

Insert( element )

// 1. Create new node

- Make memory for new element, say newNode.
- Store element in newNode's data.
- Set newNode's next and previous to empty.

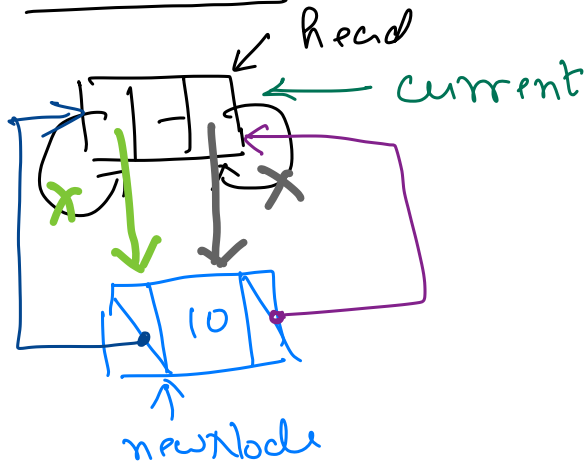
// 3. Traverse list to find node - current node.

- Set current to ~~head~~ (first node). *head's next*
- while (~~current is not empty~~) do *current is not head*
  - if (current node's data > element) then
    - // Found the node, end the traversal.
  - End the traversal.
- Set current to current's next node.

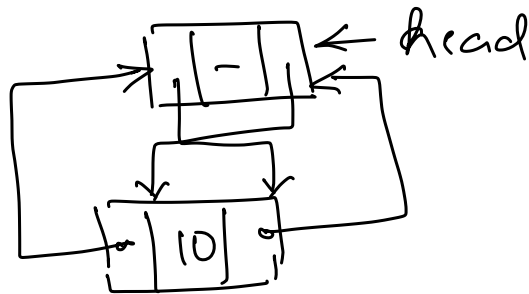
// 6. Add a new node between current and current's previous node.

- Make the current node come after newNode. // Set newNode's next to current.
- Make the current node's previous node come before newNode. // Set newNode's previous to current node's previous.
- Make newNode come after the current node's previous node. // Set current node's previous node's next to newNode.
- Make newNode come before the current node. // Set current node's previous to newNode.
- Stop.

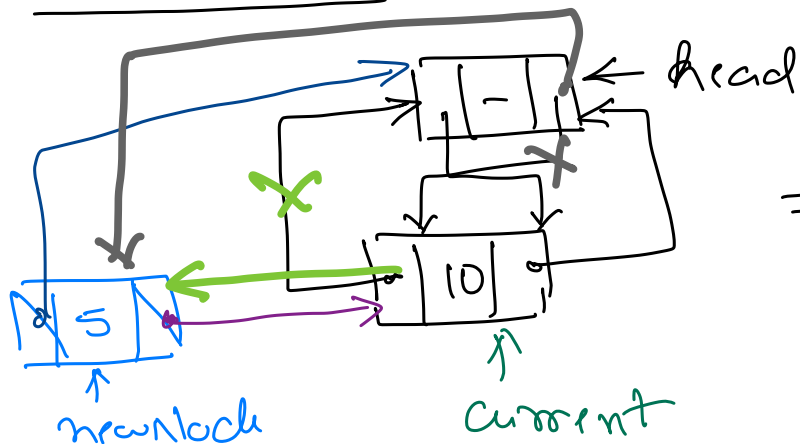
insert (10)



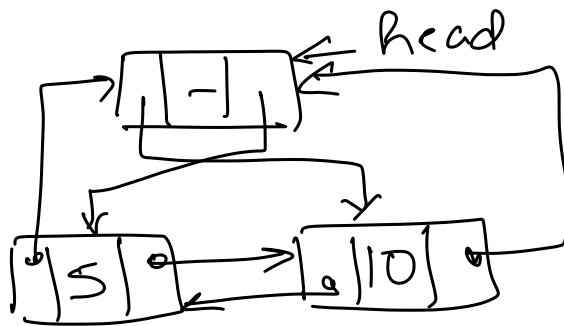
$\Rightarrow$



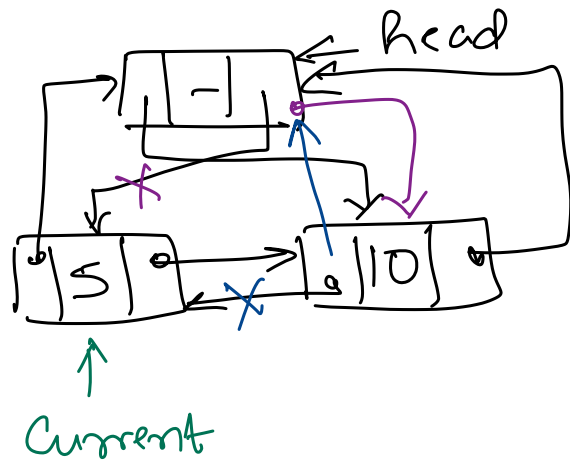
insert (5)



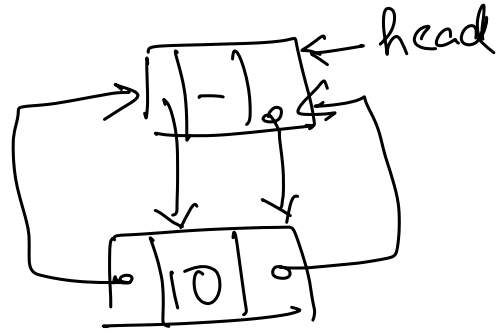
$\Rightarrow$



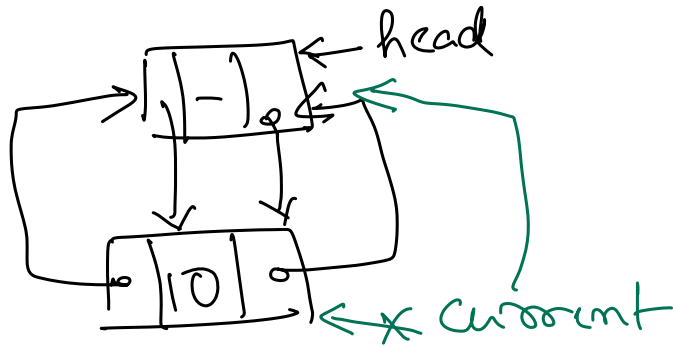
delete (5)



$\Rightarrow$



delete (20)



## Delete (element)

// Find the node to be deleted - current node

- Set current to first node (~~head~~ *head's next*)
- while (current is not ~~empty~~ *head*) do
  - if (current node's data = element) then
    - // Found the node - end the traversal.
    - End the traversal.
  - Move current to current's next node

// Have we found the node to be deleted?

- if (current is ~~empty~~ *head*) then
  - Stop.

- Make current's next node come after current's previous node. // Set current node's previous node's next to current node's next node.

- Make the current node's previous node come before the current node's next node. // Set current's next node's previous to current's previous node.

- Release memory of the current node. (Not required for JAVA).
- Stop.

Iterator  $\rightarrow$  mechanism using which we can access elements stored in a data structure, one by one.

Iterator  $\langle T \rangle$  interface in JAVA.

Iterable  $\langle T \rangle$  interface in JAVA

} Class implementing these interfaces, their object can be used in for each loop.

How to use an array to allocate memory for all nodes for a linked list?

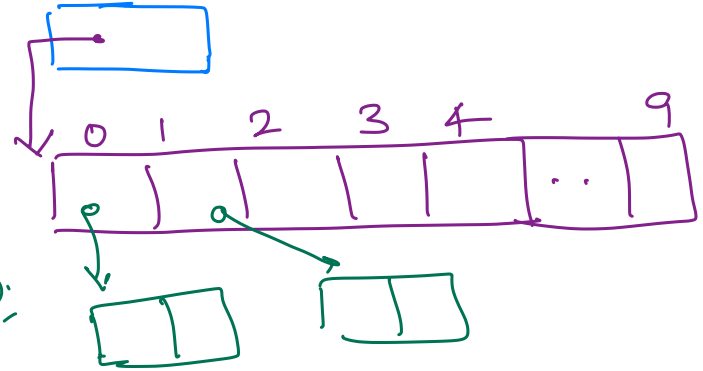
← Object Pooling.

`Node [] nodesPool;`

`nodesPool = new Node[10];`

`for (int i=0; i<10; ++i) {  
 nodesPool[i] = new Node(i);`

`nodesPool`

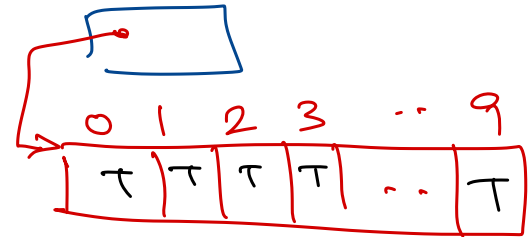


`boolean [] isNodeFree;`

`isNodeFree = new boolean[10];`

`for (int i=0; i<10; ++i)  
 isNodeFree[i] = true;`

`isNodeFree`



class NodePoolManager {

Node createNode();

void deleteNode(Node);

}

NodePoolManager nodePool;

AddAtFront(element) - Optimised

- Make space for new elements, say newNode.
- Store element in newNode's data.
- Set newNode's next to head.
- Set head to newNode.
- if tail is empty then
  - Set tail to head.
- Stop.

→ Node newNode =  
nodePool.createNode();

# Recursion

When the solution of a problem is defined as a solution of a subproblem.

In programming - When a function calls itself.

$$n! = \begin{cases} 1, & \text{if } n = 0 \text{ or } n = 1 \\ n \times (n-1)!, & \text{otherwise.} \end{cases}$$

base case.

```
int factorial ( int n ) {  
    if ( (n == 0) || (n == 1) ) } terminating  
        return 1; condition.  
    return n * factorial (n-1);  
}
```



Direct vs Indirect recursion.

Infinite recursion and terminating condition/base case.

```
... f1() {  
    :  
    f1(); ← direct  
    :      recursion  
}
```

```
... f2() {  
    :  
    f3();  
    :  
    f2();  
    :  
} ← indirect  
   recursion.
```

```
... f4() {  
    f4(); ← Infinite recursion. ⇒  
    :  
}
```

when recursive  
call is made  
before  
terminating  
condition.

# Divide and Conquer

If a problem can be divided into smaller problems such that, the solution of smaller problems gives us the solution of bigger problem.

DIVIDE - Divide larger problem into smaller problem.

CONQUER - Solve each smaller problem until they are a base case.

COMBINE (Optional) - Combine solution of smaller problems to find solution of larger problem.

## Backtracking

Build solution step by step.

At each step, we discard steps(s) that do not result in a solution.

→ Solve maze.

→ Sudoku

→ 8 queen problem.

→ knight tour.

Multiply two numbers, without using \* operator.

$$\text{multiply}(m, n) = \begin{cases} 0, & \text{if } m=0 \text{ or } n=0 \\ m, & \text{if } n=1 \\ n, & \text{if } m=1 \\ m + \text{multiply}(m, n-1), & \text{otherwise} \end{cases}$$

$m \times n$

$$\Rightarrow \underbrace{m + m + m + \dots + m}_{n \text{ times}} \Rightarrow$$

$$\Rightarrow \underbrace{n + n + n + \dots + n}_{m \text{ times.}}$$

$$m + \underbrace{(m + m + \dots + m)}_{(n-1) \text{ times}}$$

$\downarrow$   
 $m \times (n-1)$

Assignment: Define multiplication for negative numbers.

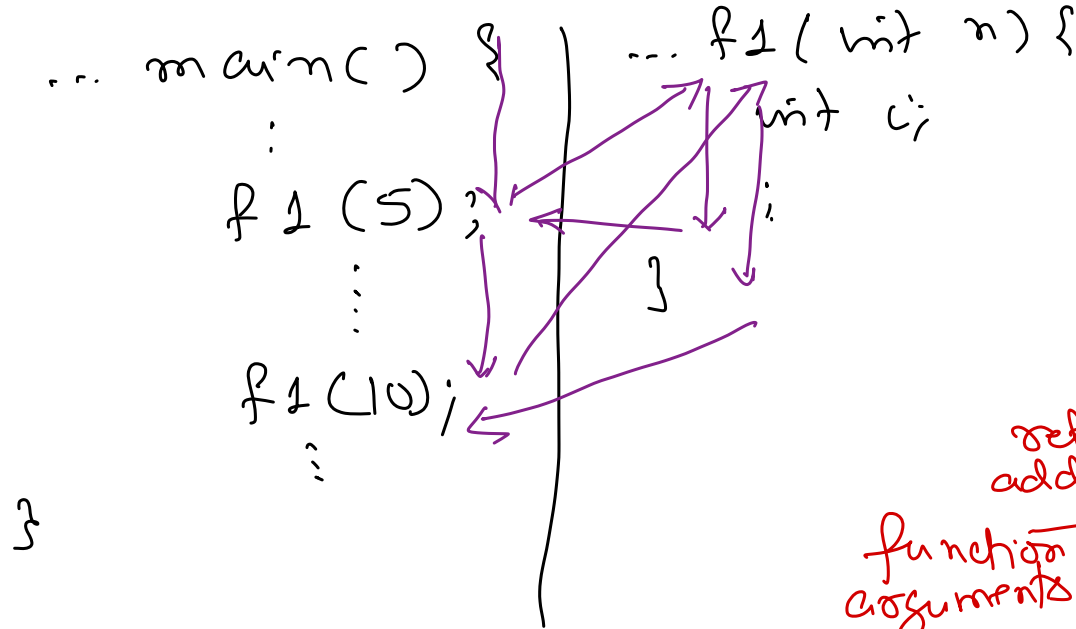
$m=5$

$n=102197$

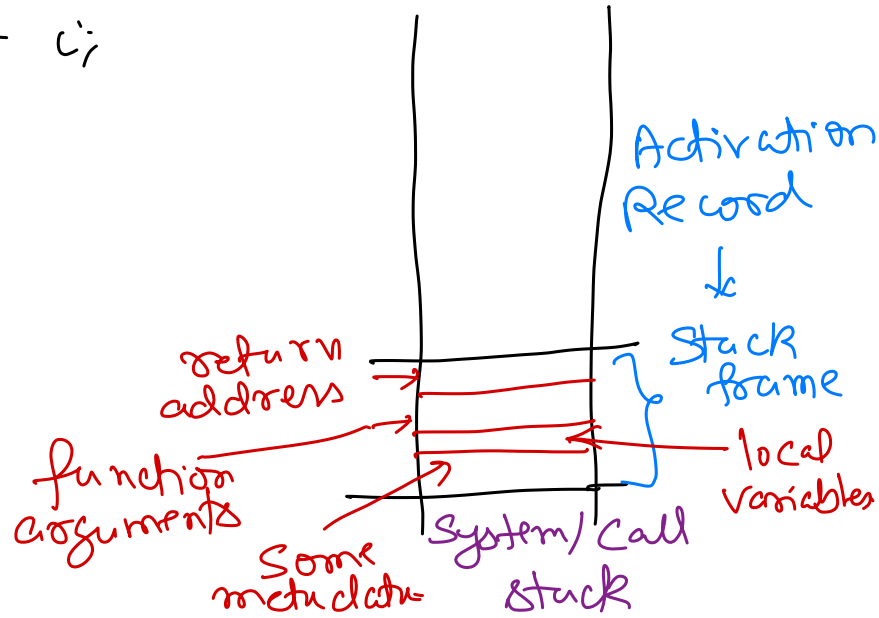
← Handle such scenario efficiently in algorithm.

Assignment: Divide two numbers  
→ give quotient  $\Rightarrow$  QUOTIENT(m,n)  
→ give remainder  $\Rightarrow$  REMAINDER(m,n)

How do function call works



Stack  
(System / call stack)



```

int factorial ( int n ) {
    if ((n==0) || (n==1))
        return 1;

```

```

    return n * factorial (n-1);
}

```

```

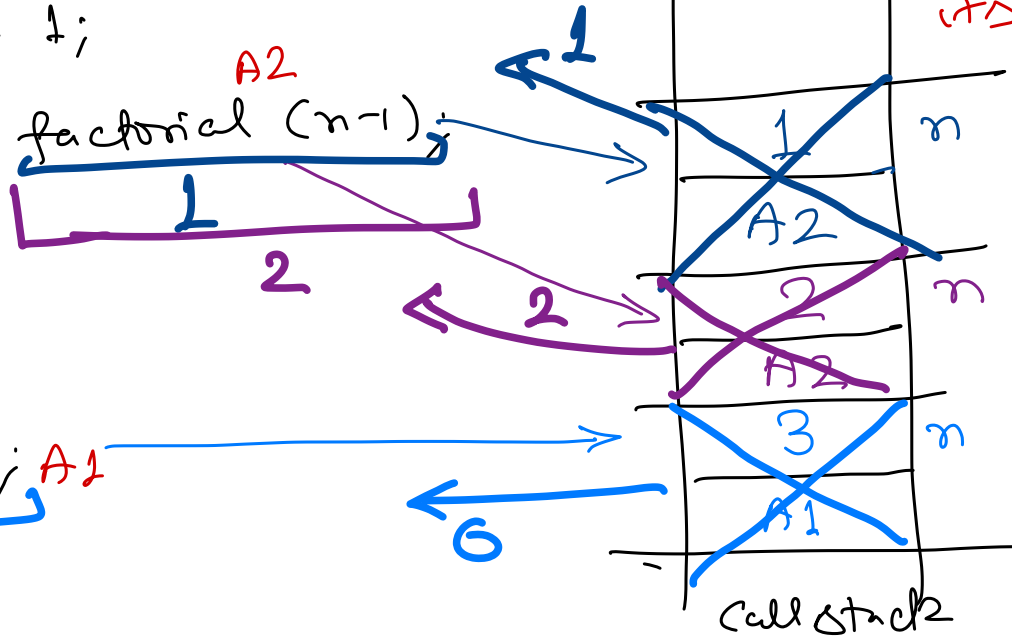
... main() {
    :

```

```

    factorial(3);
    :
}

```



When function call is over, we remove its stack frame from stack  
 ↑  
 Stack unwinding

To return value for function general purpose CPU registers are used.

Calling convention → to invoke function.

↓,

→ in which order function arguments are pushed on stack

→ who cleans up stack frame after function call is over.