

Q.5. a)

i) Prob. that any station can send a frame in the first slot:

$$\begin{aligned} P(\text{success}) &= P(A \text{ only}) + P(B \text{ only}) + P(C \text{ only}) \\ &= P_A \cdot \bar{P}_B \cdot \bar{P}_C + \bar{P}_A \cdot P_B \cdot \bar{P}_C + \bar{P}_A \cdot \bar{P}_B \cdot P_C \\ &= (0.2)(0.7)(0.6) + (0.8)(0.3)(0.6) + (0.8)(0.7)(0.4) \\ &= 0.452 \end{aligned}$$

ii) Prob. that A succeeds for the first time in 2nd slot.

$$P_A^{\text{success}} = P_A \cdot \bar{P}_B \cdot \bar{P}_C = (0.2)(0.7)(0.6) = 0.084$$

$$P_A^{\text{fail}} = 1 - 0.084 = 0.916$$

$$\begin{aligned} P(A \text{ succeeds in 2nd slot for the first time}) &= \frac{0.916 \times 0.084}{0.084} \\ &= 0.076944 \end{aligned}$$

iii) Prob. that C succeeds for the first time in 3rd slot

$$P_C^{\text{success}} = P_C \cdot \bar{P}_A \cdot \bar{P}_B = 0.224$$

$$P_C^{\text{fail}} = 1 - 0.224 = 0.776$$

$$P(C \text{ succeeds in 3rd slot for the first time}) =$$

$$(0.776)^2 \cdot (0.224) = 0.134746$$