

## Binary Search

↳ Divide & conquer

1) Sorted array

0 1 2 3 4 5 6 7  
arr = [2, 4, 8, 12, 20, 25, 50, 70]  
↑  
x = 50

i = 0

J = 7

small problem → single element

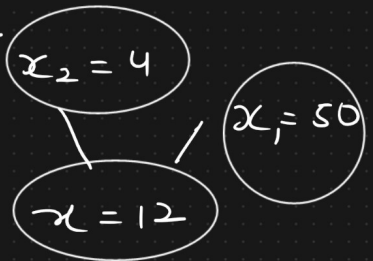
x = 50 ← [50] / only one condition  
if arr[i] == x :  
return i  
return -1

Big Problem →

overflow

$$\text{mid} \Rightarrow (i + j) // 2 = (0 + 7) // 2 = 3$$

✓  
$$\Rightarrow i + (j - i) // 2$$
$$(0 + 7) // 2 = 3$$



0 1 2 3 4 5 6 7  
[2, 4, 8, 12, 20, 25, 50, 70] → Sorted

BinarySearch(arr, 0, 7, x)  
1. mid = 3

i <= j

BinarySearch(arr, i, j, x)

2. arr[mid] == x :

return mid

Pseudocode

12 < 50  
arr[mid] < x

Recursion

BinarySearch(arr, mid + 1, j, x)

OR

$$i = \text{mid} + 1$$

$$12 > 4$$

$\text{arr}(\text{mid}) > x$  — Recursion

Binary Search (arr, i, mid-1, x)

OR

$$j = \text{mid} - 1$$

return -1