

Security in Cyber Physical System

Tutorial # 1

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1. What are the mathematical properties that are used for the secure exchange of keys (hint: in terms of symmetry equivalence etc.)?

Ans: For symmetry equivalence during the key exchange we have the followings a generator number g , a large prime number n , the two exchanging parties have two private keys a, b .

The goal is to establish a secret key that's same for both the parties (symmetric key exchange).

Suppose Alice is a party that has private key a , Bob is another party who has private key b . Alice will compute $g^a \bmod n$. Bob will compute $g^b \bmod n$. These two can be exchanged via public non-encrypted channel because finding what is a from $g^a \bmod n$ is computationally extremely hard.

Now Alice has $g^b \bmod n$, multiplying with $g^a \bmod n$, Alice will get $g^{ab} \bmod n$. Similarly Bob will multiply $g^a \bmod n$ with $g^b \bmod n$, then Bob will get $g^{ab} \bmod n$.

Now this number $g^{ab} \bmod n$ is a secret value that is not in the public domain and can not be derived from all the variables available in the public domain. Thus giving us a symmetric key $g^{ab} \bmod n$.

So the properties are following

- Given a function f , and two keys a, b , and some operation op , $f(a) \text{ op } f(b) = f(b) \text{ op } f(a)$
- f^{-1} is not easy to calculate.

2. Discuss how the above function can be used as your algorithm for the secure exchange of keys.

Ans: Suppose I've one function f and have the following properties

- Given a function f , and two keys a, b , and some operation op , $f(a) \text{ op } f(b) = f(b) \text{ op } f(a)$
- f^{-1} is not easy to calculate.

Now our key-exchange algorithm would be the following

Algorithm 1: KEY-EXCHANGE ALGORITHM

Input: Private variable a for Alice and variable b for Bob, and one suitable operation OP

- 1 Calculate $f(a)$ from Alice's end.
 - 2 Calculate $f(b)$ from Bob's end.
 - 3 Exchange $f(a)$ and $f(b)$ with each other
 - 4 Use $f(a)$ OP $f(b)$ as the symmetric key for encryption.
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