

## Divide & conquer

n is large  $\longrightarrow$  Big  $\longrightarrow$  Divide & conquer

n is small  $\longrightarrow$  small  $\longrightarrow$  return solution

$\hookrightarrow$  size of elements

Recursion  $\longrightarrow$  calling the function itself  
 $\downarrow$  directly or indirectly

Recursive  
tree

$\longrightarrow$  Recurrence Relation

- $\hookrightarrow$  1) substitution
- 2) Recursive tree
- 3) Master's Theorem

Time  
Complexity

### Pseudocode

arr  $\rightarrow$  array, p  $\rightarrow$  lower index, q  $\rightarrow$  higher index  
(len(arr)-1)

$T(n) \rightarrow$  divideAndConquer(arr, p, q):

$c \rightarrow \begin{cases} \text{if small(arr, p, q):} \\ \text{return solution} \end{cases}$

else:

Divide - ①

$c \rightarrow \text{mid} = \text{Divide}(\text{arr}, p, q) \quad T(n/2)$

conquer  $\rightarrow \begin{cases} b = \text{divideAndConquer}(\text{arr}, p, \text{mid}) \\ c = \text{divideAndConquer}(\text{arr}, \text{mid}+1, q) \end{cases}$

②

$\text{return combine}(b, c) \rightarrow c$   
 $T(n/2)$  Recursion

combine

③

optional

## Recurrence Relation

$$T(n) = 2T(n/2) + c$$

$$T(n) = aT(n/b) + f(n)$$

Binary Search

$$T(n) = T(n/2) + c$$

Quick Sort

$$T(n) = 2T(n/2) + n$$

find max. element in an array

↳ small problem

$$\underline{n \leq 2}$$

constant

$\left\{ \begin{array}{l} n=1 \rightarrow \text{return arr} \\ n=2 \rightarrow \text{one comparison} \\ \quad \quad \quad \rightarrow \text{return max element} \end{array} \right.$

$$\underline{n > 2}$$

Recursion

$\left\{ \begin{array}{l} \rightarrow \text{Divide \& Conquer} \end{array} \right.$