

Double Hashing → 2 Hash functions

$m=10$
Value = 50, 75, 99, 20, 35, 88, 45, 23, 55, 67

$$\rightarrow DH(v, i) = (\underline{hf_1(v)} + i \underline{hf_2(v)}) \% m$$

$$hf_2(v) = 1 + v \% (m-1)$$

$$hf_1(v) = v \% m$$

$$hf_1(v) = 50 \% 10 = 0$$

$$DH(50, 0) = (0 + 0) \% 10 = 0$$

$$hf_1(75) = 75 \% 10 = 5$$

$$DH(75, 0) = (5 + 0) \% 10 = 5$$

$$hf_1(99) = 99 \% 10 = 9$$

$$DH(99, 0) = (9 + 0) \% 10 = 9$$

$$hf_1(20) = 20 \% 10 = 0$$

$$DH(20, 0) = (0 + 0) \% 10 = 0$$

$$DH(20, 1) = (0 + 1 \times$$

$$hf_2(20) = 1 + 20 \% 8$$

$$= 1 + 4$$

$$= 5$$

Hash Table	
key	value
0	50
1	45
2	
3	35
4	
5	75
6	
7	
8	88
9	99

$$DH(20, 2) = (0 + 2 \times 5) \% 10$$

$$= (0 + 10) \% 10$$

$$= 0$$

$$hf_1(20) = 0$$

$$hf_2(20) = 5$$

$$\underline{\underline{(0, 5)}}$$

$$DH(20, 3) = (0 + 3 \times 5) \% 10 \\ = 5$$

$$hf_1(35) = 35 \% 10 = 5, hf_2(35) = 1 + 35 \% 8$$

$$DH(35, 0) = (5 + 0) \% 10 = 5$$

$$= 1 + 3 \\ = 4$$

$$DH(35, 1) = (5 + 1 \times 4) \% 10 = 9$$

$$DH(35, 2) = (5 + 2 \times 4) \% 10$$

$$13 \% 10 = 3$$

$$hf_1(88) = 88 \% 10 = 8$$

$$DH(88, 0) = (8 + 0) \% 10 = 8$$

$$hf_1(45) = 45 \% 10 = 5, hf_2(45) = 1 +$$

$$DH(45, 0) = (5 + 0) \% 10$$

$$= 5$$

$$45 \% 8$$

$$= 1 + 5$$

$$= 6$$

$$DH(45, 1) = (5 + 1 \times 6) \% 10$$

$$= 11 \% 10 = 1$$

(23, 55, 67) — Hash Table

Note

1) Space is available \rightarrow but still not able to insert all the elements

\hookrightarrow inside hash table

2) $\left. \begin{array}{l} \text{Search} \\ \text{Delete} \\ \text{Insertion} \end{array} \right\} \begin{array}{l} \text{Best case} \rightarrow O(1) \\ \text{Worst case} \rightarrow O(n) \end{array}$

3) Not using any extra space outside the hash table.