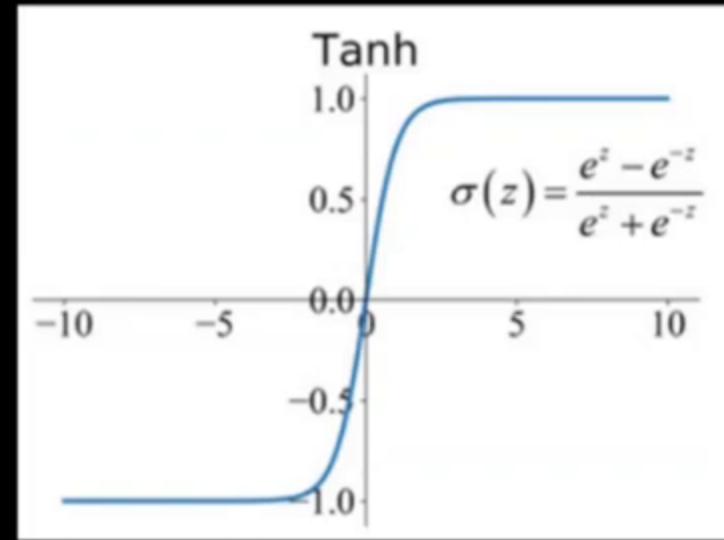


ACTIVATION  
FUNCTIONS



# TANH ACTIVATION



# Tanh Activation

ML For Nerds

# Tanh Activation

ML For Nerds

## Drawbacks of Sigmoid

- Vanishing Gradient
- Not zero-centered
- Only for Binary Classification problems

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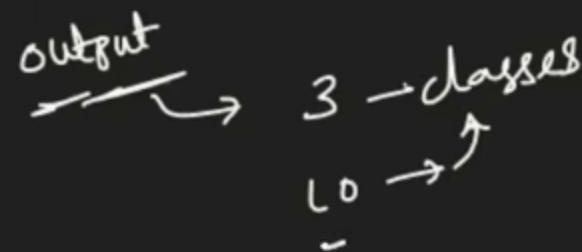
# Drawbacks of Sigmoid

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Output

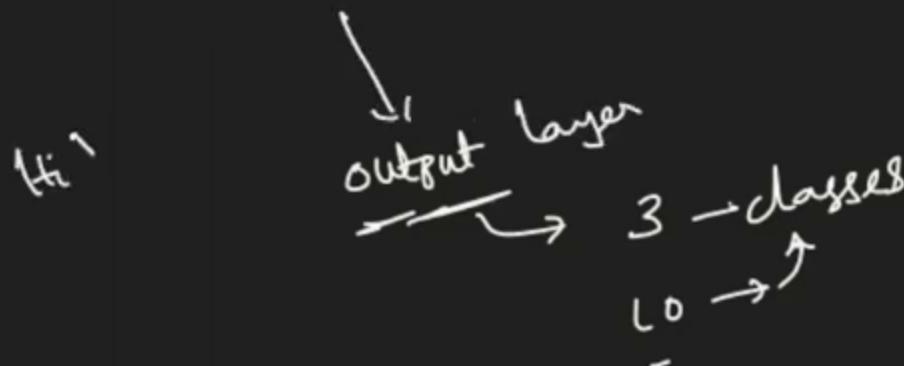
# Drawbacks of Sigmoid

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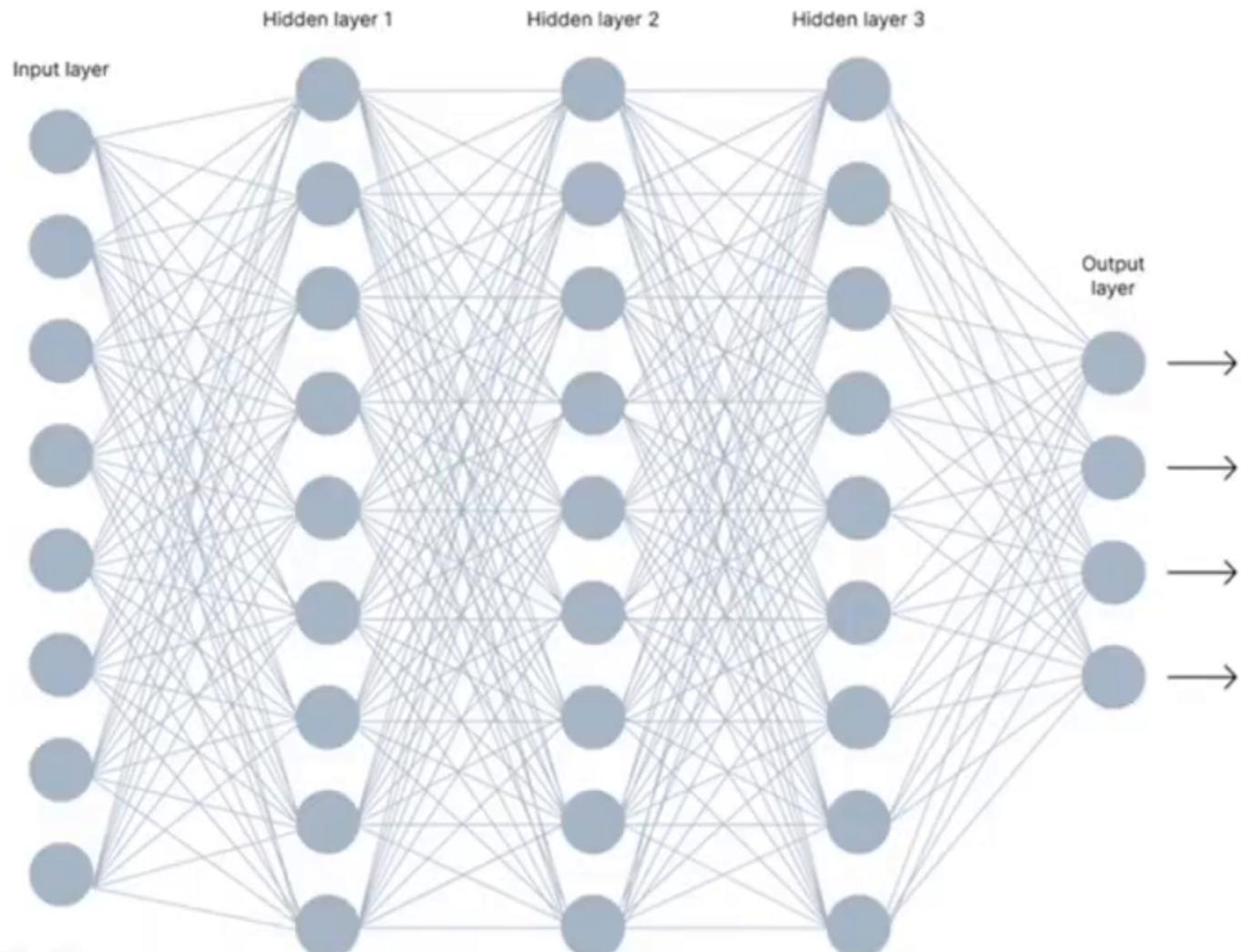


# Drawbacks of Sigmoid

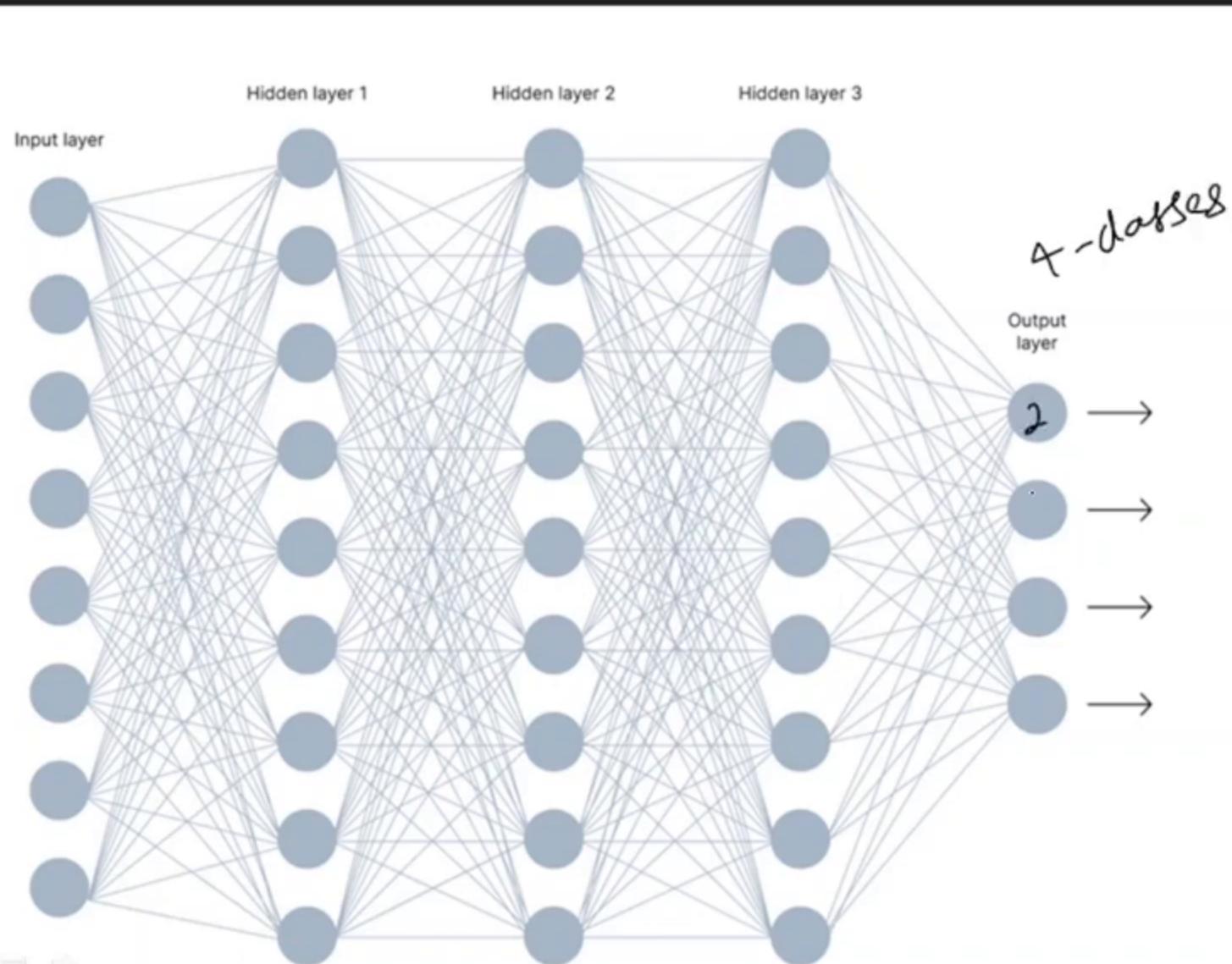
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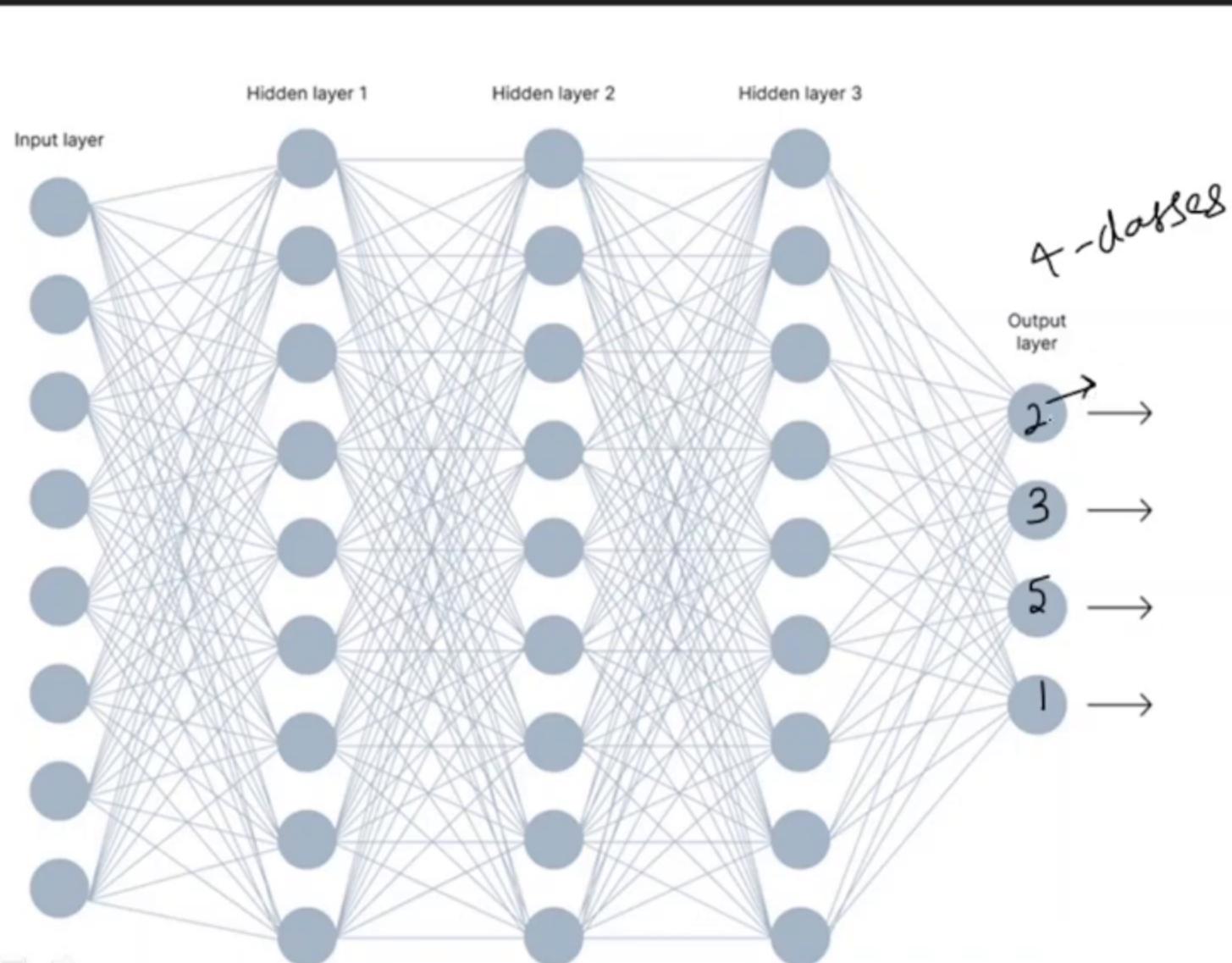
# Multi-class problem



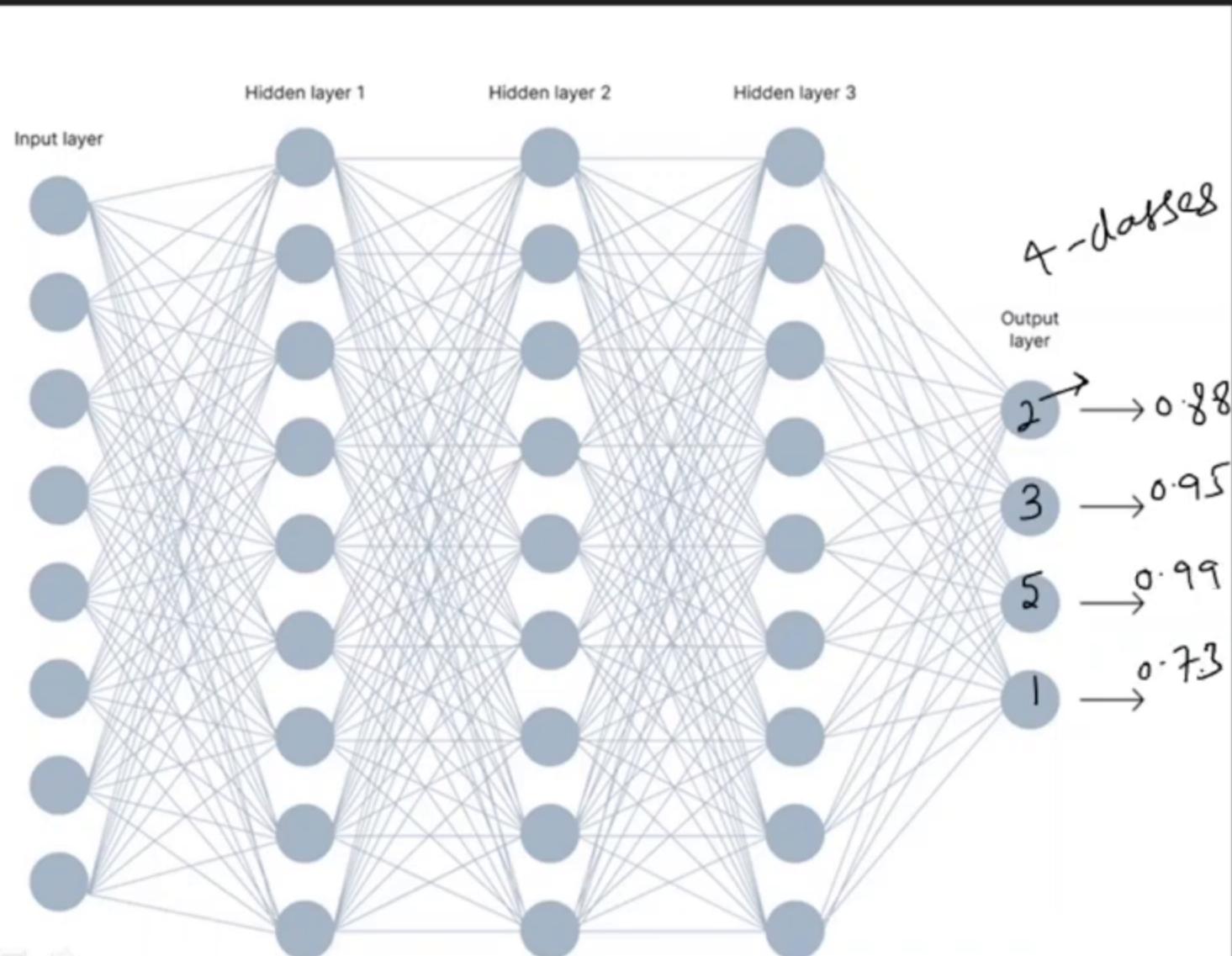
# Multi-class problem



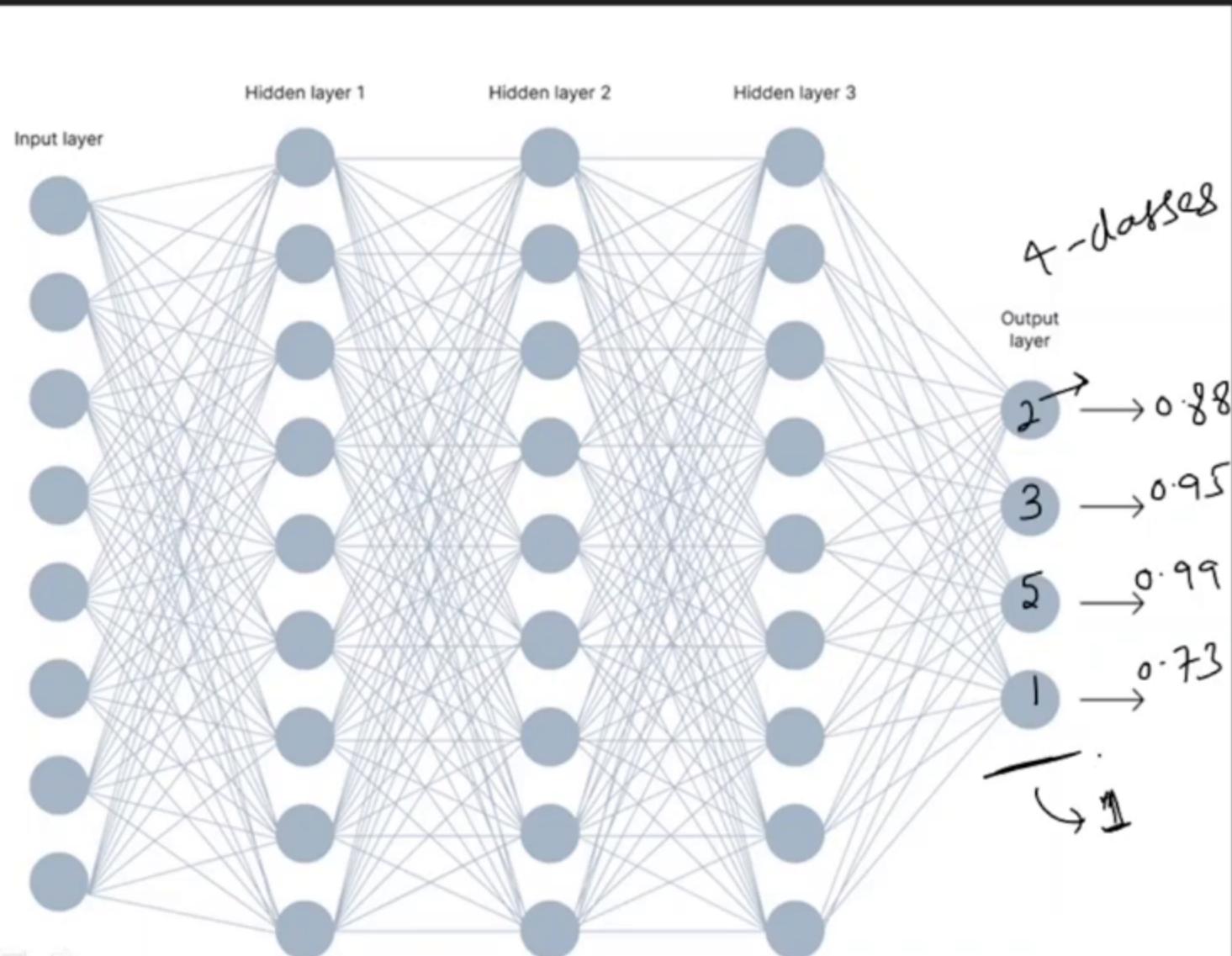
# Multi-class problem



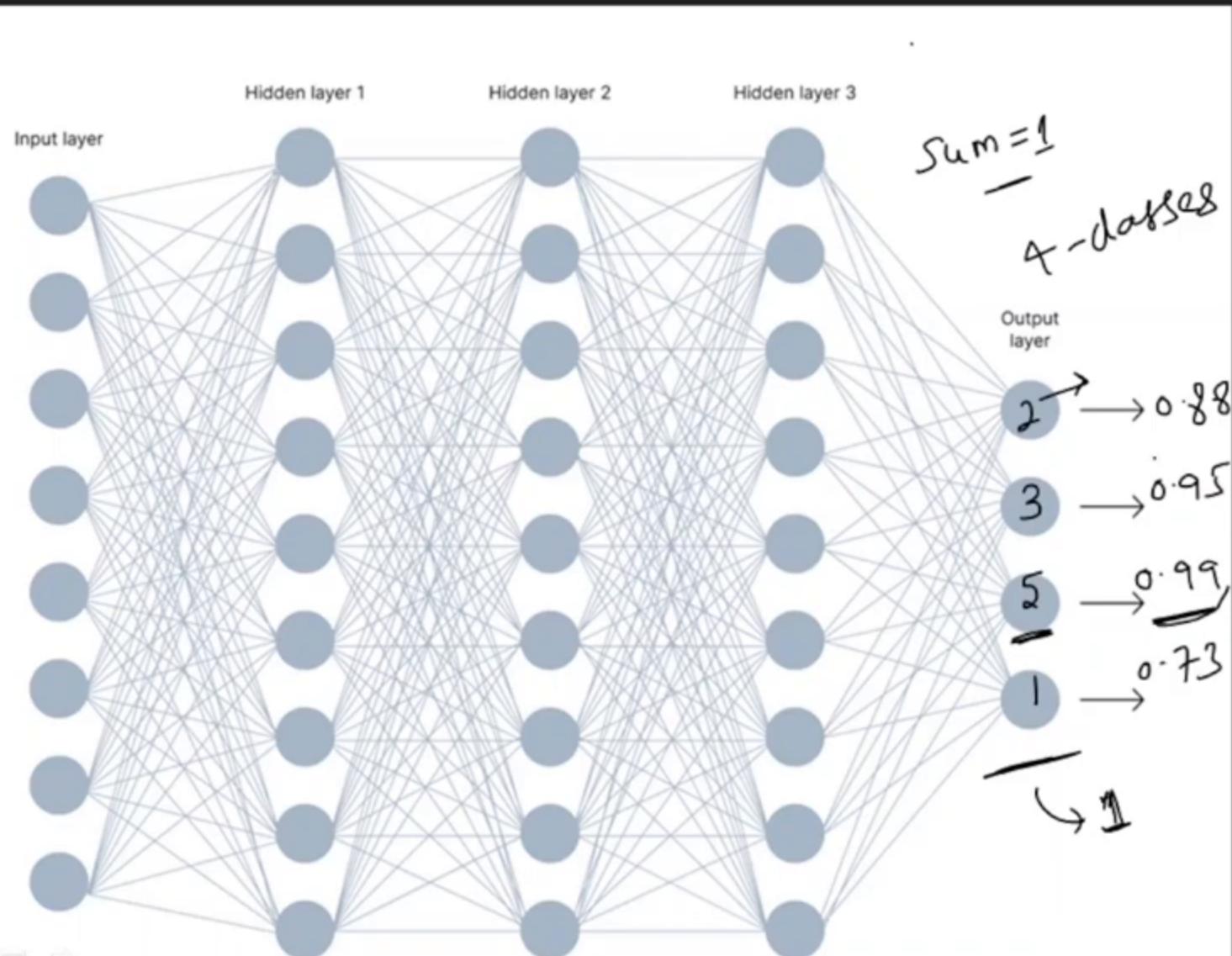
# Multi-class problem



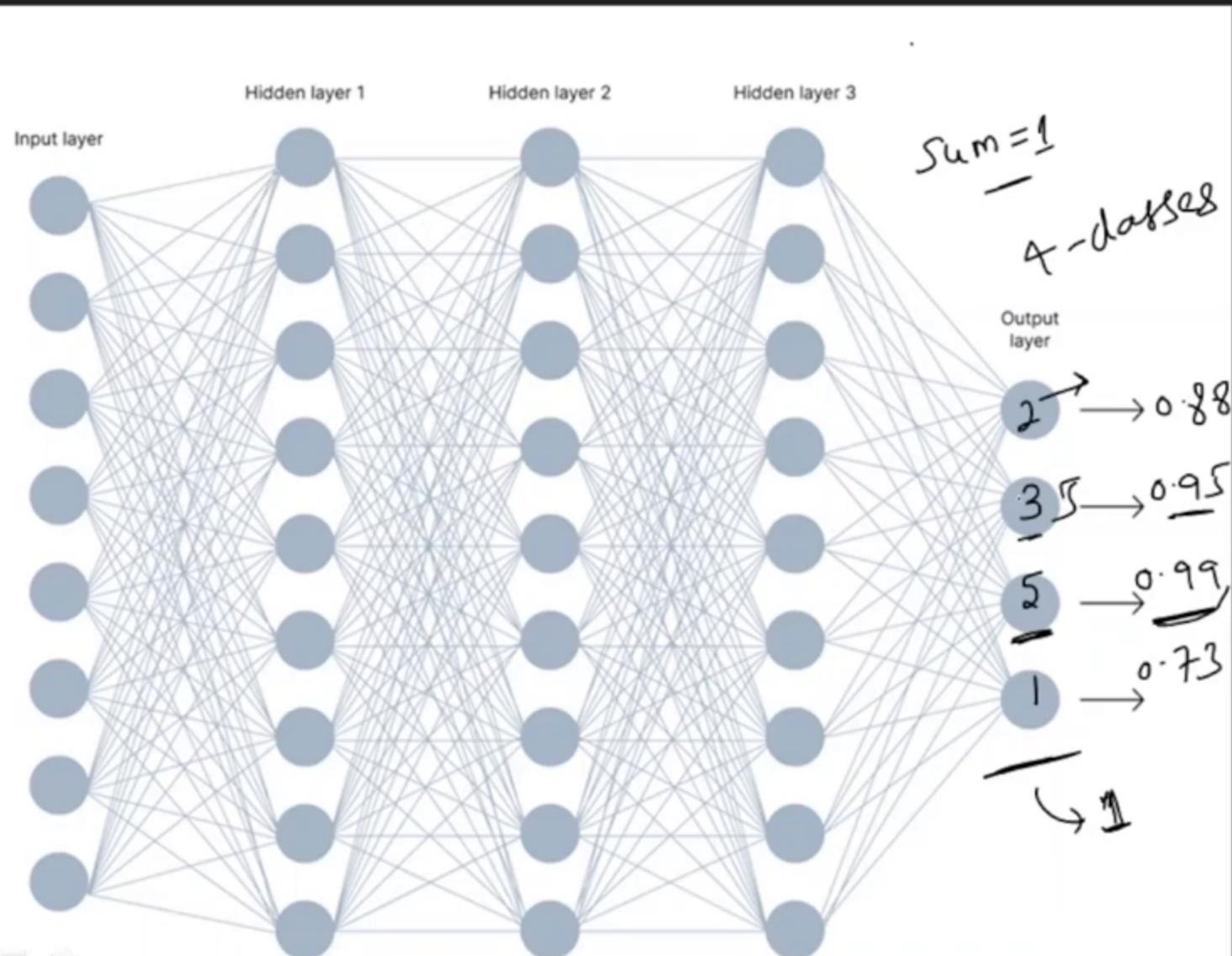
# Multi-class problem



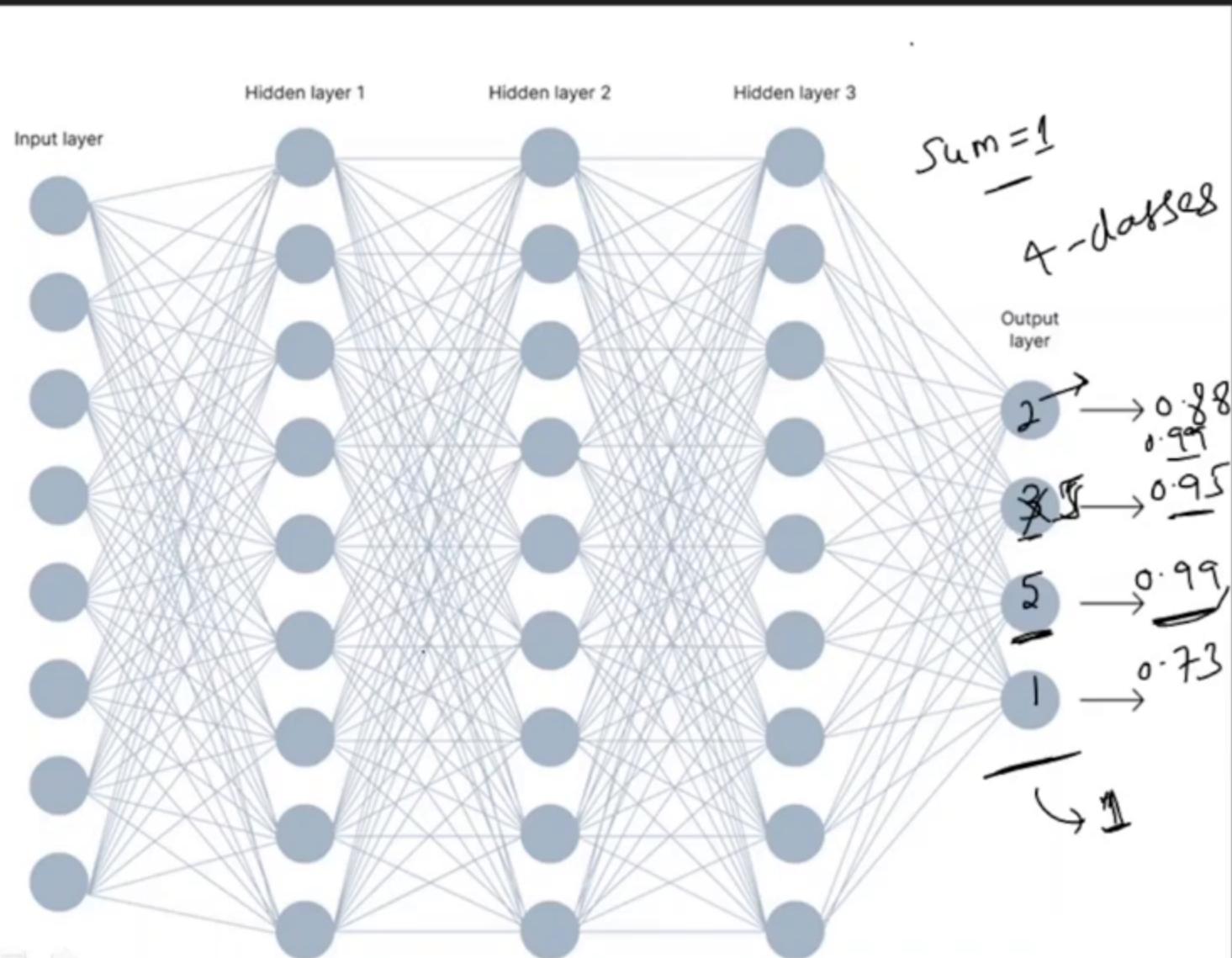
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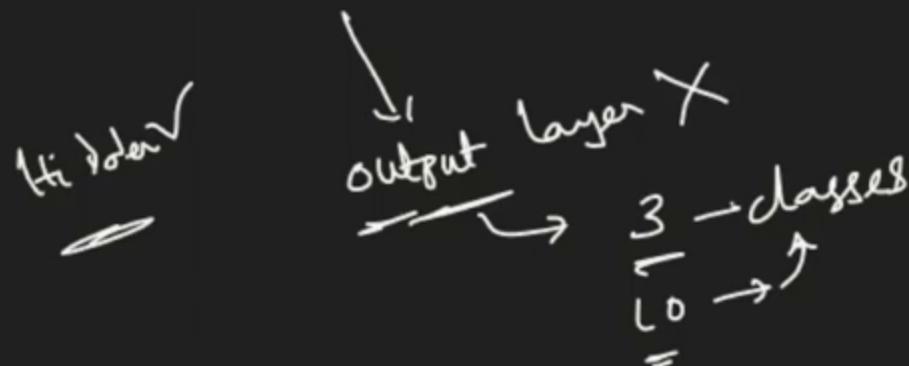


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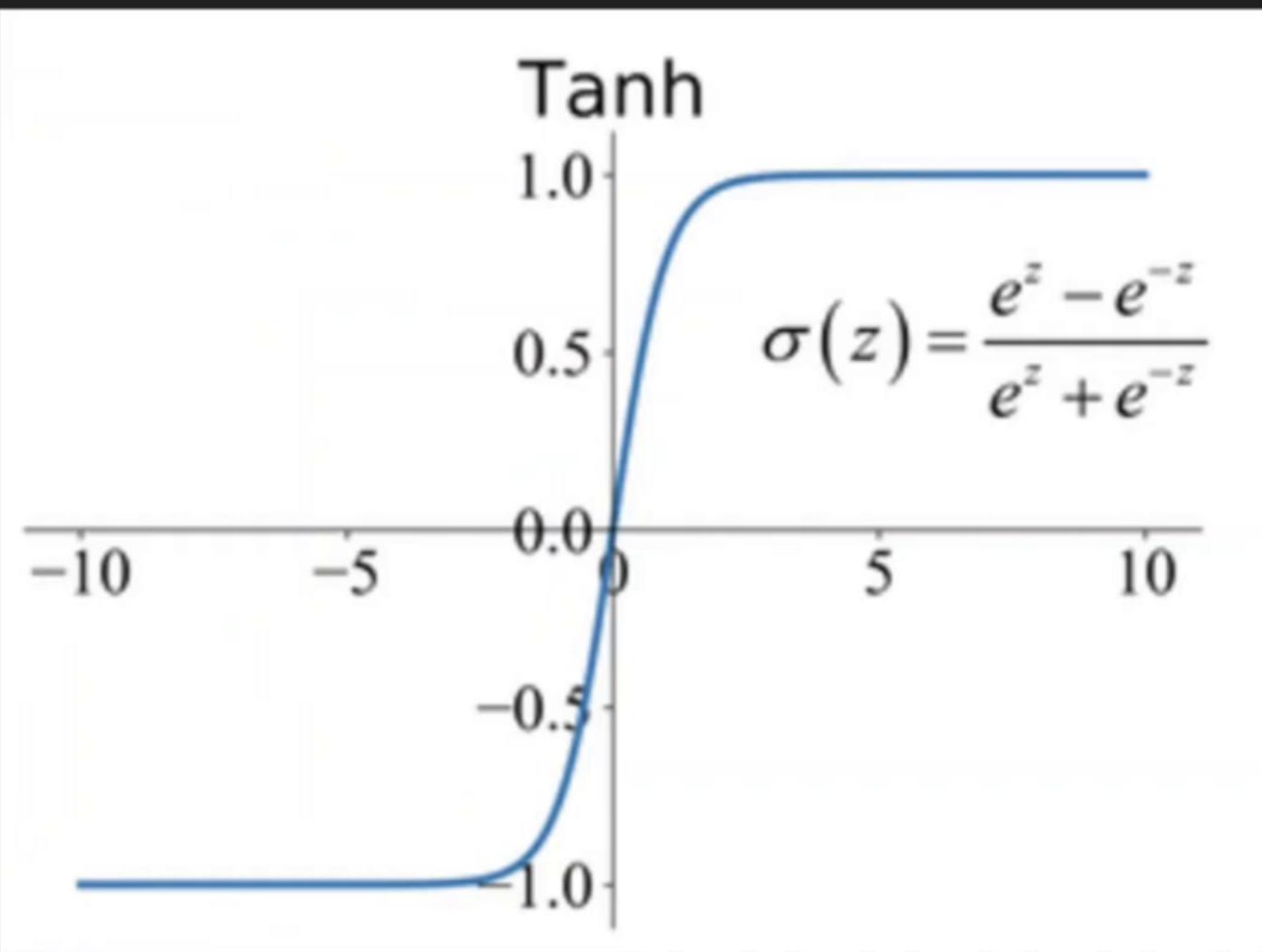
- Vanishing Gradient
- Not zero-centered  $\rightarrow$ .
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## Definition

Tanh Function

$$a = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

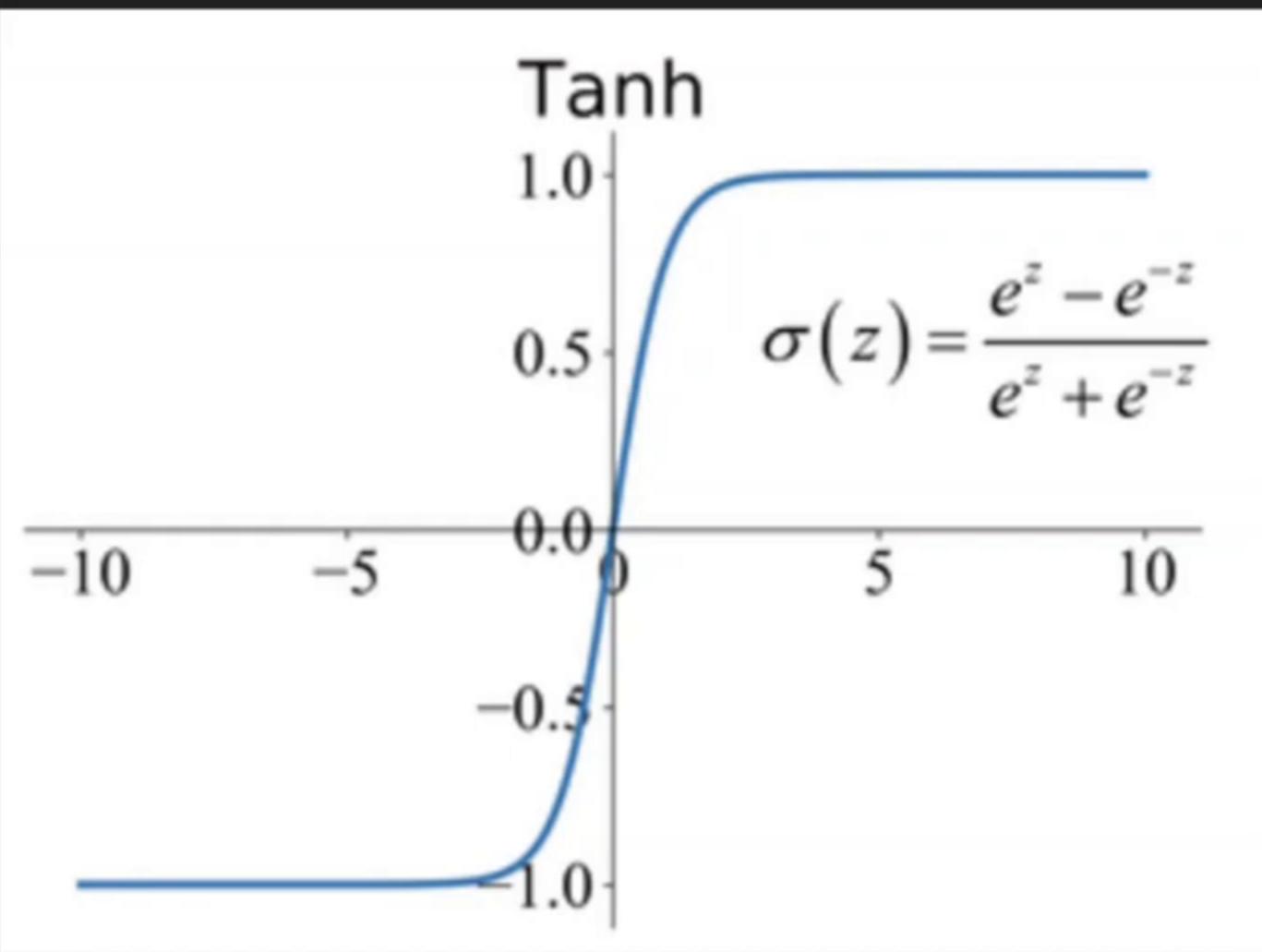


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Tanh Function

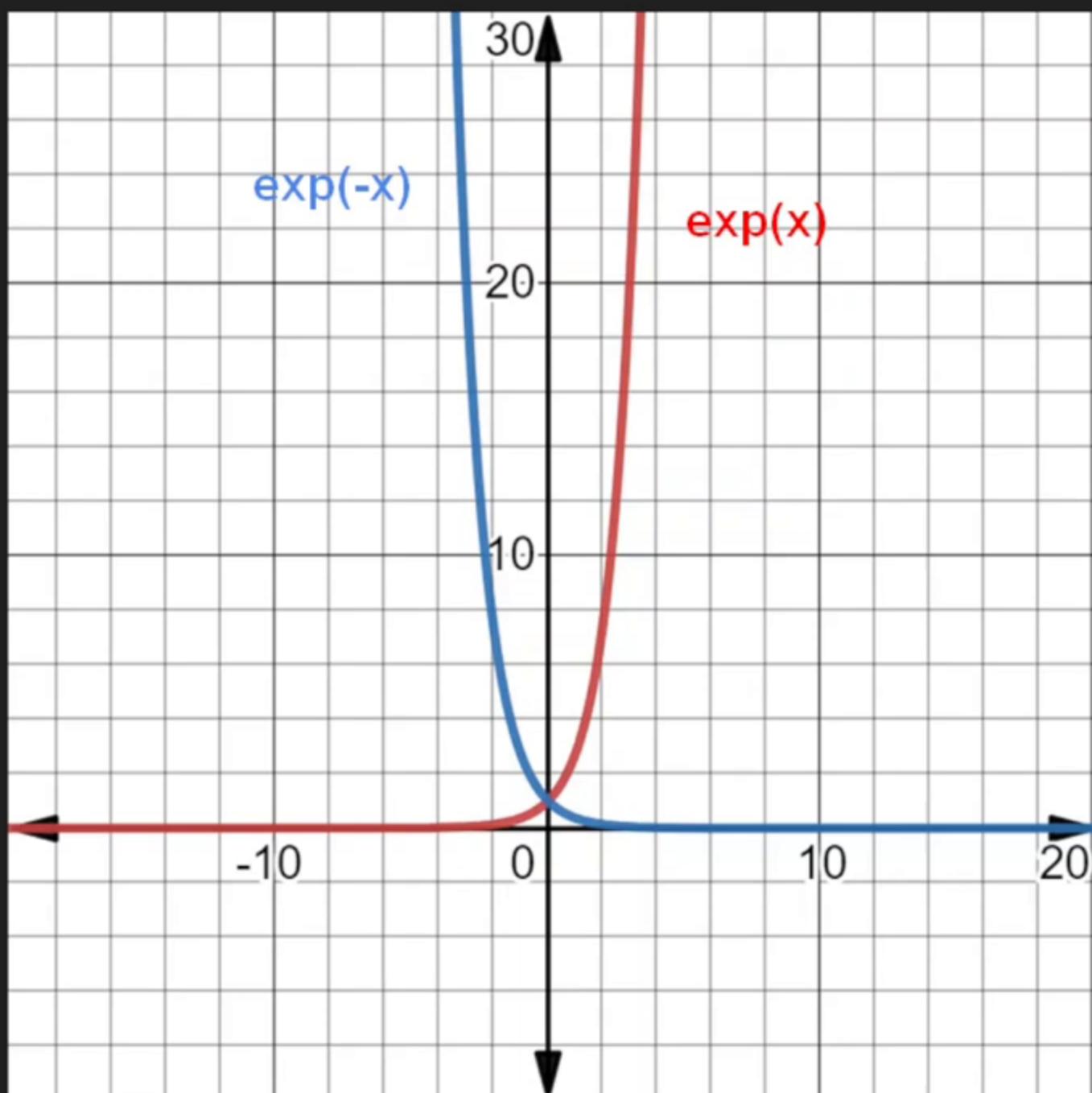
$$a = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

-t .\n



Range  $\rightarrow -1 \leq x \leq 1$

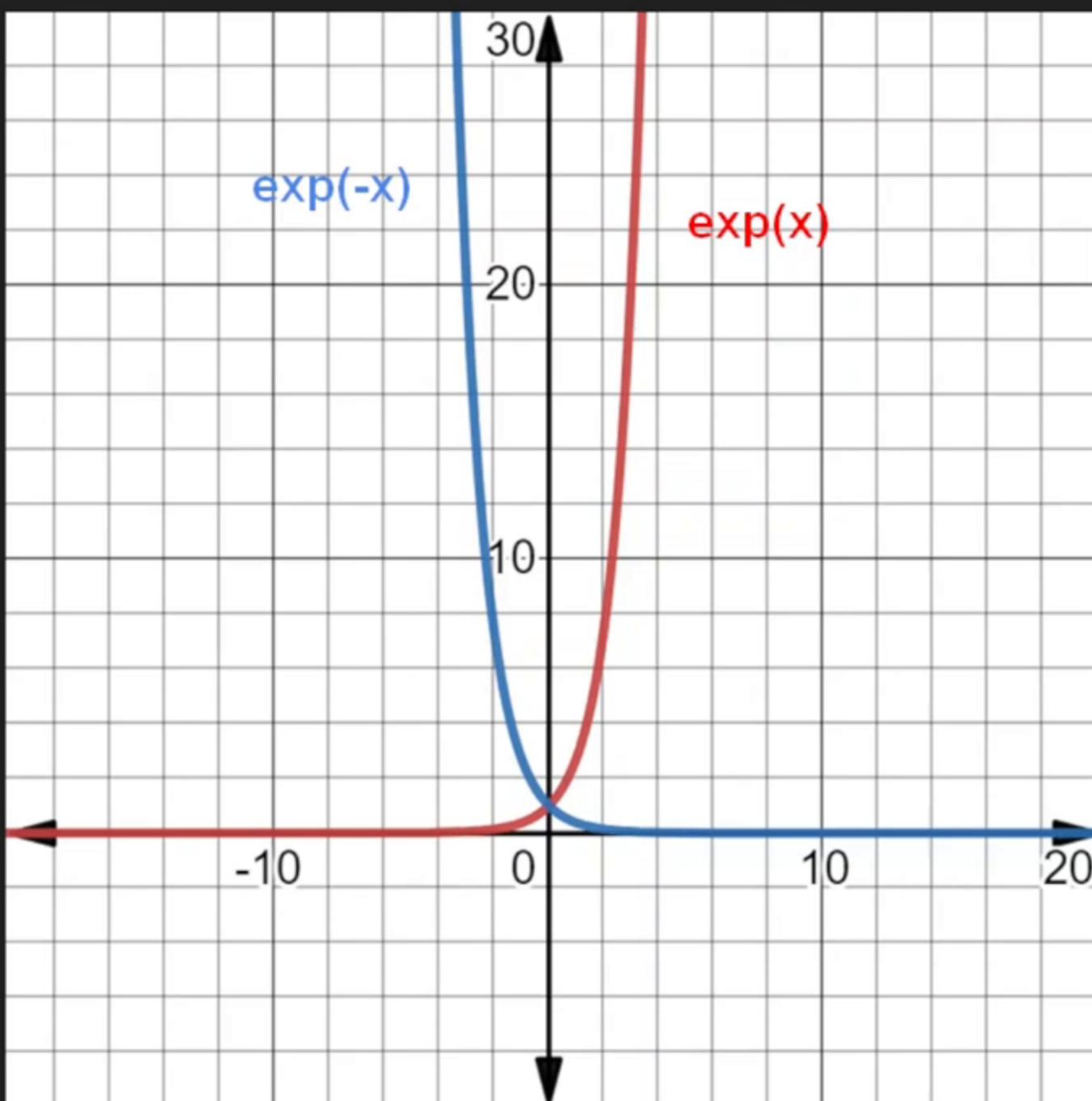
x	-inf	0	inf
$\exp(x)$	0	1	inf
$\exp(-x)$	inf	1	0



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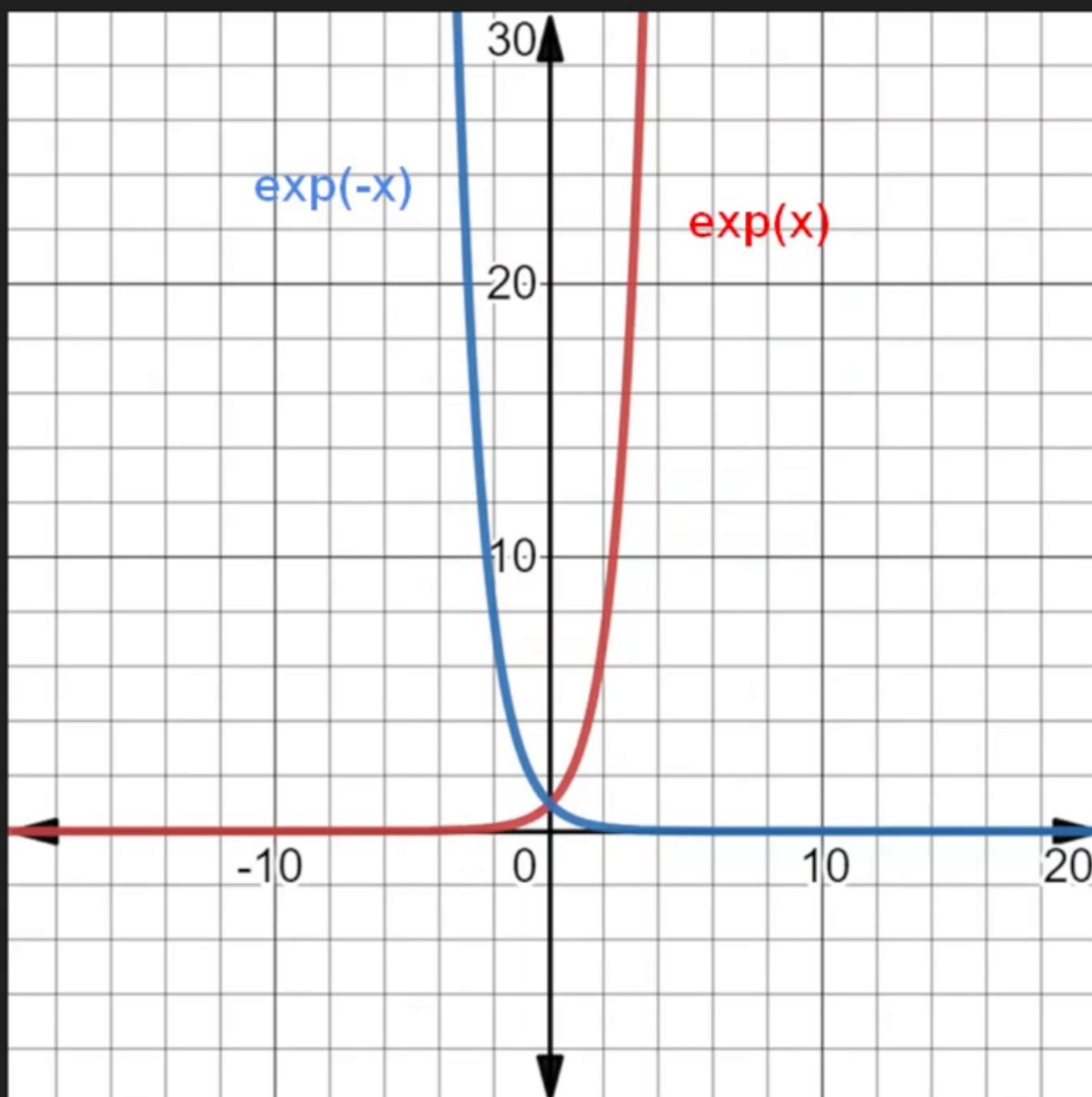
.



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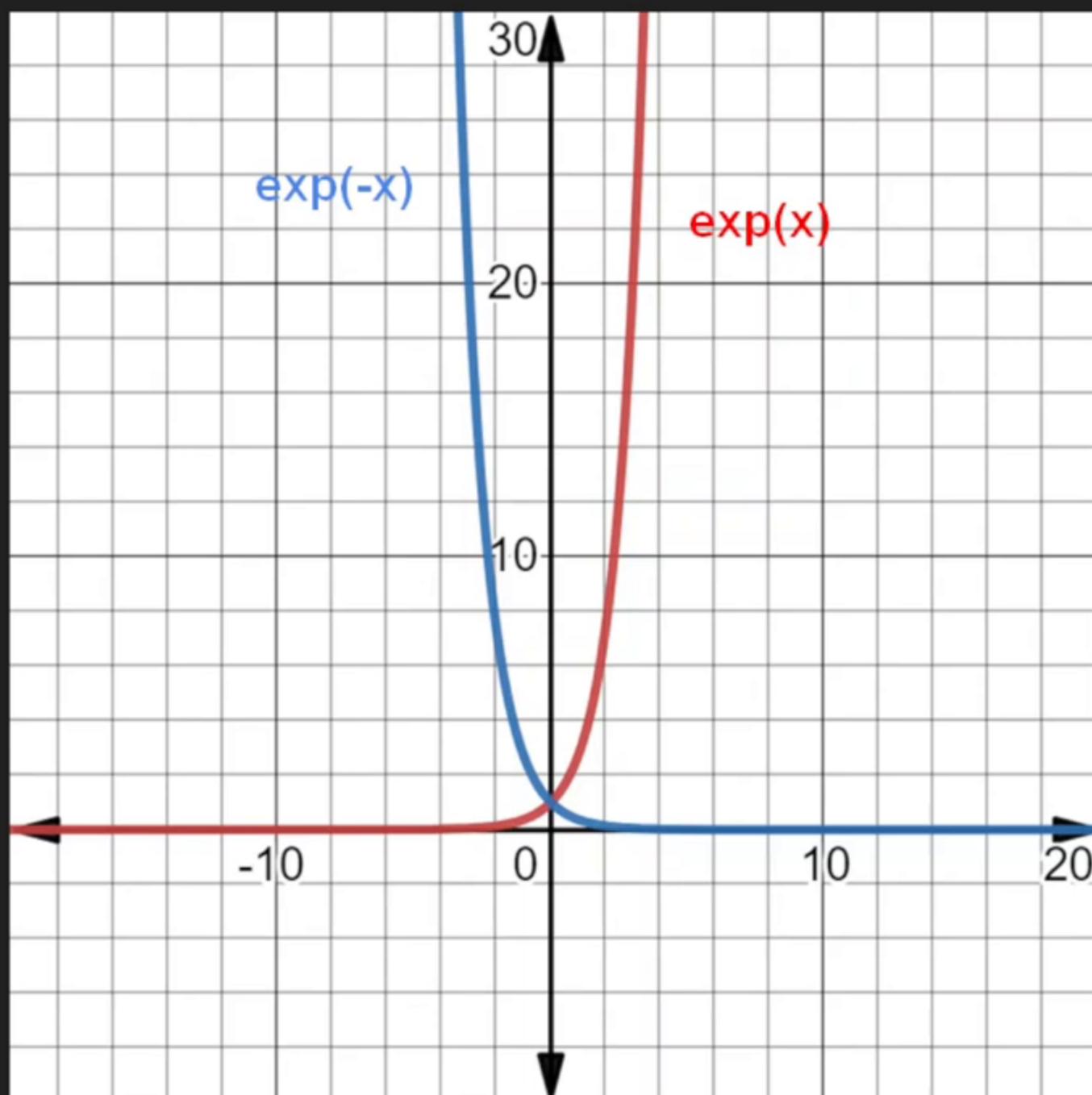
$x = -\infty \rightarrow 0^+$



Range  $\rightarrow -1 \leq x \leq 1$

x	-inf	0	inf
exp(x)	0	1	inf
exp(-x)	inf	1	0

$$x = -\infty \rightarrow \frac{0 - \infty}{0 + \infty} = -1$$



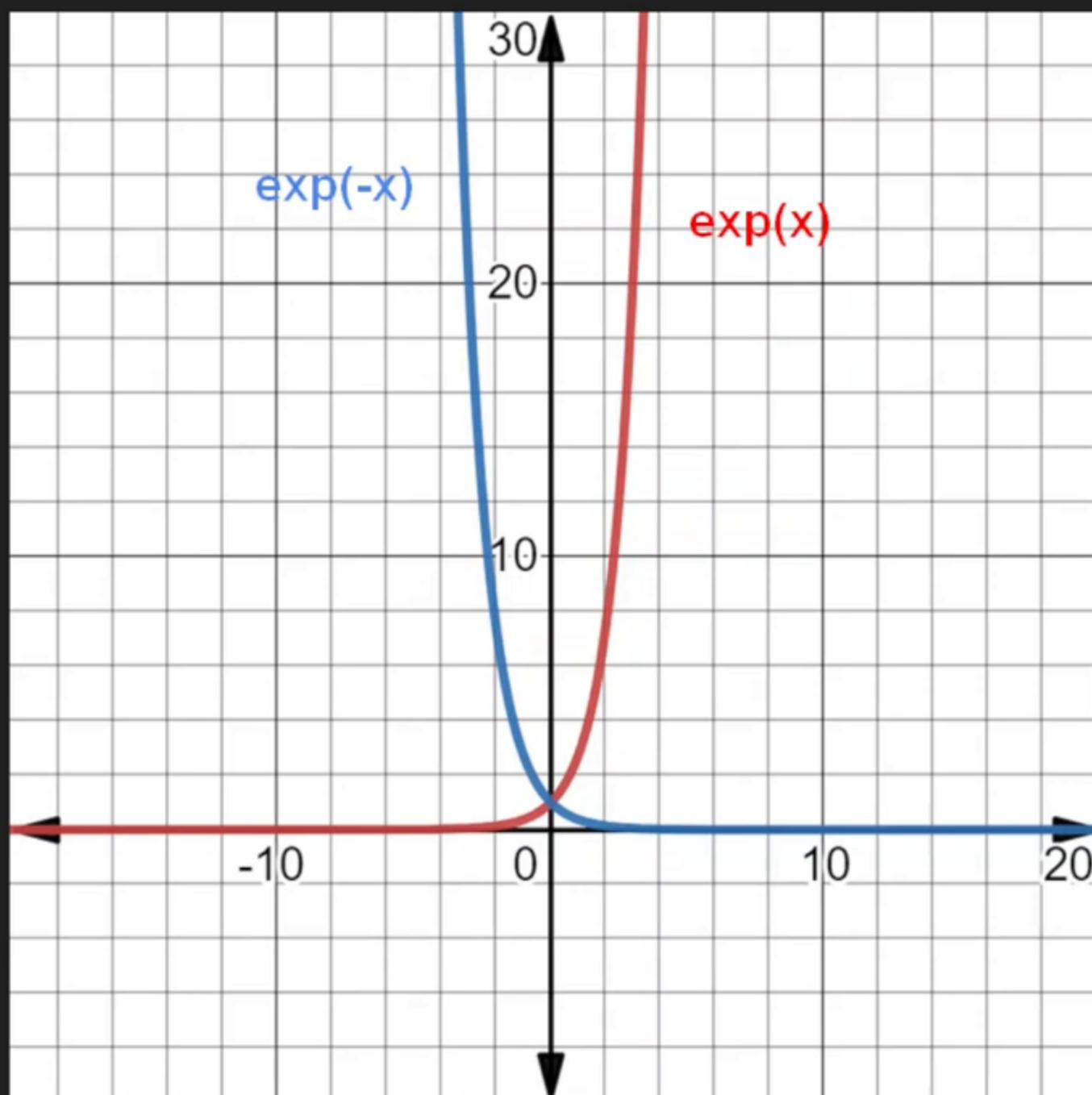
Range  $\rightarrow -1 \leq f(x) \leq 1$

$$\frac{e^x - e^{-x}}{e^x + e^{-x}}$$

x	-inf	0	inf
exp(x)	0	1	inf
exp(-x)	inf	1	0

$$x = -\infty \rightarrow \frac{0 - 0}{0 + \infty} = -1$$

$$x = 0$$



Range  $\rightarrow -1 \leq f(x) \leq 1$

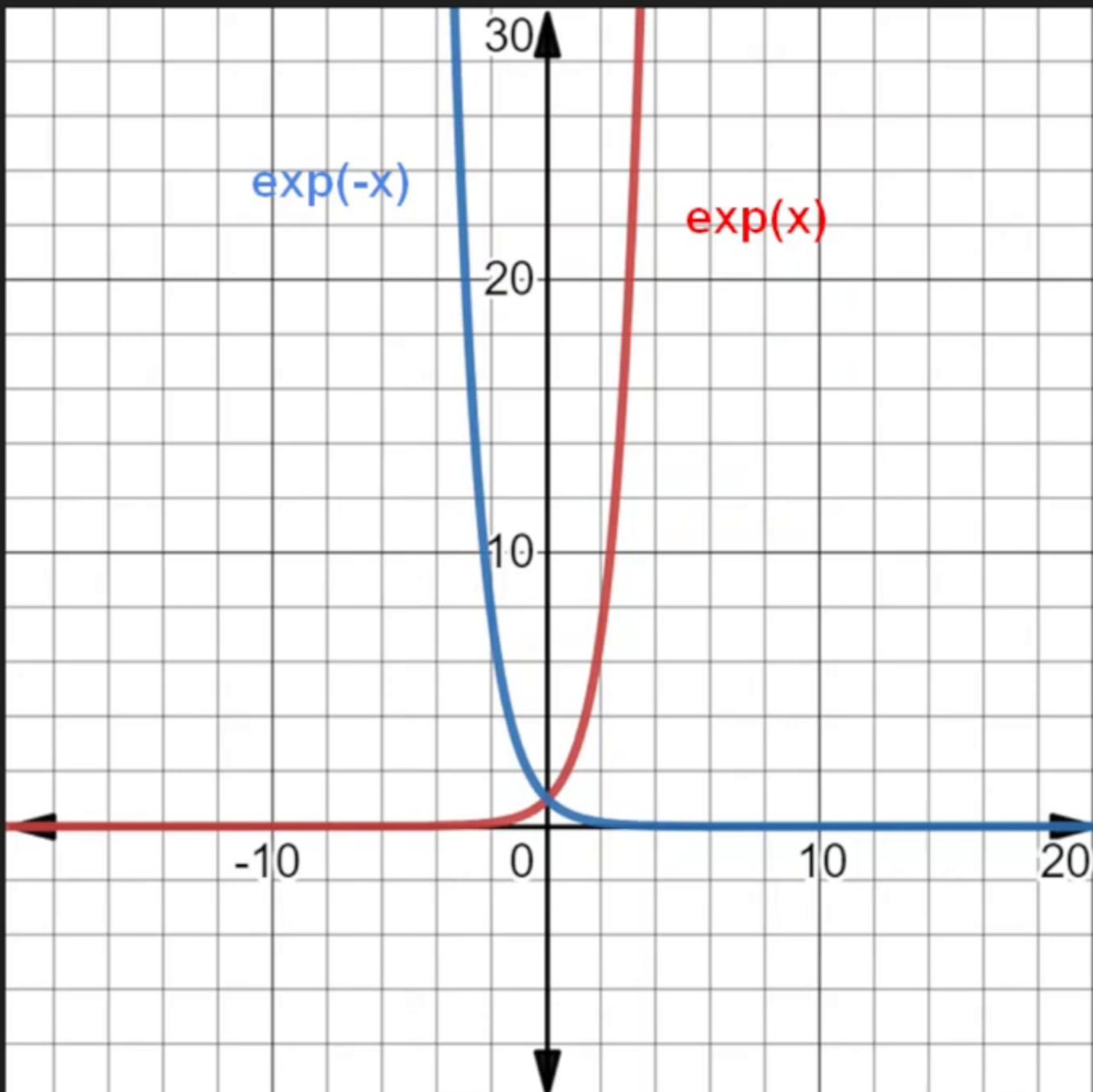
$$\frac{e^x - e^{-x}}{e^x + e^{-x}}$$

x	-inf	0	inf
exp(x)	0	1	inf
exp(-x)	inf	1	0

$$x = -\infty \rightarrow \frac{0 - 0}{0 + \infty} = -1$$

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$$x = \infty \rightarrow$$



Range  $\rightarrow -1 \leq f(x) \leq 1$

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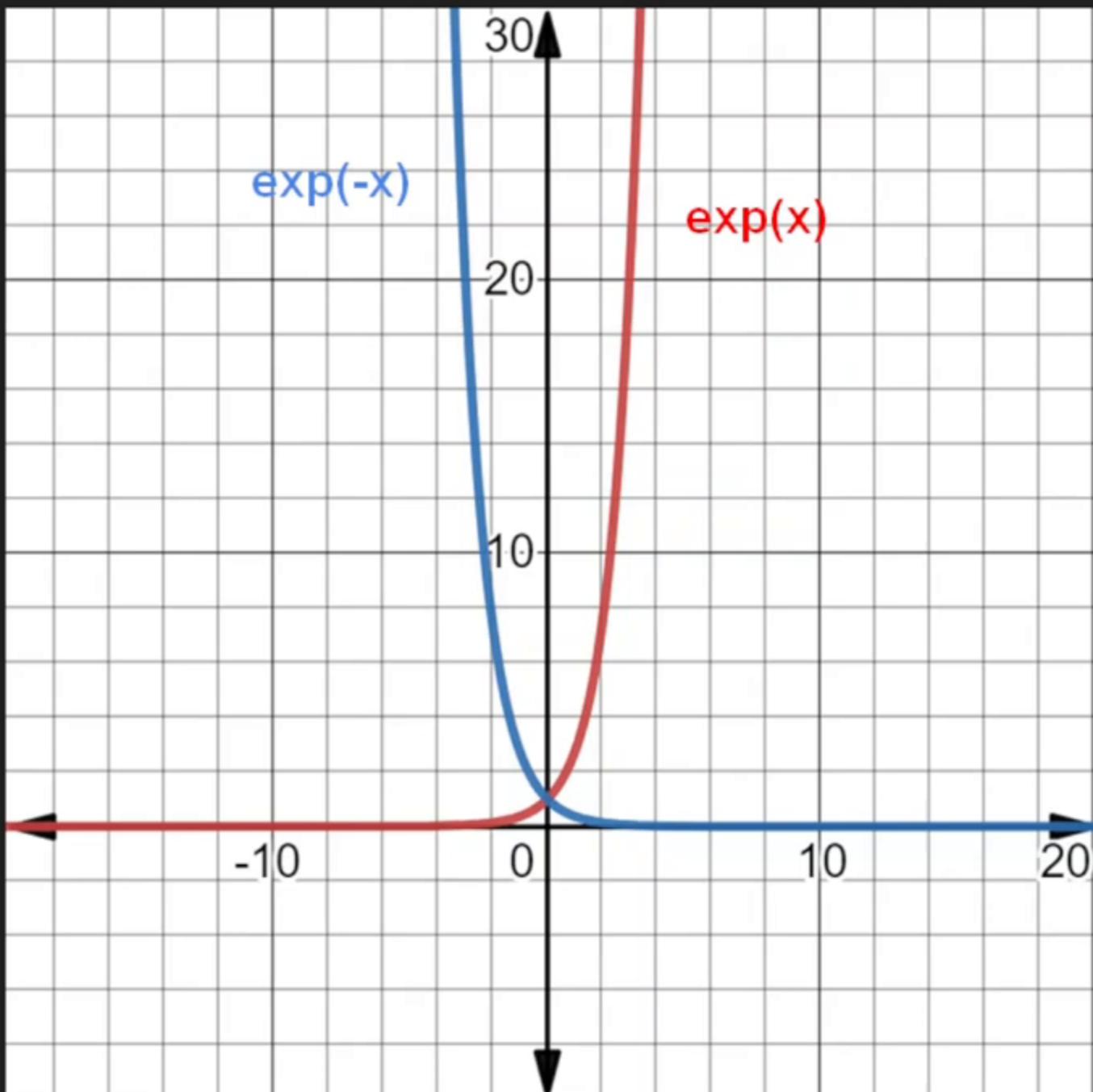
x	-inf	0	inf
exp(x)	0	1	inf
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$$x = -\infty \rightarrow \frac{0 - 0}{0 + \infty} = -1$$

$$x = 0 \rightarrow \frac{1 - 1}{1 + 1} = 0$$

$$x = \infty \rightarrow \frac{\infty - 0}{\infty + 0} = 1$$

.



Range  $\rightarrow -1 \leq \tanh x \leq 1$

$$\tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

x	$-\infty$	0	$\infty$
$\exp(x)$	0	1	$\infty$
$\exp(-x)$	$\infty$	1	0

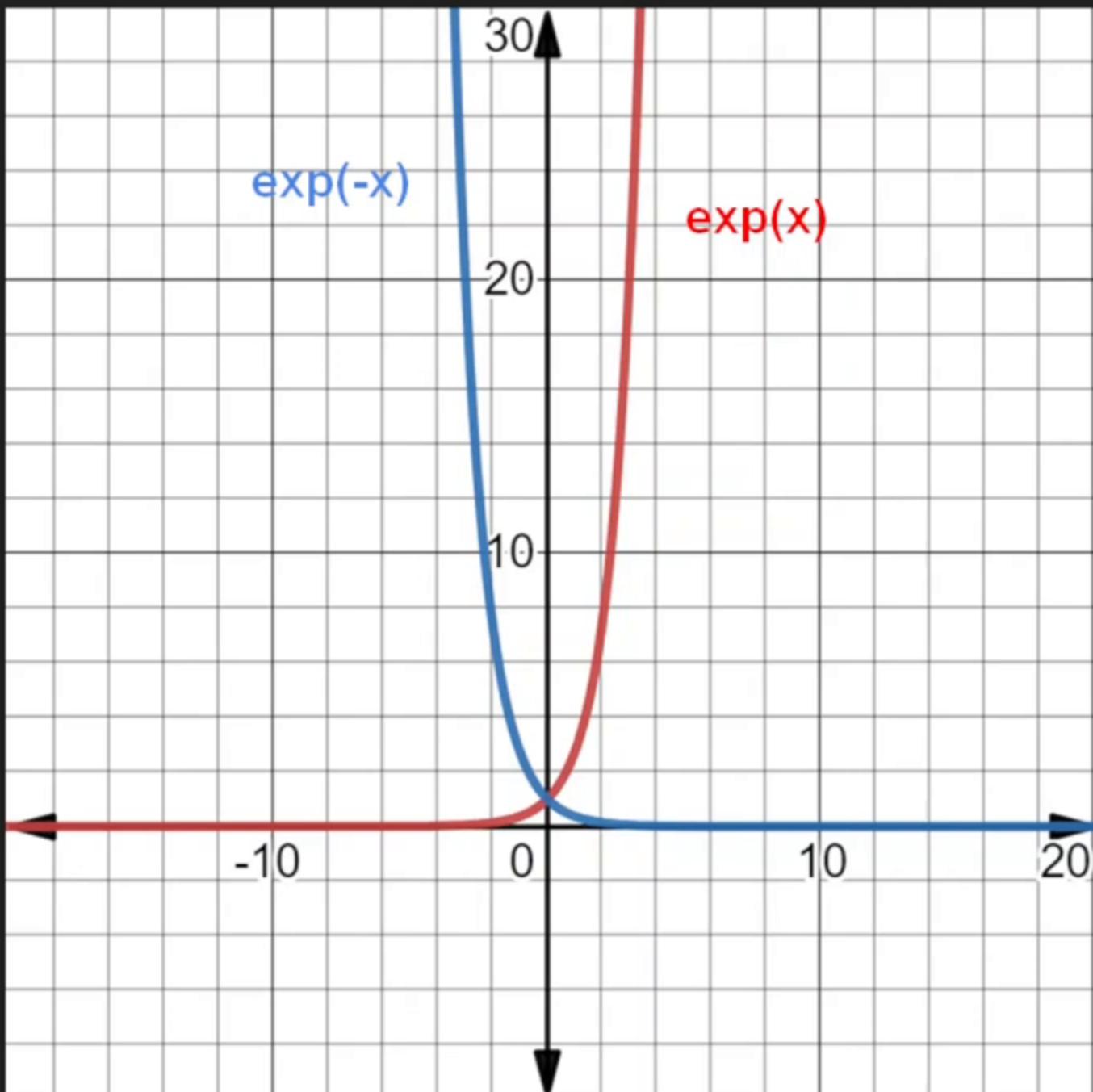
$$x = -\infty \rightarrow \frac{0 - 0}{0 + \infty} = -1$$

$$x = 0 \rightarrow \frac{1 - 1}{1 + 1} = 0$$

$$x = \infty \rightarrow \frac{\infty - 0}{\infty + 0} = 1$$

$$x \rightarrow -\infty \quad 0 \quad \infty$$

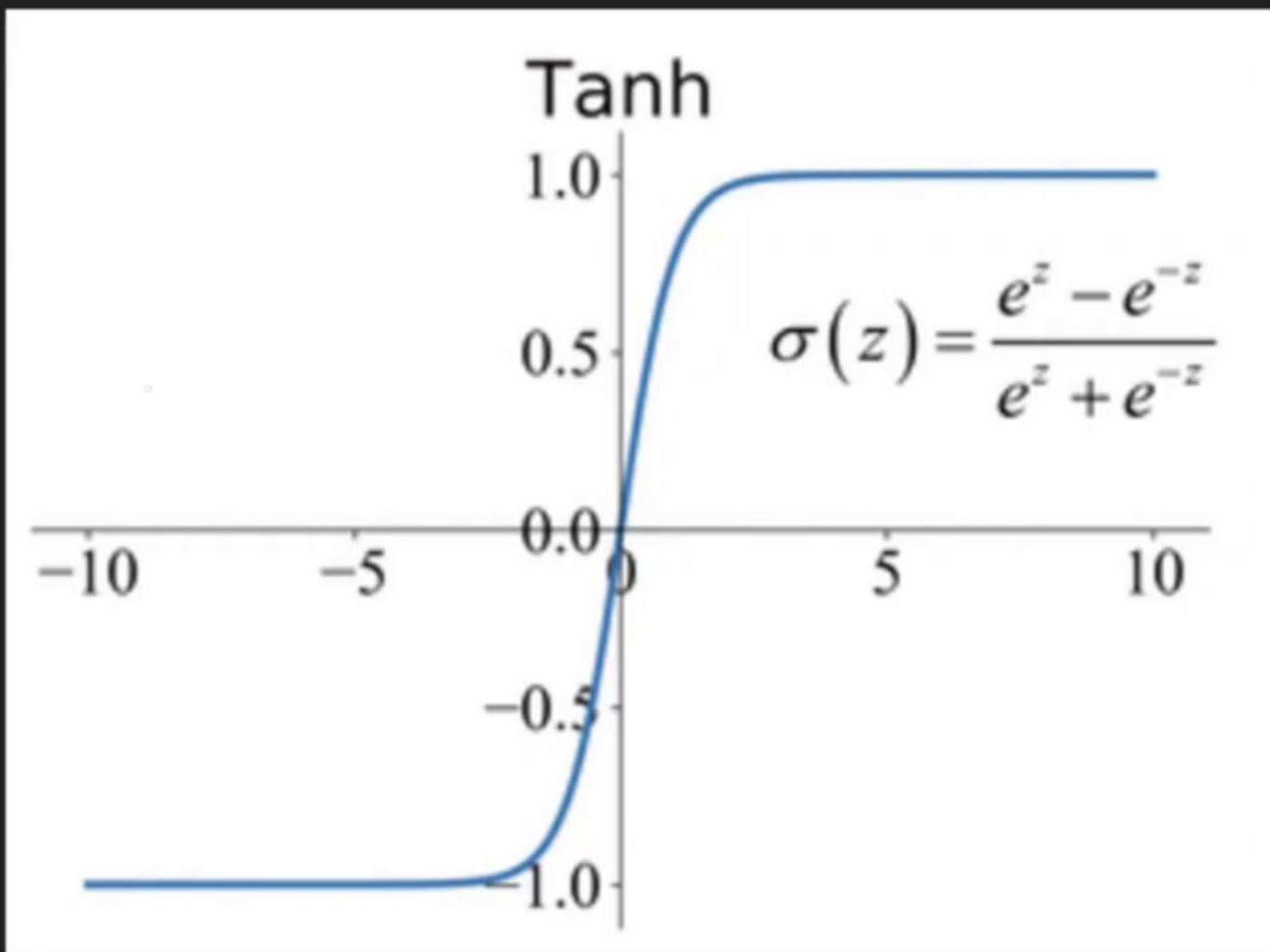
$$\tanh \rightarrow -1 \cdot$$



## Definition

Tanh Function

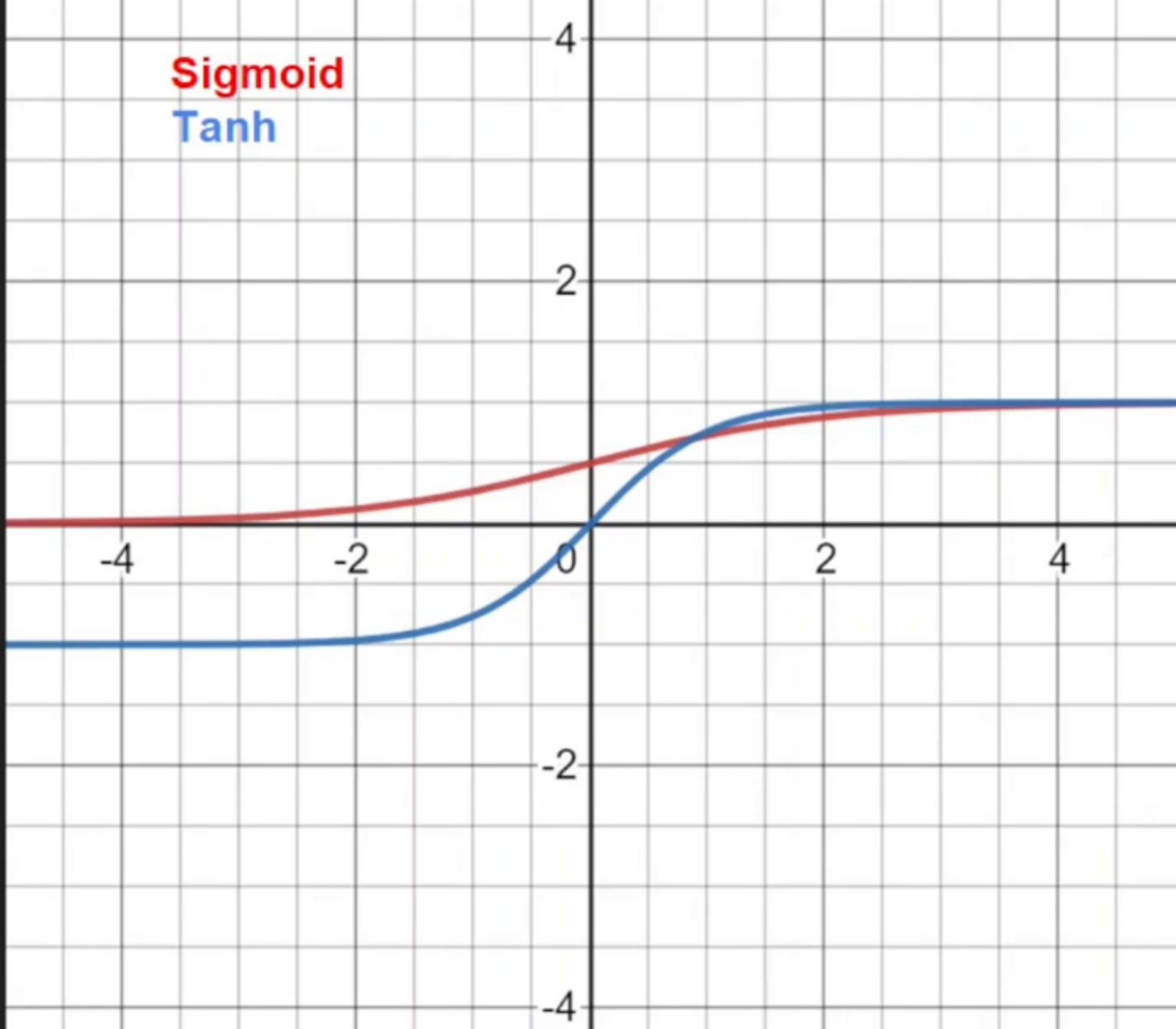
$$a = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$



1)

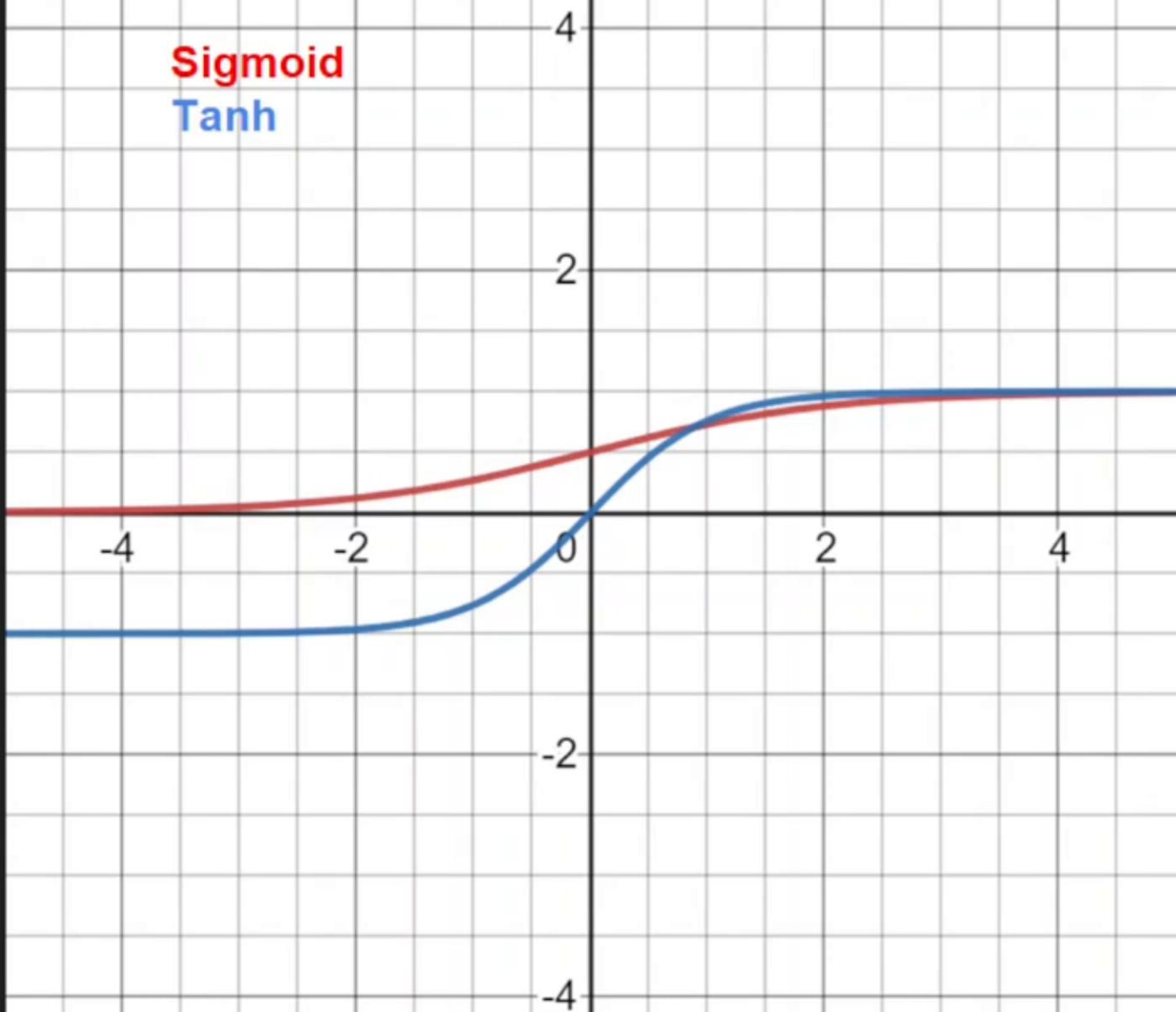
D

Sigmoid  
Tanh



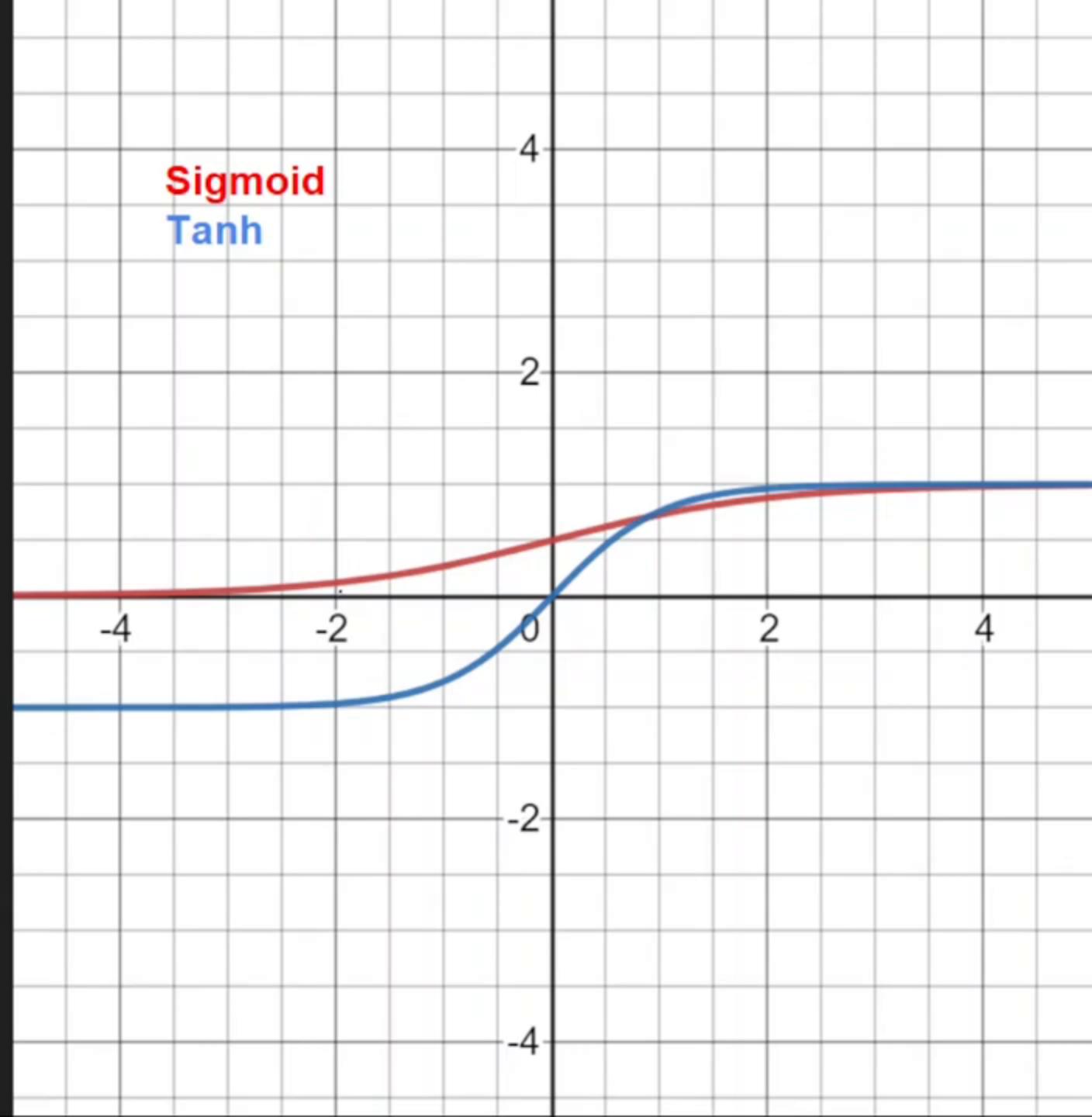
1)  $0 - 1$ ,  $-1$  to  $+1$

Sigmoid  
Tanh



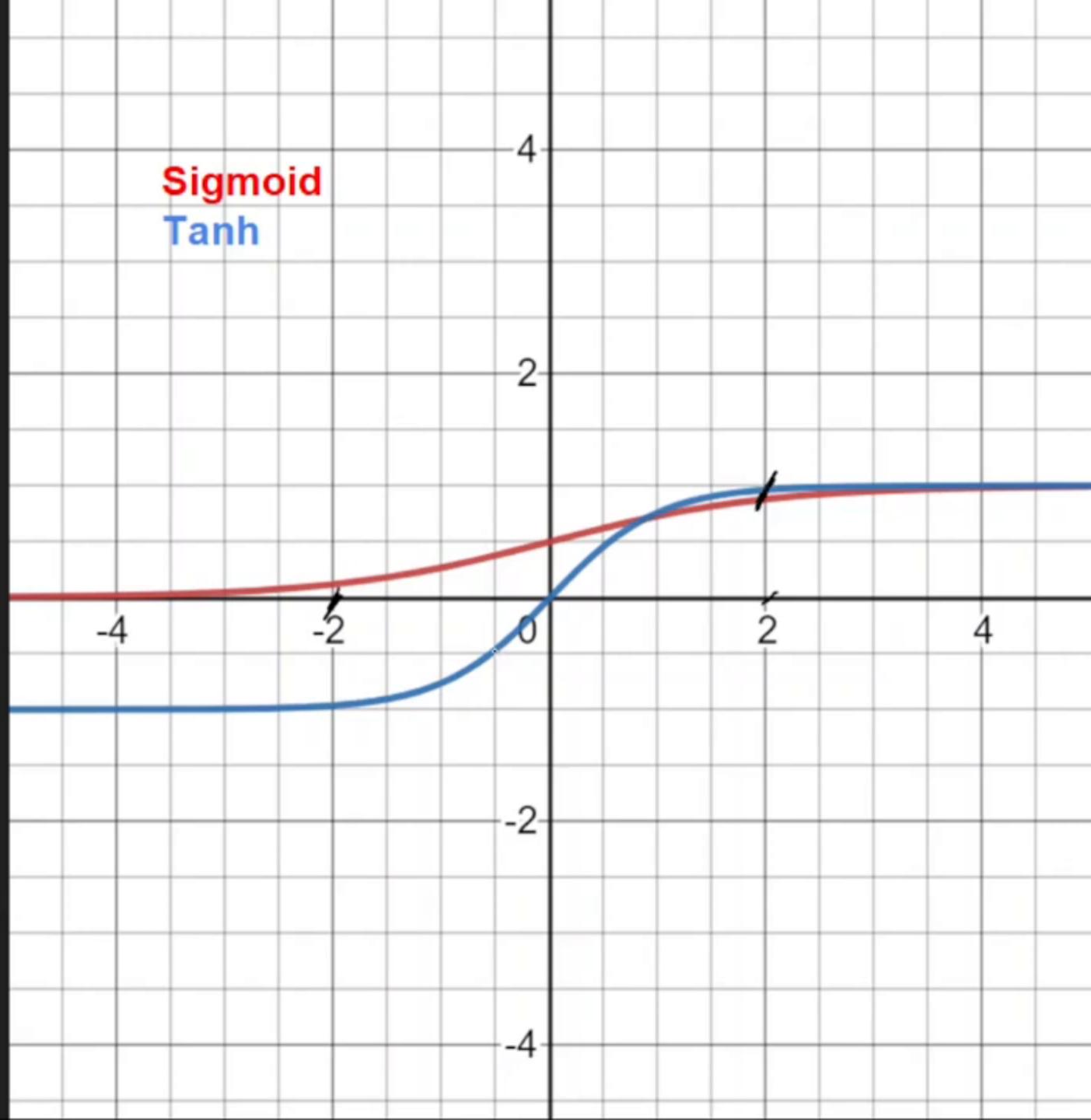
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2) tanh is steeper



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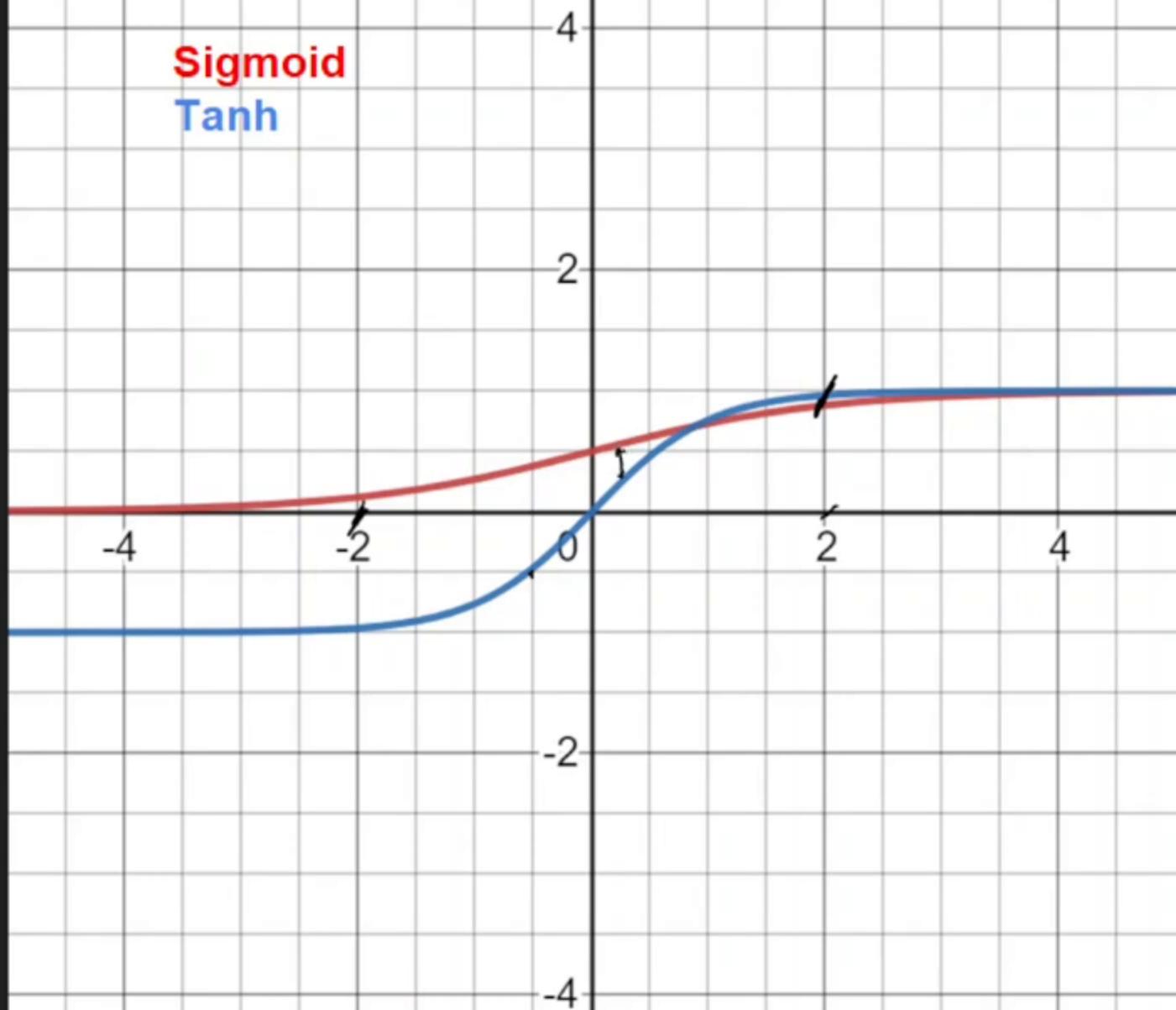


1)  $0 - 1$ ,  $-1$  to  $+1$

2) tanh is steeper



Sigmoid  
Tanh



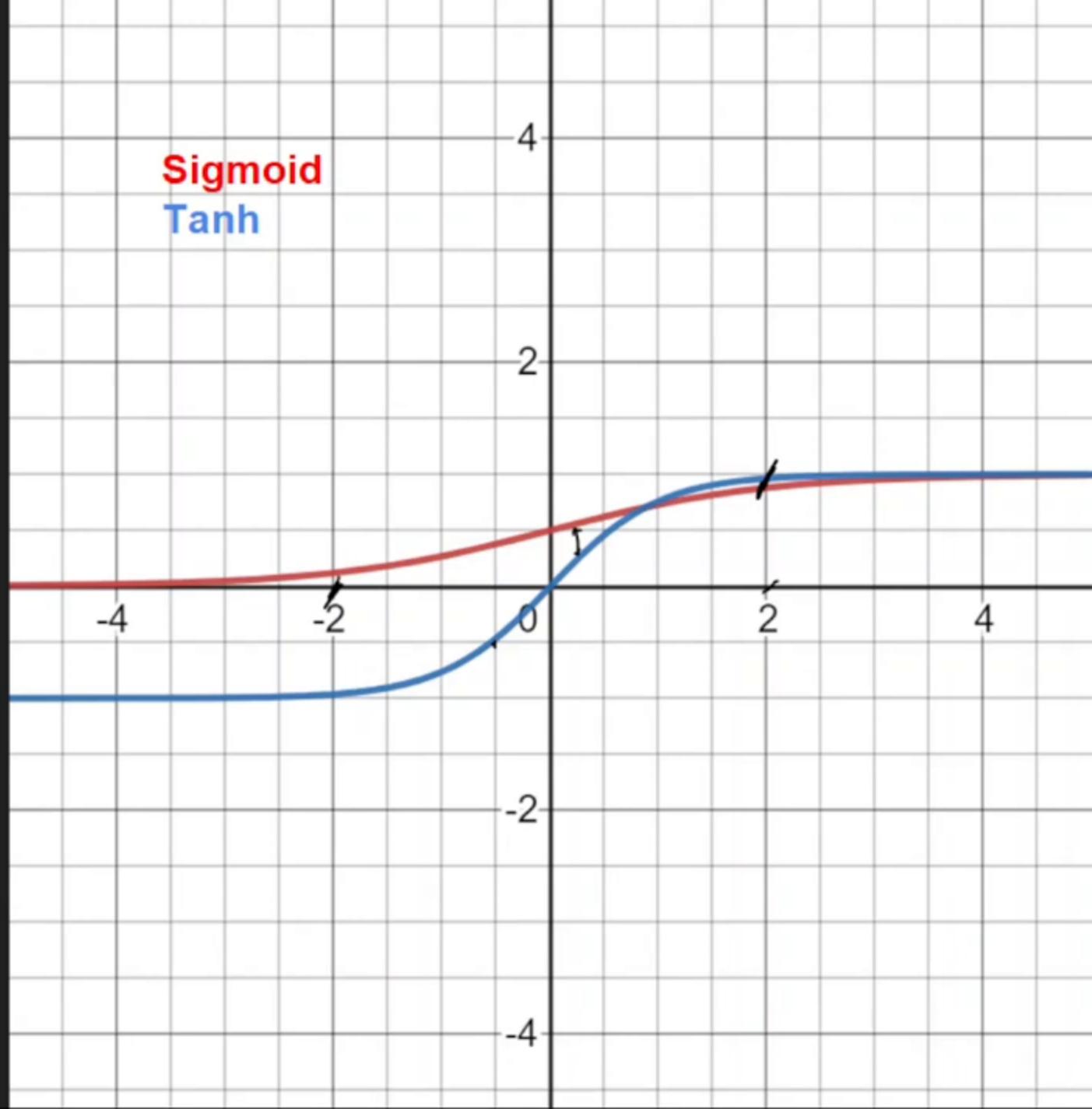
1)  $0 - 1$ ,  $-1$  to  $+1$

2) tanh is steeper



✓ large gradients

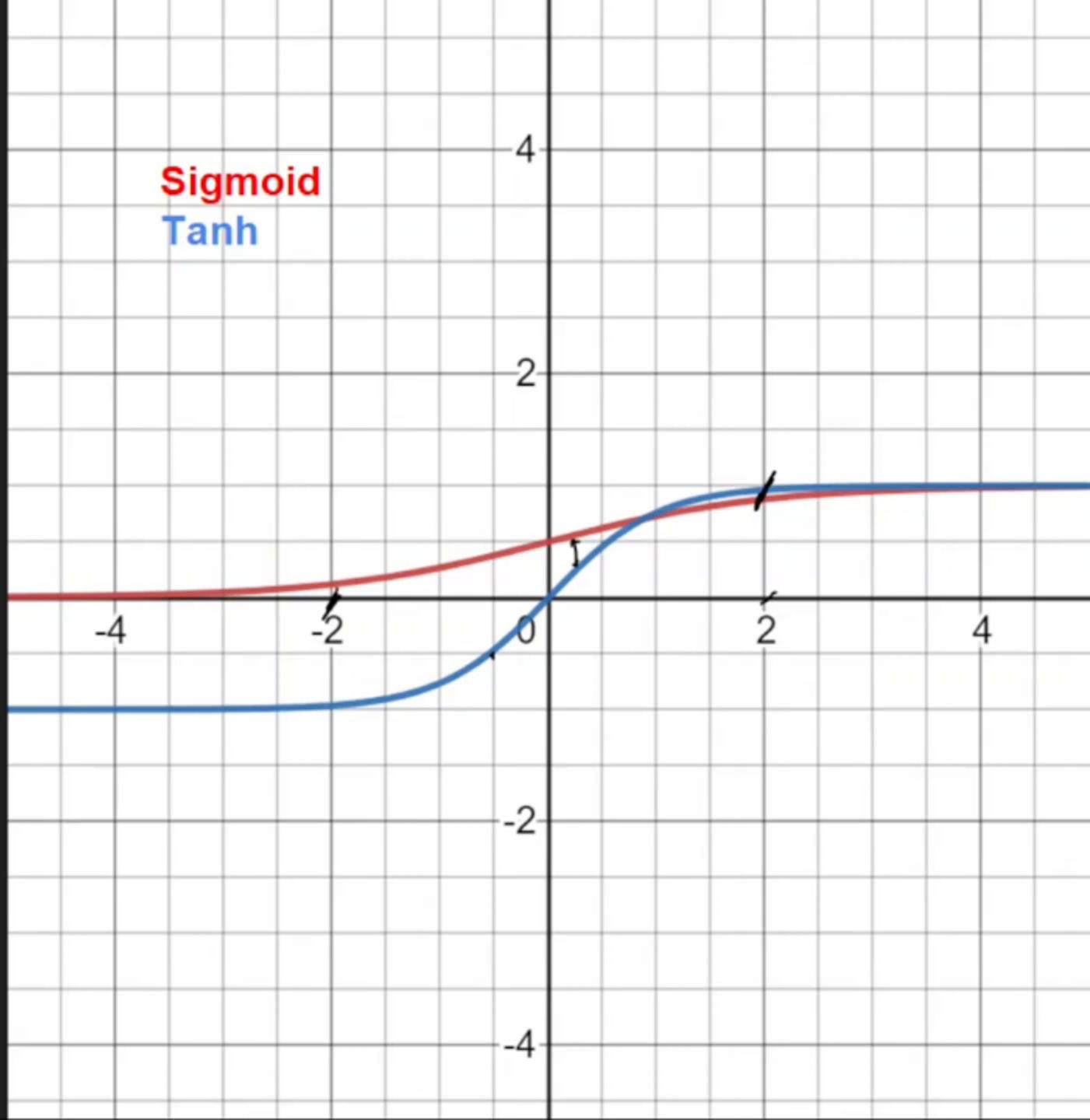
Sigmoid  
Tanh



1)  $0 - 1$ ,  $-1$  to  $+1$

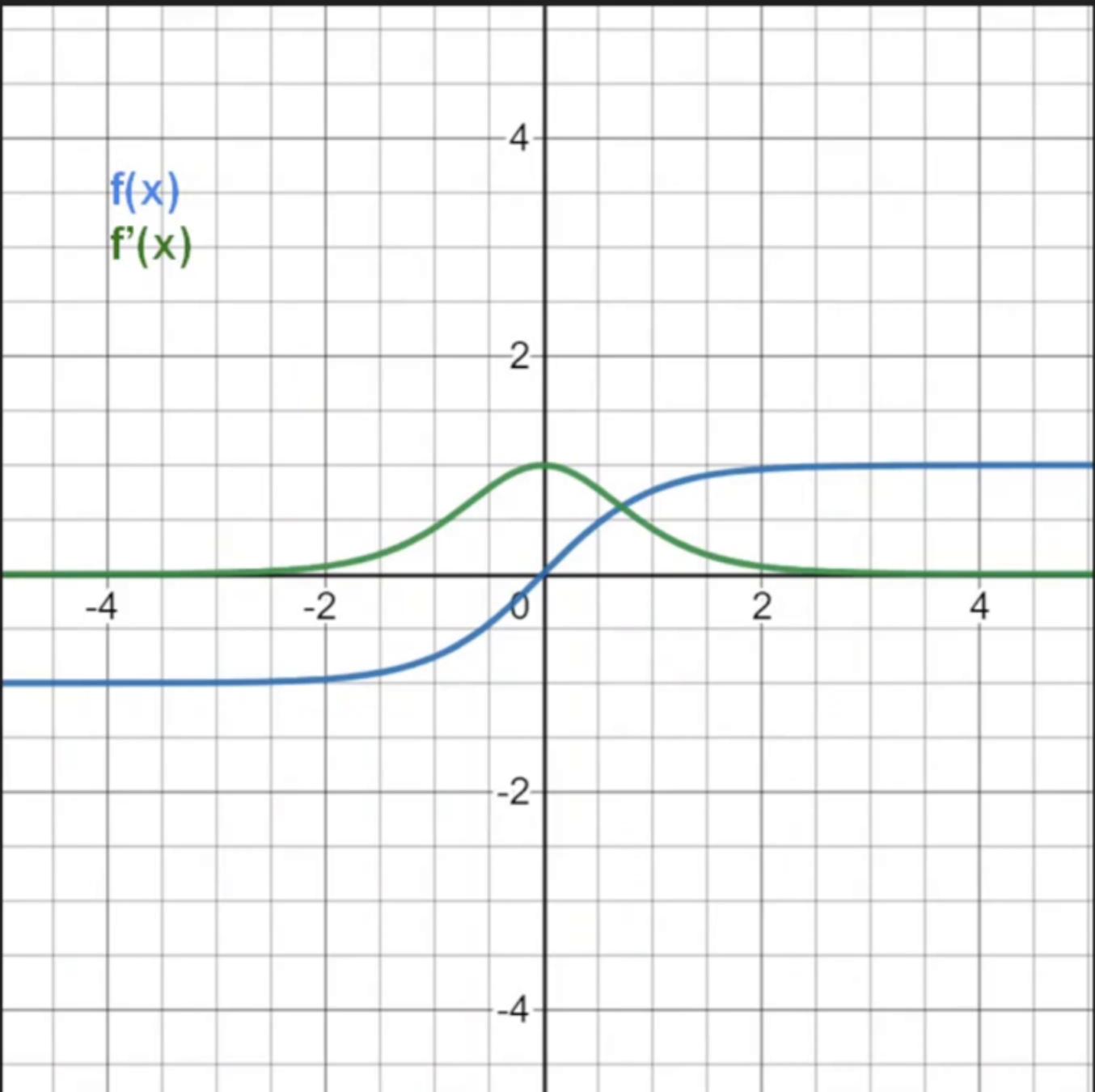
- 2)  $\tanh$  is steeper
- ↳ ↓  
↳ large gradients  
↳ -ve gradients  
↳ faster

Sigmoid  
Tanh



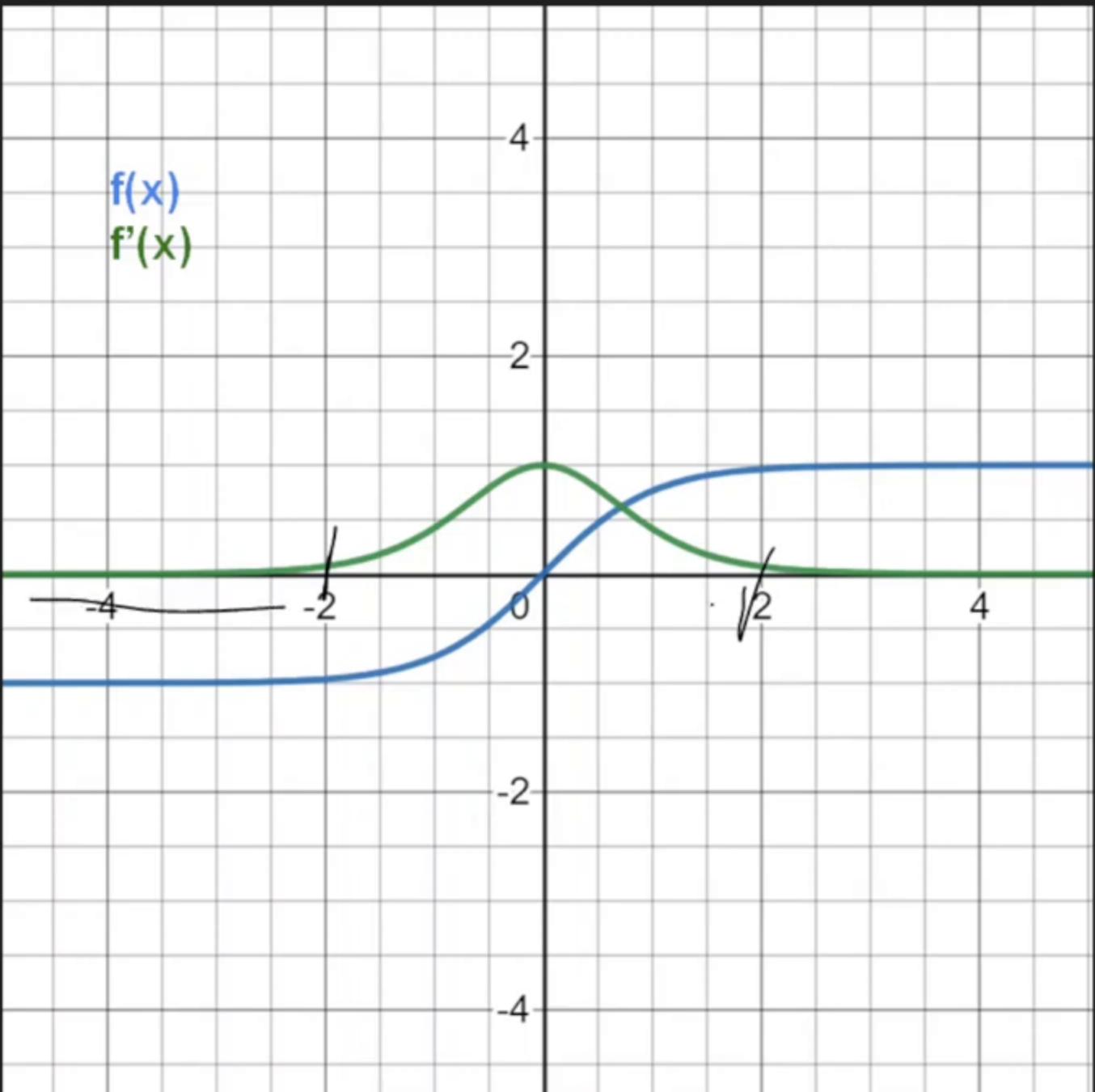
# Derivative

$$1 - (\underline{\tanh}(x))^2$$



# Derivative

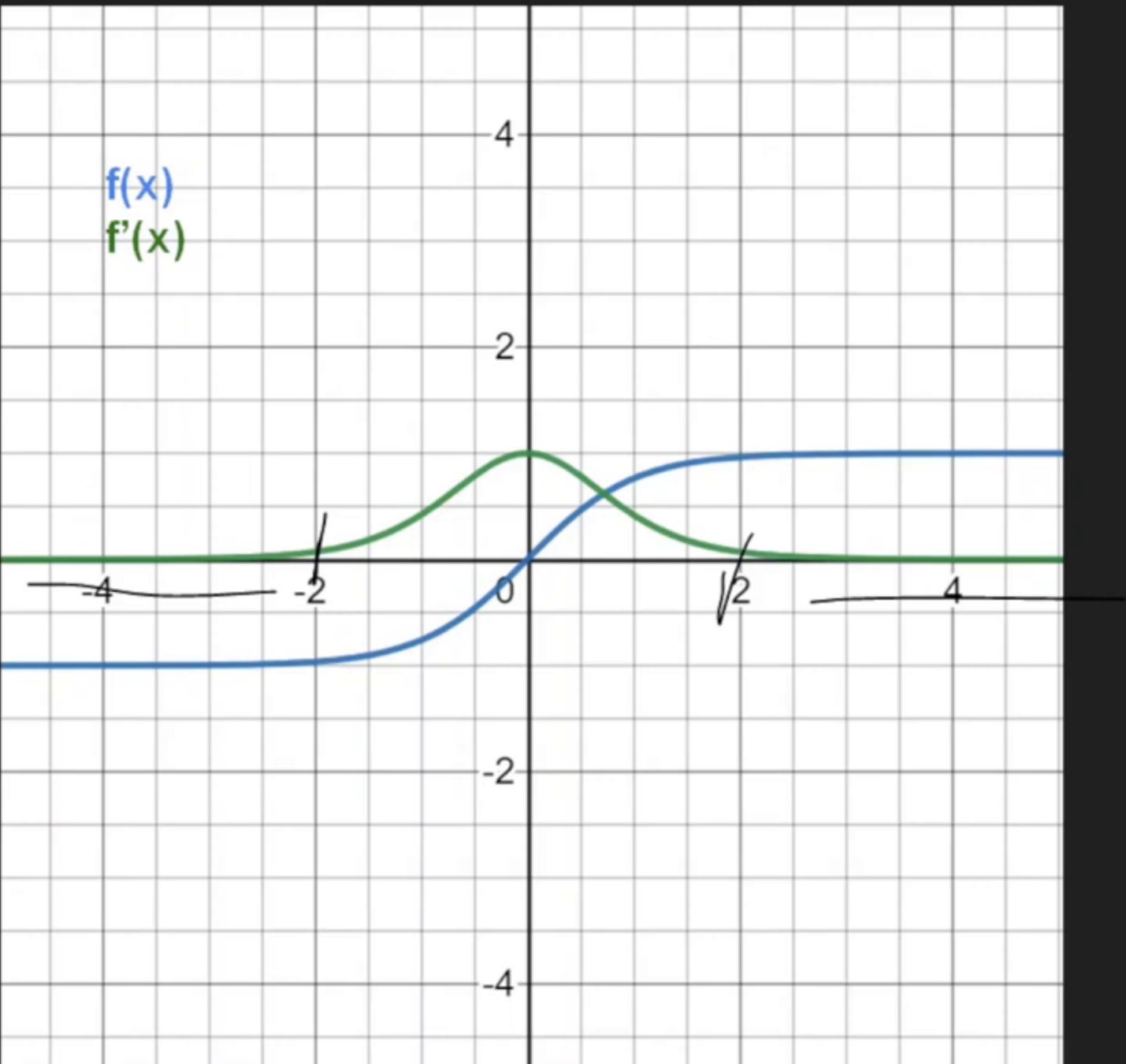
$$1 - (\underline{\tanh}(x))^2$$



# Derivative

$$1 - (\tanh(x))^2$$

Vanishing  
gradient

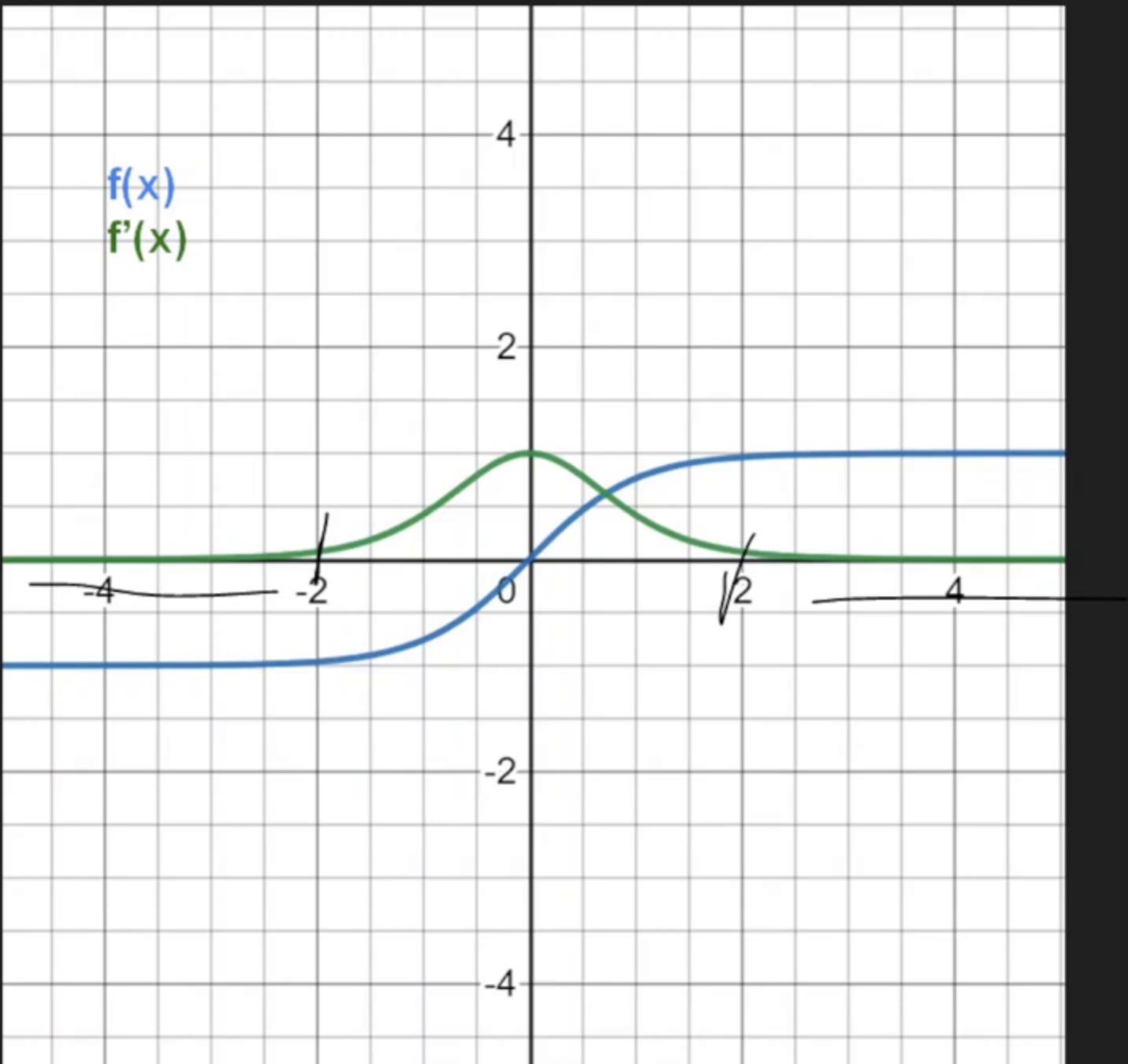


# Derivative

$$1 - (\tanh(x))^2$$

Vanishing  
gradient

-1

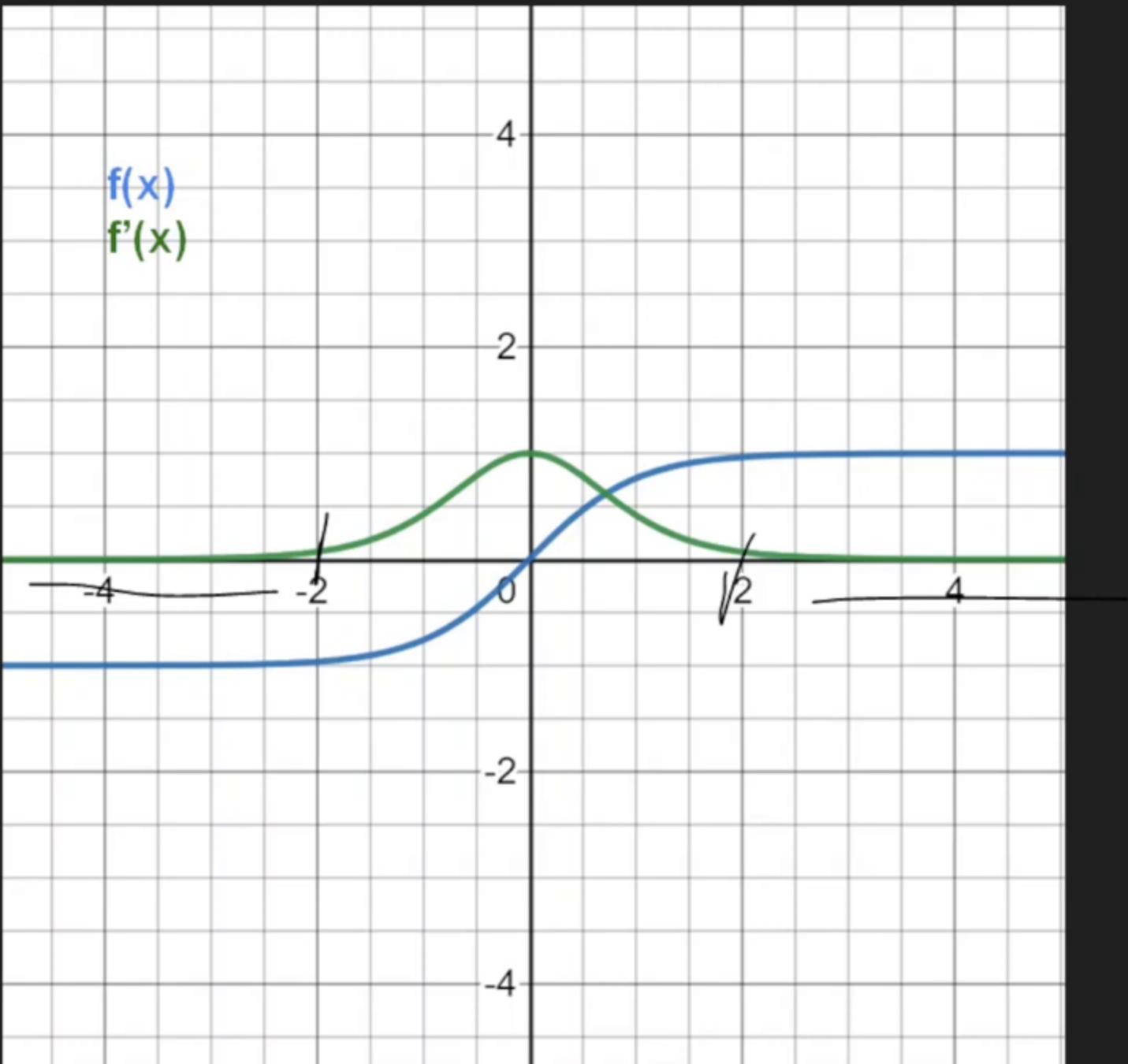


# Derivative

$$1 - (\tanh(x))^2$$

Vanishing  
gradient

$\frac{-1}{-1}$  to  $\frac{+1}{+1}$



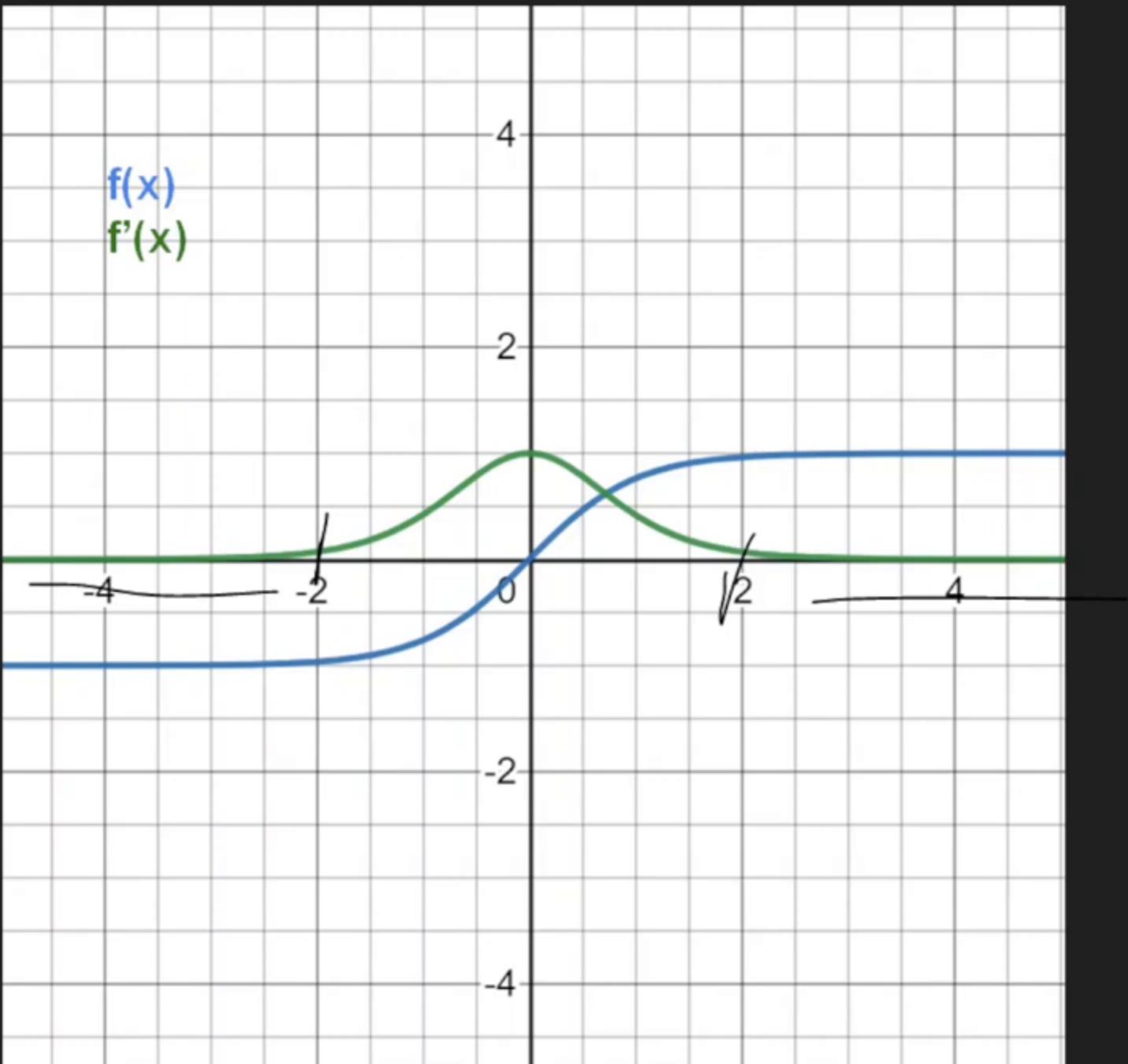
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$$1 - (\tanh(x))^2$$

Vanishing  
gradient

-1 to +1

→



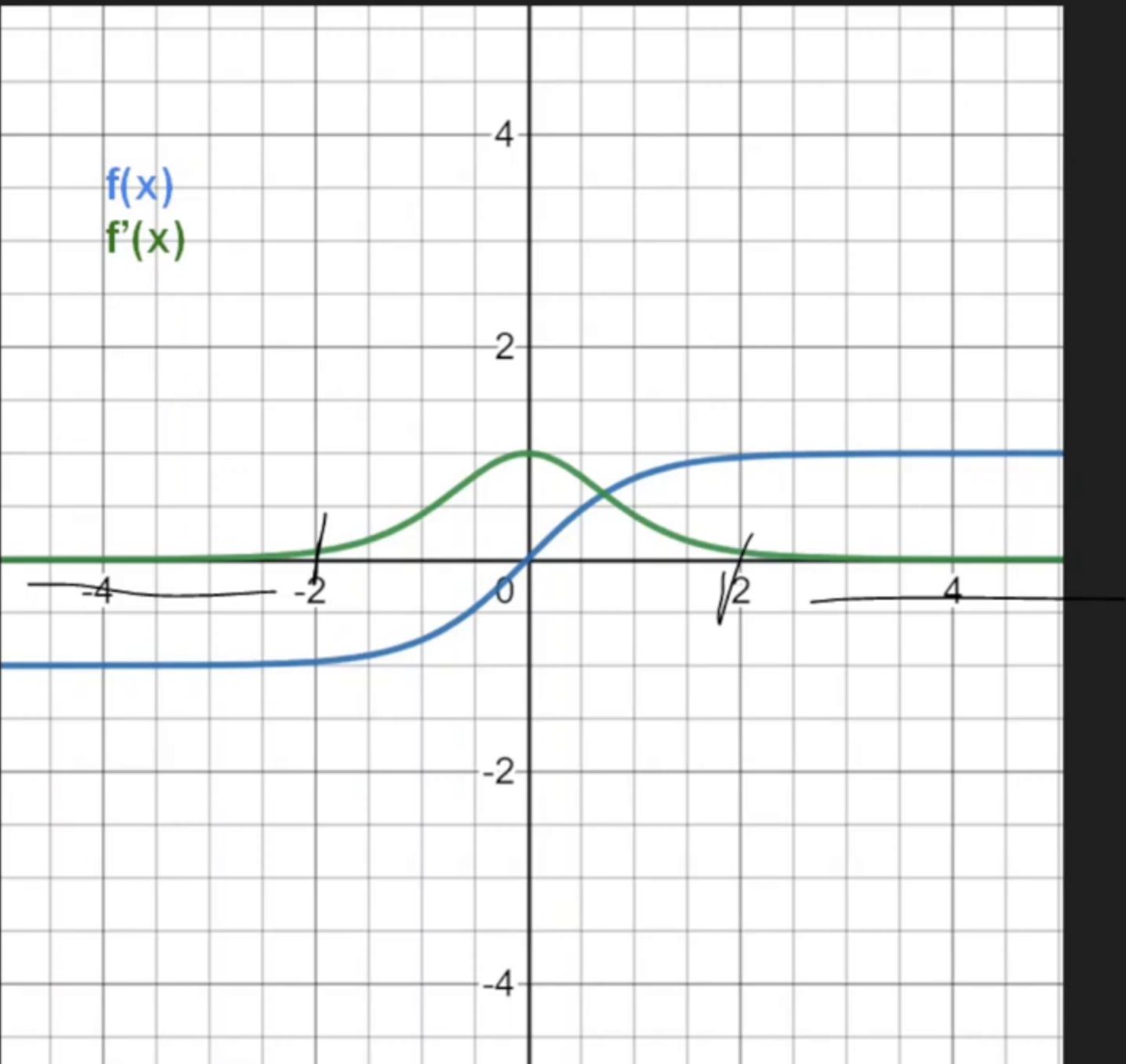
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$$1 - (\tanh(x))^2$$

Vanishing  
gradient

$-1 \rightarrow +1$

- only hidden layers
- vanishing gradient
- computationally expensive



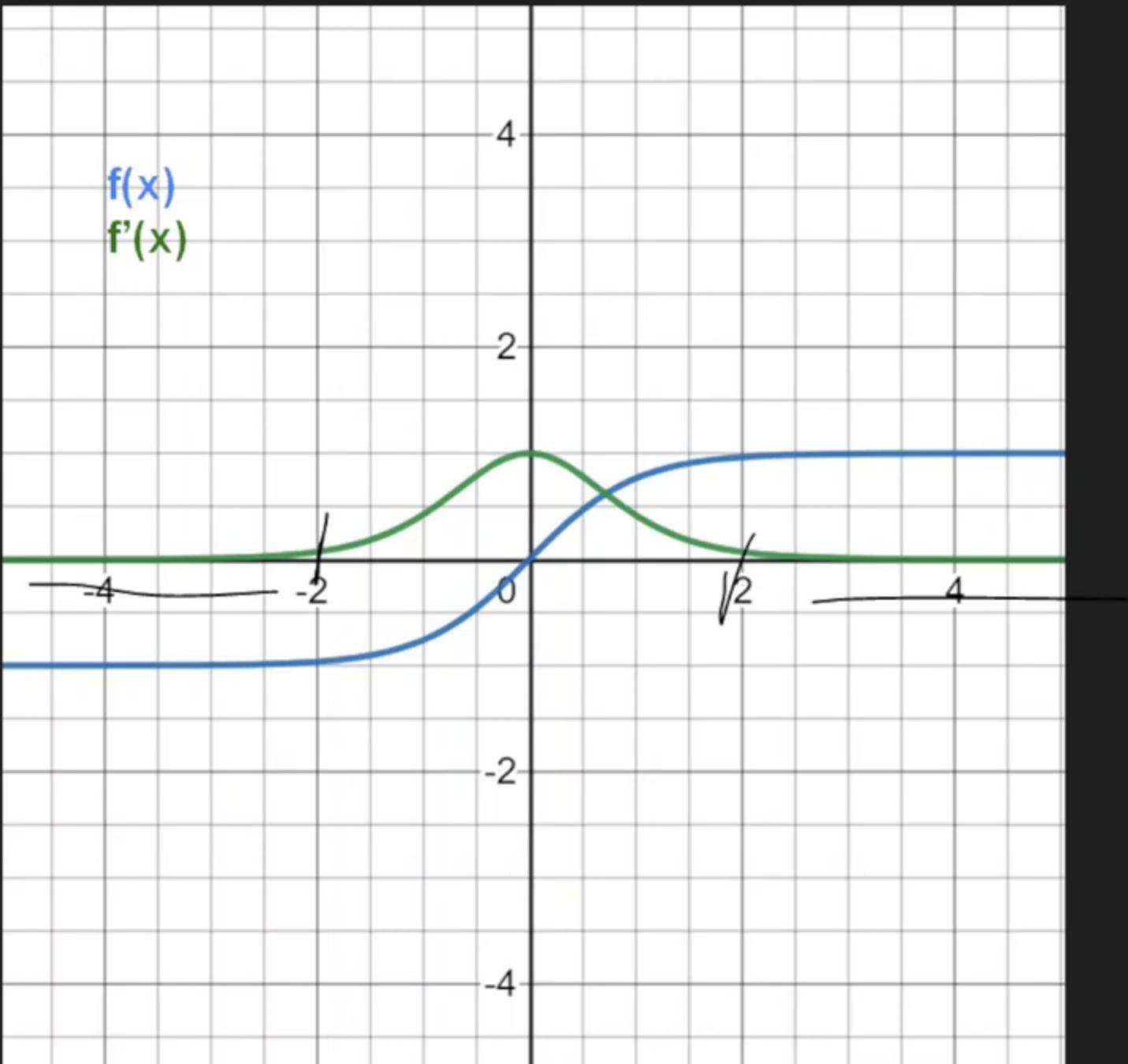
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# Python Implementation

Tanh Function  
$$a = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$
.

```
def tanh(x):
    t=(np.exp(x)-np.exp(-x))/(np.exp(x)+np.exp(-x)) # tanh function
    dt = 1-t**2 # Derivative
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Neuron.ipynb

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Tanh Activation

```
import matplotlib.pyplot as plt
import numpy as np
def tanh(x):
    t=(np.exp(x)-np.exp(-x))/(np.exp(x)+np.exp(-x))
    # t = np.tanh(x)
    dt=1-t**2
    return t,dt
```

```
[ ] z=np.arange(-4,4,0.01)

fig, ax = plt.subplots(figsize=(9, 5))
ax.spines['left'].set_position('center')
ax.spines['bottom'].set_position('center')
ax.spines['right'].set_color('none')
ax.spines['top'].set_color('none')
ax.xaxis.set_ticks_position('bottom')
ax.yaxis.set_ticks_position('left')
ax.plot(z,tanh(z)[0], color="#307EC7", linewidth=3, label="tanh")
ax.plot(z,tanh(z)[1], color="#9621E2", linewidth=3, label="derivative")
ax.legend(loc="upper left", frameon=False)
fig.show()
```

```
[ ]
```

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[ ]

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Tanh Activation

```
[1]: import matplotlib.pyplot as plt
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def tanh(x):
    t=(np.exp(x)-np.exp(-x))/(np.exp(x)+np.exp(-x))
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```

```
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```

[ ]

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```

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