

GATE

CRASH COURSE

Data Science & AI

Subject

Python-for data science
Functions, Recursion in Python

Lect No. 06

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Last Class

Quick Recap

- 1 Homework Questions Solution
- 2 Nested Lists
- 3 String Methods
- 4 Tuples
- 5 Sets and Examples



Topics to be covered

- 1 Homework Questions Solution
- 2 Set Methods and Operations
- 3 Dictionaries
- 4 Functions, Recursion
- 5 Examples





Homework Question



count=1

x=[1, 3, 5, [7, 9, [2, 4], 6], 8]

y=(5, 7, (9, 3, 1, (6, 2), 4), 8)

i=x[3][2][1] $i=4$

j=y[2][3][0] $j=6$

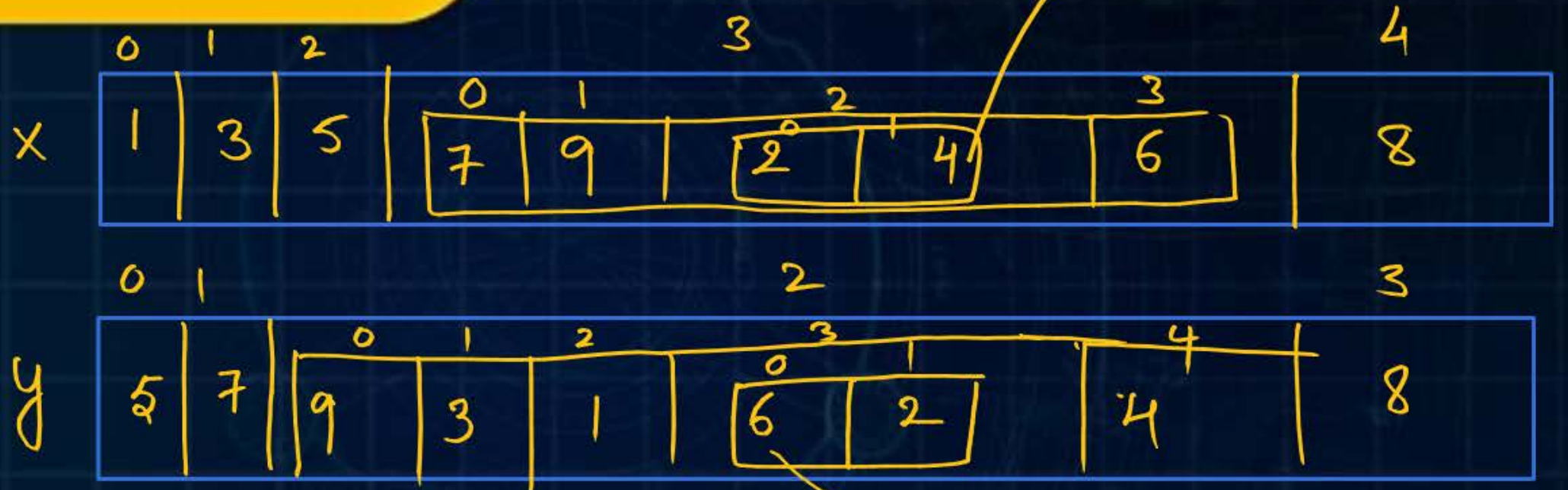
for a in range(i):

for b in range(j):

count=count+a+b

print(count)

Ans: 97



	b=0	b=1	b=2	b=3	b=4	b=5
a=0	count=1+0+0	1+0+1=2	2+0+2=4	4+0+3=7	7+0+4=11	11+5=16
a=1	16+1=17	17+2=19	19+1+2=22	22+4=26	26+5=31	31+6=37
a=2	37+2=39	39+3=42	42+4=46	46+5=51	51+6=57	57+7=64
a=3	64+3=67	67+4=71	71+5=76	76+6=82	82+7=89	89+8=97



Set Methods



Method	Shortcut	Description
add()		Adds an element to the set
clear()		Removes all the elements from the set
copy()		Returns a copy of the set
difference()	- —	Returns a set containing the difference between two or more sets
difference_update()	-= —	Removes the items in this set that are also included in another, specified set
discard()		Remove the specified item
intersection()	& —	Returns a set, that is the intersection of two other sets
intersection_update()	&= —	Removes the items in this set that are not present in other, specified set(s)
isdisjoint()		Returns whether two sets have a intersection or not



Set Methods



Method	Shortcut	Description
issubset()	<u><=</u>	Returns whether another set contains this set or not
	<	Returns whether all items in this set is present in other, specified set(s)
issuperset()	<u>>=</u>	Returns whether this set contains another set or not
	>	Returns whether all items in other, specified set(s) is present in this set
pop()		Removes an element from the set
remove()		Removes the specified element
symmetric_difference()	<u>^</u>	Returns a set with the symmetric differences of two sets
symmetric_difference_update()	<u>^=</u>	Inserts the symmetric differences from this set and another
<u>union()</u>	<u> </u>	Return a set containing the union of sets
<u>update()</u>	<u> =</u>	Update the set with the union of this set and others

Question



$$S_1 = \{1, 3, 5, 3, 7, 1, 5\} \Rightarrow S_1 = \{1, 3, 5, 7\}$$

$$S_2 = \{1, 2, 3, 4, 5\}$$

$$S_3 = \{3, 4, 5, 6, 7\}$$

$$S_4 = S_1 \cup S_3 \quad \# \quad S_4 = \{1, 3, 4, 5, 6, 7\}$$

$$S_5 = S_2 \cap S_3 \quad \# \quad S_5 = \{3, 4, 5\}$$

$$i = \text{len}(S_4 - S_5) \quad \# \quad \{1, 6, 7\} \Rightarrow \text{len}() = 3 \Rightarrow i = 3$$

$$j = S_3 \text{ difference } (S_4) \quad \# \quad j = \{\} \text{ Empty set}$$
$$\cong S_3 - S_4$$

Question



$$S_1 = \{ 'G', 'A', 'T', 'E' \}$$

$$S_2 = \{ 'E', 'X', 'A', 'M', 'I', 'N', \cancel{'A'}, \cancel{'T'}, \cancel{'E'}, 'O', 'N' \} \Rightarrow S_2 = \{ 'E', 'X', 'A', 'M', 'I', 'N', 'T', 'O' \}$$

$$S_3 = \{ 'G', 'A', 'T', 'E', \cancel{'E'}, \cancel{'X'}, \cancel{'A'}, 'M' \} \Rightarrow S_3 = \{ 'G', 'A', 'T', 'E', \underline{'X'}, \underline{'M'} \}$$

$$S_4 = \{ 'I', \cancel{'T'}, 'T', 'R', \cancel{'O'}, 'O', \cancel{'R'}, 'K', \cancel{'E'}, 'E' \} \Rightarrow S_4 = \{ \underline{'I'}, \underline{'T'}, 'R', 'O', 'K', 'E' \}$$

$$result = \text{len}(S_3 \cap S_1) \quad \text{len}(\{ 'G', 'A', 'T', 'E' \}) = 4$$

$$S_4 - S_2 = \{ 'R', 'K' \} \Rightarrow \text{len}() = 2$$

$$S_3 \cap S_1 = \{ 'X', 'M' \} \Rightarrow \text{len}() = 2$$

for i in range(len(S4 - S2)):

for j in range(len(S3 ∩ S1)):

$$result = result + i + j$$

Print(result) #8

	j=0	j=1
i=0	4+0+0=4	4+0+1=5
i=1	5+1+0=6	6+1+1= <u>8</u>



Dictionaries



- Ordered Collection
- Mutable [values can be mutable]
- dictionaries support duplicates [duplicate values not keys]
- Dictionaries are collection of {key : value} Pairs.
- Can be created as:

Object = { 'key1': value1, 'key2': value2, ... }

Ex: d = { 'a': 1, 'b': 2, 'c': 3 }

Empty Dictionary:

object = { } Ex: d = { }

object = dict()

Ex: d = dict()



Dictionaries



Access Elements of dictionary

$d = \{ 'a': 3, 'b': 7, 'c': 5 \}$

`Print(d.keys())` # $\{ 'a', 'b', 'c' \}$

`Print(d.values())` # $\{ 3, 7, 5 \}$

`Print(d.items())` # $\{ 'a': 3, 'b': 7, 'c': 5 \}$

Ex:

`for i in d.keys():`

`for j in d.values():`

`Print(i, j)` o/p: $a : 3$
 $b : 7$
 $c : 5$

(OR)

`for (i, j) in d.items():`

`Print(i, j)`



Dictionaries



Method	Description
<code>clear()</code>	Removes all the elements from the dictionary
<code>copy()</code>	Returns a copy of the dictionary
<code>fromkeys()</code>	Returns a dictionary with the specified keys and value
<code>get()</code>	Returns the value of the specified key
<code>items()</code>	Returns a list containing a tuple for each key value pair
<code>keys()</code>	Returns a list containing the dictionary's keys
<code>pop()</code>	Removes the element with the specified key
<code>popitem()</code>	Removes the last inserted key-value pair
<code>setdefault()</code>	Returns the value of the specified key. If the key does not exist: insert the key, with the specified value
<code>update()</code>	Updates the dictionary with the specified key-value pairs
<code>values()</code>	Returns a list of all the values in the dictionary

Question



$d = \{ 'IITB': 2022, 'IITM': 2023, 'IISC': 2024 \}$

$d['IITR'] = 2025$ $\# d = \{ 'IITB': 2022, 'IITM': 2023, 'IISC': 2024, 'IITR': 2025 \}$

$d.update('IITM') = 2020$ $\# d = \{ 'IITB': 2022, 'IITM': 2020, 'IISC': 2024, 'IITR': 2025 \}$

$d.pop('IITB')$ $\# d = \{ 'IITM': 2020, 'IISC': 2024, 'IITR': 2025 \}$

$d.popitem()$ $\# \{ 'IITM': 2020, 'IISC': 2024 \}$

$del d['IITM']$ $\# \{ 'IISC': 2024 \}$

$del d$ $\# \text{removes complete Dictionary}$

Question



Nested Dictionaries

```
Student = { 'Name': { 'fname': 'abc', 'lname': 'xyz' },  
            'Marks': { 'I Year': 70, 'II Year': 90 },  
            'Occupation': { 'Mother': 'Home maker', 'Father': 'BUSINESS' } }
```

```
Print ( Student ['Name'] ['lname'] ) # xyz
```

```
Print ( Student ['Occupation'] ['Father'] ) # BUSINESS
```

```
Student ['marks'] ['I Year'] = 80
```




Function : A single statement (or) multiple statements, that performs specific task (or) subtask is called function.

Advantages : 1) Modularity 2) Reusability 3) Readability of Code

```

Ex:      def add(x,y):
              z = x + y
              print(z)
              add(4,5) # 9

```

Invoke/call function : Name (arguments)



Functions, Recursion



Recursion: The Process of Calling a function by itself.

- For recursive calls, to be finite, Base Condition need to be included in function code.
- Base Case / Base Condition: The Point at which, Recursive calling will stop.

Syntax:

```
def fun(argument(s)):
```

```
    Base Condition:  
    statement(s)
```

```
    fun(argument)
```

```
    fun(argument)
```

Ex:

```
def display(i):
```

```
    if i <= 0:
```

```
        return
```

```
    print(i)
```

```
    display(i-2)
```

→ display(7)

i = 7

5

3

1

i <= 0 True

o/p:

7

5

3

1



Functions, Recursion



Question



```
def f(i):
```

```
    if i <= 0:
```

```
        return i+1
```

Base case

```
    return i + f(i-2)
```

Print ($f(7)$)

o/p: 16

$f(7)$ $i=7$

$7 \leq 0$ False

return $7 + f(5)$

$7+9=16$

$f(5)$ $i=5$

$5 \leq 0$ False

return $5 + f(3)$

$5+4=9$

$f(3)$ $i=3$

$3 \leq 0$ False

return $3 + f(1)$

$3+1=4$

$f(1)$ $i=1$

$1 \leq 0$ False

return $1 + f(-1)$

$1+0=1$

$f(-1)$ $i=-1$

$-1 \leq 0$ True

return $(-1+1)$

0

Question

```
def fun(x):
```

```
    if x < 0:
```

```
        return
```

```
    elif x <= 3:
```

```
        Print(x-1, end=' ')
```

```
        fun(x-2)
```

```
    else:
```

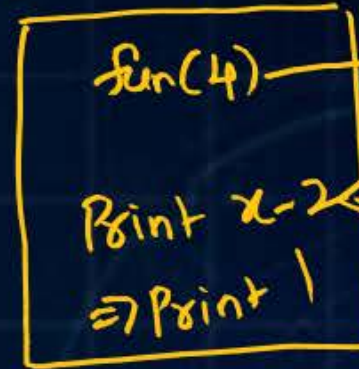
```
        fun(x-1)
```

```
        Print(x-2, end=' ') ✓
```

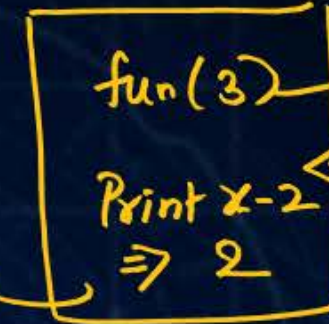
fun(5)

o/p= _____

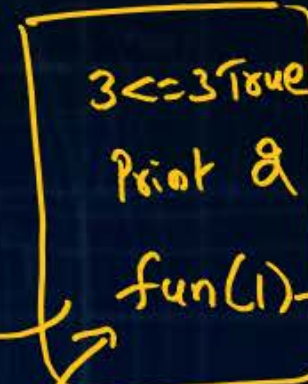
fun(5) x=5



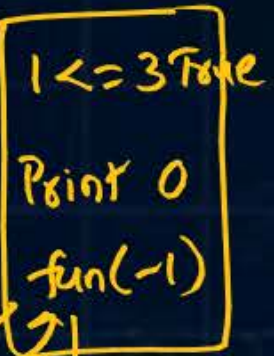
fun(4) x=4



fun(3) x=3



fun(1) x=1



fun(-1) x=-1



o/p: 2 0 2 3

Question

The Return value of $f(7)$ is 22

```
def f(x):
```

```
    if x < 1:
```

```
        return x + x
```

```
    elif x <= 2:
```

```
        return (x-1) + f(x-1)
```

```
    elif x <= 5:
```

```
        return (x+3) + f(x-3)
```

```
    else:
```

```
        return x + f(x-1)
```

$$f(7) \quad x=7$$

$$7 + f(6) \quad x=6$$

$$6 + f(5) \quad x=5$$

$$(5+3) + f(2) \quad x=2$$

$$(2-1) + f(1) \quad x=1$$

$$(1-1) + f(0) \quad x=0$$

$$(0+0)$$

$$= 7+6+8+1+0+0$$

$$= \underline{\underline{22}}$$



Summary



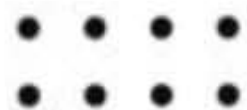
- Set methods
- Dictionaries
- Nested dict
- functions
 - Recursion*
 - Examples



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Thank
THANK



Keep Hustling!