return;
49
           }
           if (1 <= mid) update(ls, 1, r, num);</pre>
50
51
           if (r > mid) update(rs, l, r, num);
52
           tree[pos].len =
53
               tree[pos].cnt ? tree[pos].raw_len : tree[ls].len + tree[rs].len;
54
       };
55
       build(1, 0, y_set.size() - 2);
56
       auto find_pos = [&](ll num) {
57
           return lower_bound(y_set.begin(), y_set.end(), num) - y_set.begin();
58
       };
59
       11 \text{ res} = 0;
60
       for (int i = 0; i < line.size() - 1; i++) {</pre>
           update(1, find_pos(line[i].y_down), find_pos(line[i].y_up) - 1,
61
62
                   line[i].pd);
63
           res += (line[i + 1].x - line[i].x) * tree[1].len;
64
65
       return res;
66 }
```

6 杂项

6.1 高精度

```
1
  struct bignum {
2
       string num;
3
4
       bignum() : num("0") {}
5
       bignum(const string& num) : num(num) {
6
           reverse(this->num.begin(), this->num.end());
7
8
       bignum(ll num) : num(to_string(num)) {
9
           reverse(this->num.begin(), this->num.end());
10
       }
11
12
       bignum operator+(const bignum& other) {
13
           bignum res;
14
           res.num.pop_back();
15
           res.num.reserve(max(num.size(), other.num.size()) + 1);
16
           for (int i = 0, j = 0, x; i < num.size() || i < other.num.size() || j;
17
                i++) {
18
               x = j;
19
               j = 0;
20
               if (i < num.size()) x += num[i] - '0';</pre>
21
               if (i < other.num.size()) x += other.num[i] - '0';</pre>
22
               if (x >= 10) j = 1, x -= 10;
23
               res.num.push_back(x + '0');
24
25
           res.num.capacity();
26
           return res;
27
       }
28
29
       bignum operator*(const bignum& other) {
30
           vector<int> res(num.size() + other.num.size() - 1, 0);
           for (int i = 0; i < num.size(); i++)</pre>
31
32
               for (int j = 0; j < other.num.size(); j++)</pre>
33
                    res[i + j] += (num[i] - '0') * (other.num[j] - '0');
34
           int g = 0;
           for (int i = 0; i < res.size(); i++) {</pre>
35
36
               res[i] += g;
37
               g = res[i] / 10;
38
               res[i] %= 10;
39
40
           while (g) {
               res.push_back(g % 10);
41
42
               g /= 10;
43
44
           int lim = res.size();
           while (lim > 1 && res[lim - 1] == 0) lim--;
45
46
           bignum res2;
47
           res2.num.resize(lim);
48
           for (int i = 0; i < lim; i++) res2.num[i] = res[i] + '0';
```

```
49
            return res2;
50
       }
51
52
       bool operator<(const bignum& other) {</pre>
53
           if (num.size() == other.num.size())
54
                for (int i = num.size() - 1; i >= 0; i--)
55
                    if (num[i] == other.num[i]) continue;
56
                    else return num[i] < other.num[i];</pre>
            return num.size() < other.num.size();</pre>
57
58
       }
59
60
       friend istream& operator>>(istream& in, bignum& a) {
61
           in >> a.num;
62
            reverse(a.num.begin(), a.num.end());
63
           return in;
64
       }
65
       friend ostream& operator<<(ostream& out, bignum a) {</pre>
66
            reverse(a.num.begin(), a.num.end());
67
           return out << a.num;</pre>
68
       }
69 };
```

6.2 模运算

```
1
  constexpr int N = 1e5;
  constexpr int mod = 1e9 + 7;
3
  struct modint {
 4
       int x;
5
       modint(11 _x = 0) : x(_x \% mod) {}
 6
       modint pow(ll b) const {
7
           modint res(1), a = *this;
8
           while (b) {
9
               if (b & 1) res = res * a;
10
               a = a * a;
11
               b >>= 1;
12
13
           return res;
14
       }
       modint inv() const { return pow(mod - 2); }
15
16
       modint operator+(const modint& other) { return modint(x + other.x); }
17
       modint operator-() const { return {-x}; }
18
       modint operator-(const modint& other) { return modint(-other + *this); }
19
       modint operator*(const modint& other) { return modint((11)x * other.x); }
20
       modint operator/(const modint& other) { return *this * other.inv(); }
21
       friend istream& operator>>(istream& is, modint& other) {
22
           11 x;
23
           is >> _x;
24
           other = modint(_x);
25
           return is;
26
       }
27
       friend ostream& operator<<(ostream& os, modint other) {</pre>
```

6.3 分数

```
struct frac {
 1
2
       11 a, b;
3
       frac(): a(0), b(1) {}
4
       frac(ll _a, ll _b) : a(_a), b(_b) {
5
           assert(b);
6
           if (a) {
7
               int tmp = gcd(a, b);
8
               a /= tmp;
9
               b /= tmp;
10
           } else *this = frac();
11
12
       frac operator+(const frac& other) {
13
           return frac(a * other.b + other.a * b, b * other.b);
14
15
       frac operator-() const {
16
           frac res = *this;
17
           res.a = -res.a;
18
           return res;
19
       }
20
       frac operator-(const frac& other) const { return -other + *this; }
21
       frac operator*(const frac& other) const {
22
           return frac(a * other.a, b * other.b);
23
       }
24
       frac operator/(const frac& other) const {
25
           assert(other.a);
26
           return *this * frac(other.b, other.a);
27
       }
28
       bool operator<(const frac& other) const { return (*this - other).a < 0; }</pre>
29
       bool operator<=(const frac& other) const { return (*this - other).a <= 0; }</pre>
30
       bool operator>=(const frac& other) const { return (*this - other).a >= 0; }
31
       bool operator>(const frac& other) const { return (*this - other).a > 0; }
       bool operator==(const frac& other) const {
32
33
           return a == other.a && b == other.b;
34
       }
35
       bool operator!=(const frac& other) const { return !(*this == other); }
36 };
```

6.4 表达式求值

```
1 // 格式化表达式
2 string format(const string& s1) {
3    stringstream ss(s1);
4    string s2;
```

```
5
       char ch;
6
       while ((ch = ss.get()) != EOF) {
7
           if (ch == ' ') continue;
           if (isdigit(ch)) s2 += ch;
8
9
           else {
               if (s2.back() != ' ') s2 += ' ';
10
11
               s2 += ch;
               s2 += ' ';
12
13
           }
14
       }
15
       return s2;
16
17
   // 中缀表达式转后缀表达式
18
  string convert(const string& s1) {
       unordered_map<char, int> rank{
20
21
           {'+', 2}, {'-', 2}, {'*', 1}, {'/', 1}, {'^', 0}};
22
       stringstream ss(s1);
23
       string s2, temp;
24
       stack<char> op;
25
       while (ss >> temp) {
26
           if (isdigit(temp[0])) s2 += temp + ' ';
           else if (temp[0] == '(') op.push('(');
27
28
           else if (temp[0] == ')') {
29
               while (op.top() != '(') {
30
                   s2 += op.top();
                   s2 += ' ';
31
32
                   op.pop();
33
               }
34
               op.pop();
35
           } else {
               while (!op.empty() && op.top() != '(' &&
36
                       (temp[0] != '^' && rank[op.top()] <= rank[temp[0]] ||</pre>
37
38
                        rank[op.top()] < rank[temp[0]])) {</pre>
39
                   s2 += op.top();
                   s2 += ' ';
40
41
                   op.pop();
42
43
               op.push(temp[0]);
44
           }
45
46
       while (!op.empty()) {
47
           s2 += op.top();
           s2 += ' ';
48
49
           op.pop();
50
51
       return s2;
52
53
  // 计算后缀表达式
54
55 int calc(const string& s) {
56
       stack<int> num;
```

```
57
       stringstream ss(s);
58
       string temp;
59
       while (ss >> temp) {
60
           if (isdigit(temp[0])) num.push(stoi(temp));
61
           else {
62
               int b = num.top();
63
               num.pop();
64
               int a = num.top();
65
               num.pop();
               if (temp[0] == '+') a += b;
66
               else if (temp[0] == '-') a -= b;
67
               else if (temp[0] == '*') a *= b;
68
               else if (temp[0] == '/') a /= b;
69
               else if (temp[0] == '^') a = ksm(a, b);
70
71
               num.push(a);
72
           }
73
74
       return num.top();
75 }
```

6.5 日期

```
l int month[] = {0, 31, 28, 31, 30, 31, 30, 31, 30, 31, 30, 31};
  int pre[13];
3
  vector<int> leap;
 4
  struct Date {
5
       int y, m, d;
6
       bool operator<(const Date& other) const {</pre>
7
           return array<int, 3>{y, m, d} <</pre>
8
                  array<int, 3>{other.y, other.m, other.d};
9
       }
10
       Date(const string& s) {
11
           stringstream ss(s);
12
           char ch;
13
           ss >> y >> ch >> m >> ch >> d;
14
15
       int dis() const {
16
           int yd = (y - 1) * 365 +
17
                     (upper_bound(leap.begin(), leap.end(), y - 1) - leap.begin());
18
19
               pre[m - 1] + (m > 2 && (y % 4 == 0 && y % 100 || y % 400 == 0));
20
           return yd + md + d;
21
22
       int dis(const Date& other) const { return other.dis() - dis(); }
23 };
  for (int i = 1; i <= 12; i++) pre[i] = pre[i - 1] + month[2];</pre>
24
25
  for (int i = 1; i <= 1000000; i++)
26
       if (i % 4 == 0 && i % 100 || i % 400 == 0) leap.push_back(i);
```

6.6 对拍

linux/Mac

```
g++ a.cpp -o program/a -02 -std=c++17
  g++ b.cpp -o program/b -02 -std=c++17
  g++ suiji.cpp -o program/suiji -02 -std=c++17
 5
  cnt=0
6
7
  while true; do
 8
      let cnt++
9
       echo TEST:$cnt
10
       ./program/suiji > in
11
12
       ./program/a < in > out.a
13
       ./program/b < in > out.b
14
15
       diff out.a out.b
16
       if [ $? -ne 0 ]; then break; fi
17
  done
```

windows

```
@echo off
 1
2
3 g++ a.cpp -o program/a -02 -std=c++17
  g++ b.cpp -o program/b -02 -std=c++17
  g++ suiji.cpp -o program/suiji -O2 -std=c++17
7
  set cnt=0
8
9
  :again
10
       set /a cnt=cnt+1
       echo TEST:%cnt%
11
12
       .\program\suiji > in
13
       .\program\a < in > out.a
       .\program\b < in > out.b
14
15
16
      fc output.a output.b
  if not errorlevel 1 goto again
```

6.7 编译常用选项

```
1 -Wall -Woverflow -Wextra -Wpedantic -Wfloat-equal -Wshadow -fsanitize=address,undefined
```

6.8 开栈

不同的编译器可能命令不一样

```
1 -Wl,--stack=0x10000000
2 -Wl,-stack_size -Wl,0x10000000
3 -Wl,-z,stack-size=0x10000000
```

6.9 clang-format

```
BasedOnStyle: Google
IndentWidth: 4
ColumnLimit: 80
4 AllowShortIfStatementsOnASingleLine: AllIfsAndElse
5 AccessModifierOffset: -4
EmptyLineBeforeAccessModifier: Leave
7 RemoveBracesLLVM: true
```