

GATE

CRASH COURSE

DS & AI

Machine learning

Naive Bayes
Lec No. 05

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GATE WALLAH

Topics to be Covered

- 1 Bayes Classifier
 - 2 Naive Bayes.
- Classification



In Bayes classifier \Rightarrow

If any new test point is (x_i)

then we find $P(x_i/y_j)P_{y_j}$

$\cdot P(x_i/y_1)P_{y_1} \checkmark$

$\cdot P(x_i/y_2)P_{y_2} \checkmark$

$\cdot P(x_i/y_m)P_{y_m} \checkmark$

a No of values/dimension

data					Y
x^1	x^2	x^3	\dots	x^D	M
					Class
					y_1
					y_2
					\vdots
					y_m
$\cdot P_{y_j} = \frac{\text{No of Points of class } y_j}{\text{Total No of Points in dataset.}}$					

So $\underbrace{P(x_i/y_i)} \cdot P_{y_i}^{\checkmark}$

→ this is calculated from dataset

$\Rightarrow \underline{x_i^0} \Rightarrow \underline{\underline{a^D}}$

$P(x_i/y_1) \rightarrow a^D$

$P(x_i/y_2) \rightarrow a^D$

$P(x_i/y_3) \rightarrow a^D$

⋮
M class.

Total No of Parameters $(a^D M) + M$

Bayes Classifier

- ⇒ Work on MAP Rule
- ⇒ For any point x_i it find $P(x_i|c_j)Pc_j$
- ⇒ For all class we find $P(x_i|c_j)Pc_j$
- ⇒ So, whichever class $\max P(x_i|c_j)Pc_j$ that class will be assigned to x_i
- ⇒ $Pc_j = \frac{\text{Number of points in Class } c_j}{\text{Total number of points in training data}} \Rightarrow M \text{ probable}$

Bayes Classifier

- $P(x_i|c_j)$ = calculated from + training data
- M: Number of classes, D: Number of dimensions, each dimension can take a values,

$$P(x_i^1, x_i^2, \dots, x_i^x / c_j) \Rightarrow (a^D \times M)$$

- Total parameters = $(a^D M + M) \Rightarrow$ These parameters are used by the hypothesis to find class of the point.

Bayes Classifier

- @time of testing we get a point $(x_j) \Rightarrow P(x_j^1, x_j^2, \dots, x_j^D / c_j^D)$ for this we need find $P(x_j / c_k) P_{ck}$ since x_j will be a combination of D dimensions thus $P(x_j / c_k)$ will be available So, find $\max P(x_j / c_k) P_{ck} \Rightarrow$ The class with max $(P(x_j / c_k) P_{ck})$ is assigned.

Bayes Optimum Classifier

- Similar to bayes classifier but here we have more than one hypothesis
 - For each hypothesis we need to find $P(x_i / c_k)P_{c_j} \Rightarrow (a^D M + M)$
 - For each hypothesis $\rightarrow (a^D M + M)$ parameters
 - At time of testing $\sum_{i=1}^H P(h_i / D)P(c_j / h_i)$
- \Rightarrow H no of hypothesis
- \Rightarrow All these parameters are used by each hypothesis to find class for given point i.e $P(c_j/h_i)$
- \Rightarrow For any given point this is calculated for each class which ever class has max value that is assigned.

Bayes Classification

$$\max[P(x_i/c_j)Pc_j]$$

- Dimension are ind
- All dimension have equal contribution

$$\max P(x_i^1 / c_j) P(x_i^2 / c_j)$$

$$P(x_i^D / c_j) Pc_j$$

Number of parameters

Naïve Bayes Classifier

Bayes Class	Naive Bayes
$P(x_j/c_j)Pc_j$	$P(x_i^1 / c_j)P(x_i^2 / c_j)...$
Probable for all combined available	$P(x_i^D / c_j)Pc_j$

Naïve Bayes Classifier

Here also we have to find $P(x_i/y_j)P_{y_j}$

$$\Rightarrow P_{y_j} \Rightarrow \frac{\# \text{ of Points of class } y_j}{\text{Total No of points}}$$

$P(x_i/y_j)$

Since x_i is data point, this has many dimension
we assume all dimension are Independent

Naïve Bayes Classifier

- we have D dimension of A values ✓
 - M No of classes.
- for each dimension (AM)
for whole data (DAM)

Problem in Naïve Bayes
Algorithm..

Topic : Bayesian Decision Theory



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes .
Rain	Mild	High	Weak	Yes .
Rain	Cool	Normal	Weak	Yes .
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Weak	Yes .
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes .
Rain	Mild	Normal	Strong	Yes .
Sunny	Mild	Normal	Strong	Yes .
Overcast	Mild	High	Strong	Yes .
Overcast	Hot	Normal	Weak	Yes .
Rain	Mild	High	Strong	No

we have to find class of
this test point

$$P_{\text{Yes}} = \frac{9}{14} \quad P_{\text{No}} = \frac{5}{14}$$

$$P[\text{Test point/Yes}] P_{\text{Yes}}$$

and

$$P[\text{Test point/No}] P_{\text{No}}$$

Topic : Bayesian Decision Theory



Test point \Rightarrow (over cast, mild, normal, weak)

In Naive Bayes we assume
all dimension are independent

$P[\text{overcast, mild, normal, weak} / \text{yes}]$

$\rightarrow P[\text{overcast} / \text{yes}] P[\text{mild} / \text{yes}] P(\text{normal} / \text{yes})$
 $P(\text{weak} / \text{yes})$
(from Training data)

we have to find class of
this test point

$$P_{\text{yes}} = \frac{9}{14} \quad P_{\text{no}} = \frac{5}{14}$$

$$P[\text{Test point} / \text{yes}] P_{\text{yes}}$$

and

$$P[\text{Test point} / \text{no}] P_{\text{no}}$$

Topic : Bayesian Decision Theory



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Weak	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

3x2

Outlook	P(P/Yes)	P(O/No)
Sunny	2/9 $P(S Y)$	3/5 $P(S No)$
Overcast	4/9 $P(O Y)$	0 $P(O No)$
Rain	3/9 $P(R Y)$	2/5 $P(R No)$

3x2

Temperature	P(T/Yes)	P(T/No)
Hot	2/9 $P(H Y)$	2/5 $P(H No)$
Mild	4/9 $P(m Y)$	2/5 $P(m No)$
Cold	3/9 $P(C Y)$	1/5 $P(C No)$

2x2

Humidity	P(H/Yes)	P(H/No)
High	3/9	4/5
Normal	6/9	1/5

2x2

Wind	P(W/Yes)	P(W/No)
Weak	6/9	2/5
Strong	3/9	3/5

Topic : Bayesian Decision Theory

Sunny Count \rightarrow $\left. \begin{matrix} 3 \text{ No} \\ 2 \text{ Yes} \end{matrix} \right\} \begin{matrix} P(S/Y) = 2/9 \\ P(S/No) = 3/5 \end{matrix}$



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny ✓	Hot	High	Weak	No
Sunny ✓	Hot	High	Strong	No
Overcast ●	Hot	High	Weak	Yes ●
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast ●	Cool	Normal	Weak	Yes ●
Sunny ✓	Mild	High	Weak	No
Sunny ✓	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny ✓	Mild	Normal	Strong	Yes
Overcast ●	Mild	High	Strong	Yes ●
Overcast ●	Hot	Normal	Weak	Yes ●
Rain	Mild	High	Strong	No

Outlook	P(P/Yes)	P(O/No)
Sunny	$2/9$ $P(S/Y)$	$3/5$
Overcast ✓	$4/9$ $P(O Y)$	0
Rain	$3/9$ $P(R Y)$	$2/5$

Temperature	P(T/Yes)	P(T/No)
Hot	$2/9$	$2/5$
Mild	$4/9$	$2/5$
Cold	$3/9$	$1/5$

Humidity	P(H/Yes)	P(H/No)
High	$3/9$	$4/5$
Normal	$6/9$	$1/5$

Wind	P(W/Yes)	P(W/No)
Weak	$6/9$	$2/5$
Strong	$3/9$	$3/5$

Topic : Bayesian Decision Theory



Overcast : 4 Yes
0 No | $P(O/Y) = \frac{4}{9}$
 $P(O/No) = 0/5$

Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny ✓	Hot	High	Weak	No
Sunny ✓	Hot	High	Strong	No
Overcast •	Hot	High	Weak	Yes •
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast •	Cool	Normal	Weak	Yes •
Sunny ✓	Mild	High	Weak	No
Sunny ✓	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny ✓	Mild	Normal	Strong	Yes
Overcast •	Mild	High	Strong	Yes •
Overcast •	Hot	Normal	Weak	Yes •
Rain	Mild	High	Strong	No

Outlook	P(P/Yes)	P(O/No)
Sunny •	$\frac{2}{9} P(S Y)$	$\frac{3}{5}$ •
Overcast ✓	$\frac{4}{9} P(O Y)$ •	0 •
Rain •	$\frac{3}{9} P(R Y)$ •	$\frac{2}{5}$ •

Temperature	P(T/Yes)	P(T/No)
Hot	$\frac{2}{9}$	$\frac{2}{5}$
Mild	$\frac{4}{9}$	$\frac{2}{5}$
Cold	$\frac{3}{9}$	$\frac{1}{5}$

Humidity	P(H/Yes)	P(H/No)
High •	$\frac{3}{9}$	$\frac{4}{5}$
Normal •	$\frac{6}{9}$	$\frac{1}{5}$

Wind	P(W/Yes)	P(W/No)
Weak	$\frac{6}{9}$	$\frac{2}{5}$
Strong	$\frac{3}{9}$	$\frac{3}{5}$

Topic : Bayesian Decision Theory



$$\text{Rain} = \begin{matrix} 3 \text{ Yes} \\ 2 \text{ No} \end{matrix} \mid \begin{matrix} P(R|Y) = 3/9 \\ P(R|No) = 2/5 \end{matrix}$$

Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny ✓	Hot	High	Weak	No
Sunny ✓	Hot	High	Strong	No
Overcast ●	Hot	High	Weak	Yes ●
Rain ●	Mild	High	Weak	Yes ✓
Rain ●	Cool	Normal	Weak	Yes ✓
Rain ●	Cool	Normal	Strong	No ✗
Overcast ●	Cool	Normal	Weak	Yes ●
Sunny ✓	Mild	High	Weak	No
Sunny ✓	Cool	Normal	Weak	Yes
Rain ●	Mild	Normal	Strong	Yes ✓
Sunny ✓	Mild	Normal	Strong	Yes
Overcast ●	Mild	High	Strong	Yes ●
Overcast ●	Hot	Normal	Weak	Yes ●
Rain ●	Mild	High	Strong	No ✓

Outlook	P(P/Yes)	P(O/No)
Sunny	2/9 P(S Y)	3/5
Overcast	4/9 P(O Y)	0
Rain	3/9 P(R Y)	2/5

Temperature	P(T/Yes)	P(T/No)
Hot	2/9	2/5
Mild	4/9	2/5
Cold	3/9	1/5

Humidity	P(H/Yes)	P(H/No)
High	3/9	4/5
Normal	6/9	1/5

Wind	P(W/Yes)	P(W/No)
Weak	6/9	2/5
Strong	3/9	3/5

Topic : Bayesian Decision Theory

High $P(H/Y) = 3/9$
 $P(H/No) = 4/5$

Normal $P(N/Y) = 6/9$ | $P(N/No) = 1/5$



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Weak	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

Outlook	P(P/Yes)	P(O/No)
Sunny	$2/9 P(S Y)$	$3/5$
Overcast	$4/9 P(O Y)$	0
Rain	$3/9 P(R Y)$	$2/5$

Temperature	P(T/Yes)	P(T/No)
Hot	$2/9$	$2/5$
Mild	$4/9$	$2/5$
Cold	$3/9$	$1/5$

Humidity	P(H/Yes)	P(H/No)
High	$3/9$	$4/5$
Normal	$6/9$	$1/5$

Wind	P(W/Yes)	P(W/No)
Weak	$6/9$	$2/5$
Strong	$3/9$	$3/5$

Test = (O, M, N, w) \Leftarrow Yes.

$P(O, m, N, w / \text{Yes}) P_{\text{Yes}}$

$P(O/Y) P(M/Y) P(N/Y) P(w/Y) P_Y$

$\left(\frac{4}{9} \times \frac{4}{9} \times \frac{6}{9} \times \frac{6}{9} \times \frac{9}{14} \right)$

$P(O, m, N, w / \text{No}) P_{\text{No}}$

$P(O/N) P(M/N) P(N/\text{No}) P(w/\text{No}) P_{\text{No}}$

○

Topic : Bayesian Decision Theory



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Weak	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

Outlook	$P(P/Yes)$	$P(O/No)$
Sunny	$2/9 P(S Y)$	$3/5$
Overcast	$4/9 P(O Y)$	0
Rain	$3/9 P(R Y)$	$2/5$

Temperature	$P(T/Yes)$	$P(T/No)$
Hot	$2/9$	$2/5$
Mild	$4/9$	$2/5$
Cold	$3/9$	$1/5$

Humidity	$P(H/Yes)$	$P(H/No)$
High	$3/9$	$4/5$
Normal	$6/9$	$1/5$

Wind	$P(W/Yes)$	$P(W/No)$
Weak	$6/9$	$2/5$
Strong	$3/9$	$3/5$

$$2 + \alpha/9 + 3\alpha$$

$$4 + \alpha/9 + 3\alpha$$

$$3 + \alpha/9 + 2\alpha$$

$$P(O, M, N, w/\text{yes}) P_{\text{yes}} \Rightarrow P(O/Y) P(M/Y) P(N|Y) P(W/Y) P_Y$$

$$\Rightarrow \left(\frac{4}{9} \times \frac{4}{9} \times \frac{6}{9} \times \frac{6}{9} \times \frac{9}{14} \right)$$

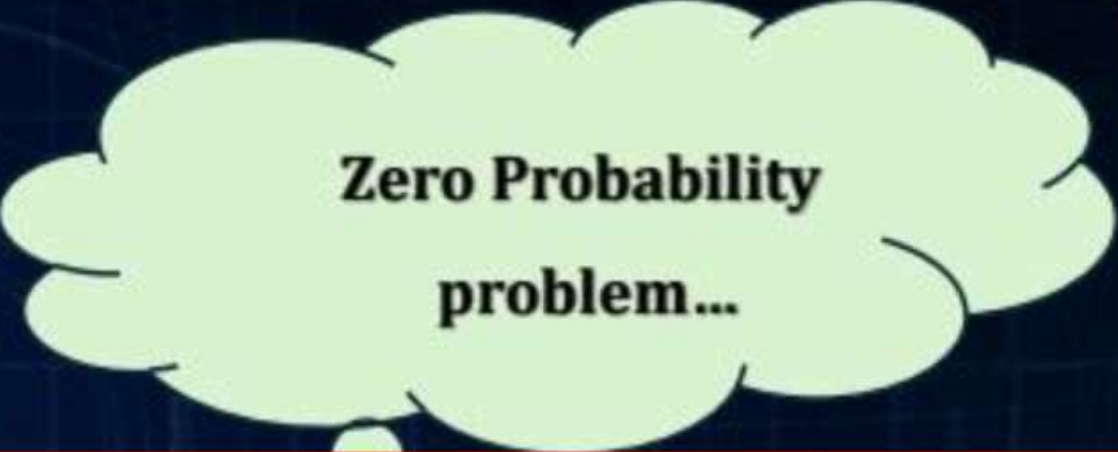
$$P(O, M, N, w/\text{yes}) P_{\text{yes}} \Rightarrow P(O/N) P(M/N) P(N|N) P(W/N) P_N$$

$$\Rightarrow 0 \times \dots \dots \dots \Rightarrow 0$$

- Since $P(\text{over cost no}) = 0$
- Thus, in naïve bayes if any test point has 1st dimension = over cost then $P(x_i/\text{No})P_{N_p} = 0$ and test point \rightarrow Yes class always

Navive Bayes Algorithm

- This is called zero probable problem
- Reason → Because in whole training data no data point with class no has dimension 1 = over cast



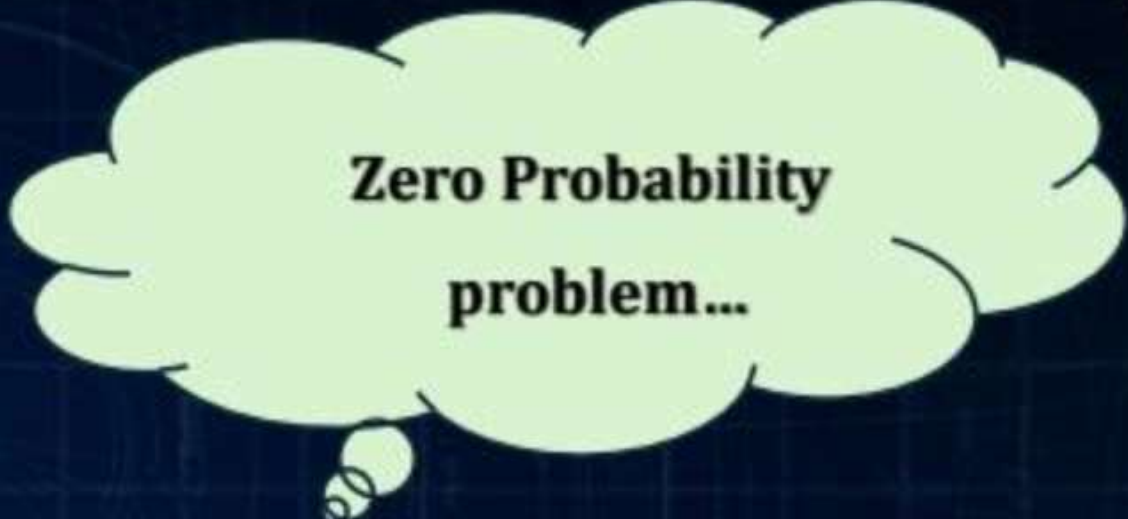
Zero Probability
problem...

Navive Bayes Algorithm

Solution to zero probable problem \Rightarrow

2 solutions

1. inc the data
2. add the arbitrary points \rightarrow smoothening process ✓



Zero Probability
problem...

Navive Bayes Algorithm

Solving the zero
probability problem..

- Smoothing techniques,
adding virtual entries..
- Additional data...

1st dimension

Yes

$$\begin{aligned}P(S/Y) &= 2/9 \\ P(O/Y) &= 4/9 \\ P(R/Y) &= 3/9\end{aligned}$$

S
S
O
O
O
O
R
R
R
R

No

$$\begin{aligned}P(S/N) &= \frac{3}{5} \\ P(R/N) &= \frac{2}{5} \\ P(O/N) &= 0\end{aligned}$$

S
S
S
R
R
R



Smoothing by α

1st dimension
Yes

$$P(S/Y) = \frac{2+\alpha}{9+3\alpha}$$

$$P(O/Y) = \frac{4+\alpha}{9+3\alpha}$$

$$P(R/Y) = \frac{2+\alpha}{9+3\alpha}$$

S
S
O
O
O
O
R
R
R

α times
S, R, O

No

S
S
S
R
R
R

α times S
 α times R
 α times O

$$P(S/N) = \frac{3+\alpha}{5+3\alpha}$$

$$P(R/N) = \frac{2+\alpha}{5+3\alpha}$$

$$P(O/N) = \frac{\alpha}{5+3\alpha}$$

if smoothing is done in
any dimension

$$P(s/y) = \frac{2}{9} \longrightarrow \frac{2+\alpha}{9+3\alpha}$$

3: bcoz dimension has 3 values.

$$P(s/No) = \frac{3}{5} \longrightarrow \frac{3+\alpha}{5+3\alpha}$$

Topic : Bayesian Decision Theory



After smoothing new probable $\Rightarrow \frac{\text{Old value } \alpha}{\text{Old value } k\alpha}$
K = number of values a dimension can take

3rd dimension

H
H
H
N
N
N
N
N
N
...
...
...

$$\rightarrow P(H|Y) = \frac{3 + \alpha}{9 + 2\alpha}$$

$$\rightarrow P(N|Y) = \frac{6 + \alpha}{9 + 2\alpha}$$

Topic : Bayesian Decision Theory



Test point \Rightarrow (over cast, mild, normal, weak)

Outlook	Temperature	Humidity	Wind	Play tennis
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Weak	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Strong	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

Outlook	P(O/Yes)	P(O/No)
Sunny	$\frac{2}{9} \Rightarrow \frac{2 + \alpha}{9 + 3\alpha}$	$\frac{3}{5} \Rightarrow \frac{3 + \alpha}{5 + 3\alpha}$
Overcast	$\frac{4}{9} \Rightarrow \frac{4 + \alpha}{9 + 3\alpha}$	$\frac{0}{5} \Rightarrow \frac{0 + \alpha}{5 + 3\alpha}$
Rain	$\frac{3}{9} \Rightarrow \frac{3 + \alpha}{9 + 3\alpha}$	$\frac{2}{5} \Rightarrow \frac{2 + \alpha}{5 + 3\alpha}$

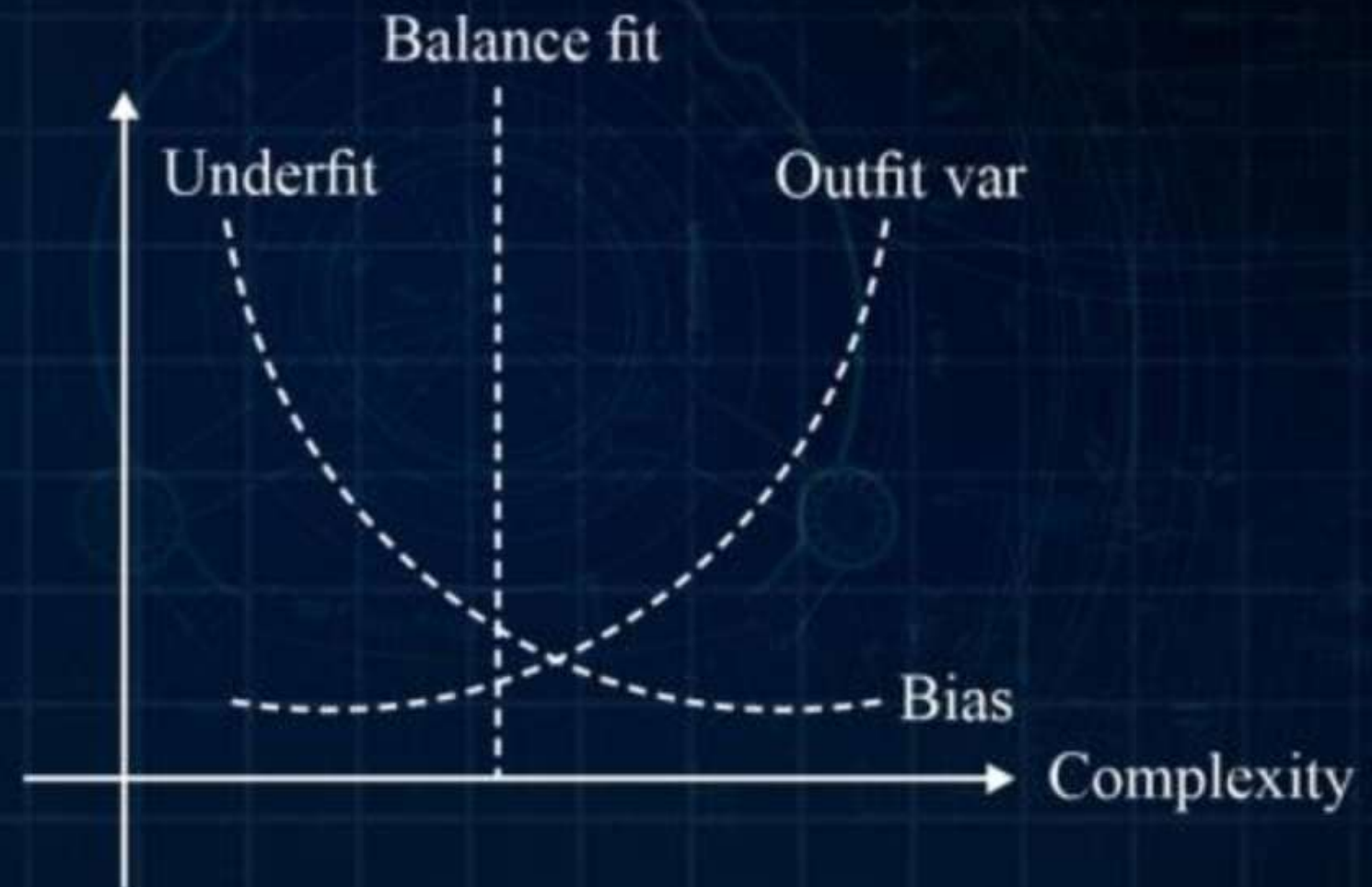
Temperature	P(T/Yes)	P(T/No)
Hot	$\frac{2}{9} = \frac{2 + \alpha}{9 + 3\alpha}$	$\frac{2}{5} = \frac{2 + \alpha}{5 + 3\alpha}$
Mild	$\frac{4}{9}$	$\frac{2}{5}$
Cold	$\frac{3}{9}$	$\frac{1}{5}$

Humidity	P(H/Yes)	P(H/No)
High	$\frac{3}{9} \Rightarrow \frac{3 + \alpha}{9 + 2\alpha}$	$\frac{4}{5} \Rightarrow \frac{4 + \alpha}{5 + 2\alpha}$
Normal	$\frac{6}{9} \Rightarrow \frac{6 + \alpha}{9 + 2\alpha}$	$\frac{1}{5} \Rightarrow \frac{1 + \alpha}{5 + 2\alpha}$

Topic : Bayesian Decision Theory



Laplace Smoothing \Rightarrow Mean $\alpha = 1$



$\alpha = 0$ ✓	$\alpha = 0$	$\alpha \Rightarrow$ Very large	
Fitting \Rightarrow	Overfit ✓	Balance fit	Underfitting ✓
Bias \Rightarrow	Low ✓	Low	High
Variance \Rightarrow	High ✓	Low	Low

- How to solve for continuous dimension in naive bayes.

In this case $P(x_i|c_j)P_{c_j}$

$$\left(P\left(x_i^1 / C_j \right) \dots P_{C_j} \right)$$

What if the dimension are continuous in nature

$$P(S|Y) = 2/9$$

$$P(O|Y) = 4/9$$

$$P(R|Y) = 3/9$$

$$P(S|N) = 3/5$$

$$P(O|Y) = 0$$

$$P(R|N) = 2/5$$

Topic : Bayesian Decision Theory



Naïve Bayes Algorithm

What if the dimension are continuous in nature

The numeric weather data with summary statistics

Outlook	Temperature		Windily		Play	
	Yes	No	Yes	No	Yes	No
Sunny	2	3	83	85	9	5
Overcast	4	0	70	80		
Rainy	3	2	68	65		
			64	72		
			69	71		

mean $\Rightarrow 70.8$
var $\Rightarrow 41.36$

$\mu = 74.6$
 $\sigma^2 = 49.84$

$$\begin{aligned}
 &P(S/Y) = 2/9 \quad P(R/Y) = 3/9 \\
 &P(S/N) = 3/5 \quad P(R/N) = 2/5 \\
 &P(O/Y) = 4/9 \\
 &P(O/N) = 0 \\
 &P(T/Y) = N(70.8, 41.36) \\
 &P(T/N) = N(74.6, 49.84)
 \end{aligned}$$

$$\begin{aligned}
 P(F/Y) &= \frac{6}{9} \\
 P(F/N) &= \frac{2}{5} \\
 P(T/Y) &= \frac{3}{9} \\
 P(T/N) &= \frac{3}{5}
 \end{aligned}$$

$$\begin{aligned}
 P_Y &= 9/14 \\
 P_N &= 5/14
 \end{aligned}$$

- Find class of (Sunny, 78, ~~78~~, true)

$$P[S, 78, T/Yes] P_{Yes}$$

$$P(S/Y) P(78/Y) P(T/Y) P_Y$$

$$\frac{2}{9} \times \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \times \frac{3}{9} \times \frac{9}{14}$$

$\frac{1}{\sqrt{2\pi\sigma^2}} \rightarrow 41.36$
 $\frac{(x-\mu)^2}{2\sigma^2} \rightarrow 70.8$
 $= 0.03314$

$$P[S, 78, T/No] P_{No}$$

$$P(S/N) P(78/N) P(T/N) P_{No}$$

$$\frac{3}{5} \times \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \times \frac{3}{5} \times \frac{5}{14}$$

$\frac{1}{\sqrt{2\pi\sigma^2}} \rightarrow 49.8$
 $\frac{(x-\mu)^2}{2\sigma^2} \rightarrow 74.6$
 $= 0.503 \checkmark$

Topic : Bayesian Decision Theory

Naïve Bayes Algorithm

The numeric weather data with summary statistics											
Outlook			Temperature		Humidity		Windy			Play	
	Yes	No	Yes	No	Yes	No		Yes	No	Yes	No
Sunny	2	3	83	85	86	85	False	6	2	9	5
Overcast	4	0	70	80	96	90	True	3	3		
Rainy	3	2	68	65	80	70					
			64	72	65	95	$\rightarrow \Sigma = 86.2$				
			69	71	70	91	$\sigma^2 = 75.76$				
			75	↓	80						
			75	$\Sigma=74.6$	70						
			72	$\sigma^2 = 49.84$	90	$\rightarrow \text{mean} = 79.11$					
			81		75	$\rightarrow \sigma^2 = 72.76$					

- PDF of temp and Humidity \Rightarrow

$$P(T/Y) \Rightarrow \frac{1}{\sqrt{2\pi \times 34.66}} e^{\frac{-(x-73)^2}{2 \times 34.66}}$$

$$P(T/N) \Rightarrow \frac{1}{\sqrt{2\pi \times 49.84}} e^{\frac{-(x-74.6)^2}{2 \times 49.84}}$$

$$P(h/Y) \Rightarrow \frac{1}{\sqrt{2\pi \times 92.76}} e^{\frac{-(x-79.11)^2}{2 \times 92.76}}$$

$$P(h/N) \Rightarrow \frac{1}{\sqrt{2\pi \times 75.76}} e^{\frac{-(x-86.2)^2}{2 \times 75.76}}$$

Topic : Basic of Machine Learning

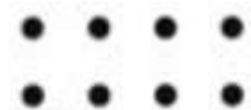


The numeric weather data with summary statistics

Outlook			Temperature		Humidity		Windly			Play	
	Yes	No	Yes	No	Yes	No		Yes	No	Yes	No
Sunny	2	3	83	85	86	85	False	6	2	9	5
Overcast	4	0	70	80	96	90	True	3	3		
Rainy	3	2	68	65	80	70					
			64	72	65	95					
			69	71	70	91					
			75		80						
			75		70						
			72		90						
			81		75						

A thick yellow arrow pointing to the right, positioned above the word 'Thank'.

Thank
THANK



Keep Hustling!