

GATE

CRASH COURSE

ALL BRANCH

Subject

General Aptitude

Numbers (Lec 01)

By – Amulya Ratan Sir



Topics *to be covered*

- 1 Number Calculations
- 2 Unit Digit ✓
- 3 Divisibility Rule ✓
- 4 Questionnaire





Number System



Logical

Question

Evaluate:

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1 - \frac{1}{2}}}}$$

$$= \frac{1}{1 + \frac{1}{1 + \frac{1}{\frac{1}{2}}}}$$

$$= \frac{1}{1 + \frac{1}{1 + 2}}$$

$$= \frac{1}{1 + \frac{1}{3}}$$

$$= \frac{1}{\frac{4}{3}}$$

$$= \frac{3}{4}$$

$$1 + \frac{1}{3} = \frac{3+1}{3}$$

(A) $\frac{4}{5}$

(B) $\frac{3}{4}$

(C) $\frac{3}{5}$

(D) None

$$1 \div \frac{1}{2} = 1 \times \frac{2}{1}$$

Question

What would the unit digit in the answer of given expression:

$$1! + 2! + 3! + \dots + 2025!$$

$$\begin{aligned} 1! &= 1 \\ 2! &= 2 \end{aligned}$$

$$3! = 6$$

$$4! = 24$$

$$5! = 120$$

$$\begin{array}{r} 120 \\ \times 6 \\ \hline 720 \end{array}$$

$$\begin{array}{r} 720 \\ \times 7 \\ \hline 5040 \end{array}$$

$$13$$

- (A) 0
(B) 3
(C) 5
(D) 9

Question

What would the remainder when the answer of given expression is divided by 3?

$$1! + 2! + 3! + \dots + 2025! = \underline{\underline{\text{Ans}}}$$

A 2

B 0

C 1

D Indeterminable

$$R = \underline{\underline{0}}$$

3) Ans (

$$\begin{array}{r} 4 \\ \hline R = 1 \end{array}$$

$R = ?$

Question



5 apples, 6 oranges and 7 bananas cost ₹ 250, while 6 apples, 4 oranges and 2 bananas cost ₹180. The cost (in ₹) of 4 oranges and 8 bananas is

A 210

C 180

D Indeterminable

$$(5A + 6O + 7B = 250) \times 6$$

$$(6A + 4O + 2B = 180) \times 5$$

$$\underline{\underline{4O + 8B = 150}}$$

$$30A + 360 + 42B = 1500$$

$$30A + 200 + 10B = 900$$

$$\underline{\underline{160 + 32B = 600}} \div 4$$

Question

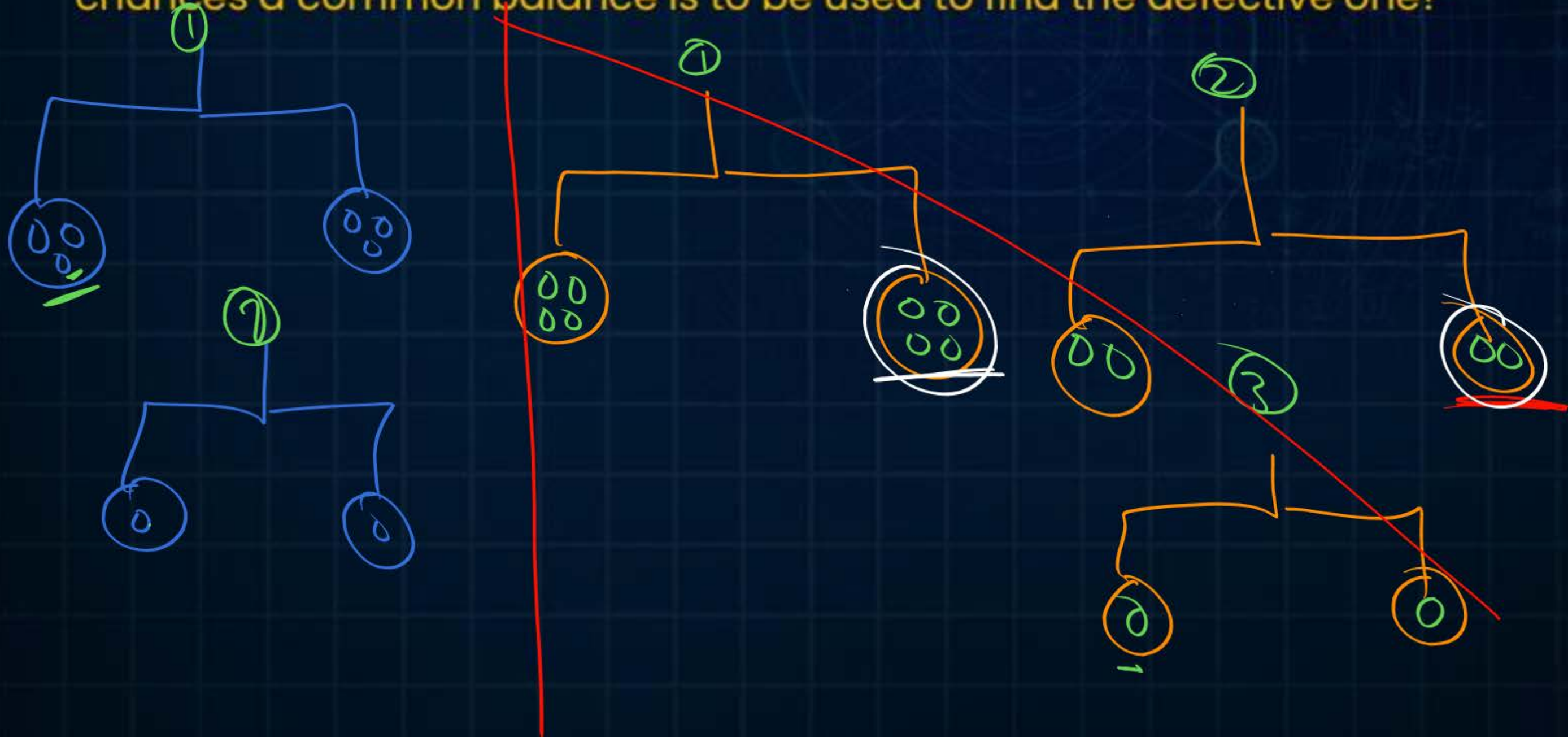
✓ Case 1 =
Case 2 ≠ 2 chance

18

6 balls



There are 8 balls of which one is defective. Given that the defective ball is of less weight and remaining are of equal weights. What are the minimum number of chances a common balance is to be used to find the defective one?



Question



A bag consist of 48 ^① red colour balls, 16 ^② green colour balls, 12 yellow colour balls, 11 ^④ black colour balls and 11 ^⑤ white colour balls. How many minimum number of balls are to be taken out from the bag randomly so that we get at least two balls of same colour?

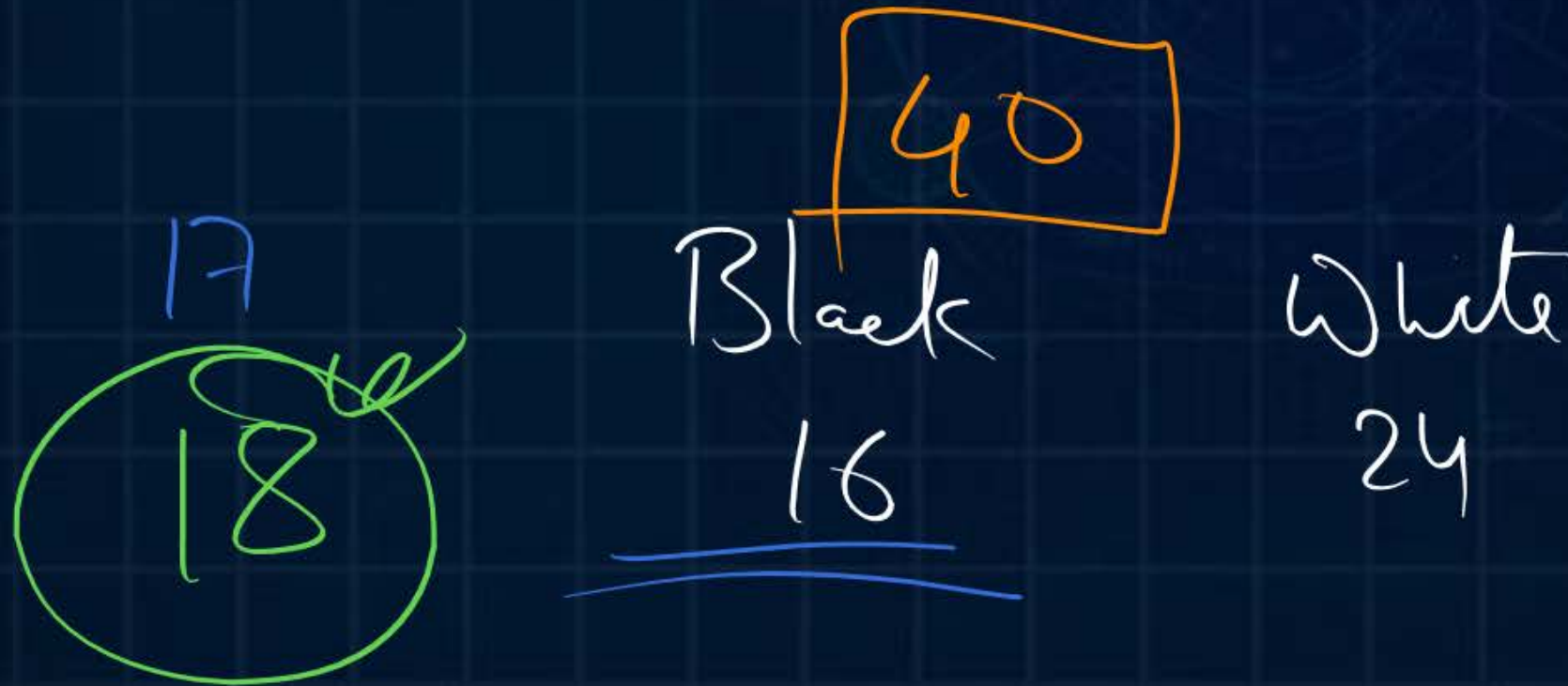
(blind folded)

6 balls

Question



A shelf consist of 40 socks. 40% of these are black and remaining are white. How many minimum number of socks are to taken out from the shelf randomly (blindly), so that we get at least two white socks?



Question



A box consist of 40 pairs of shoes of equal size. 40% of these are black and remaining are white. How many minimum number of shoes are to taken out from the box randomly, so that we get at least a pair of black shoes?

A 50

B 65 ✓

C 52

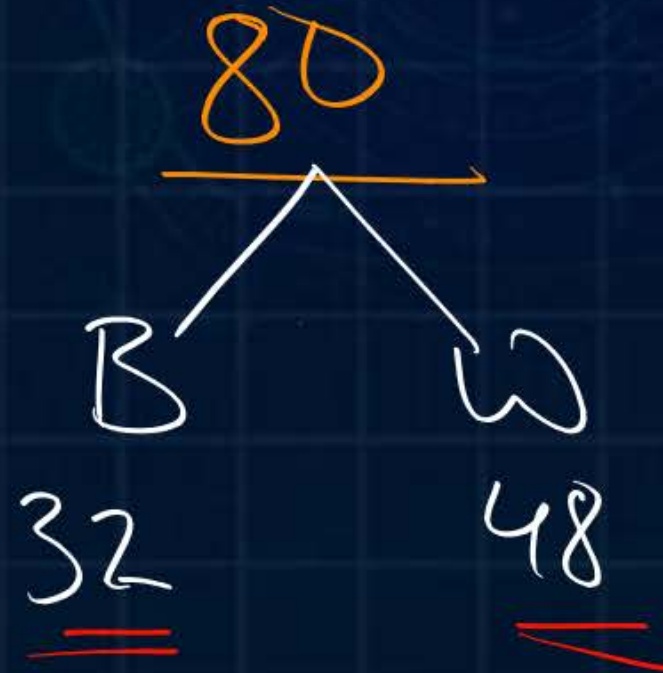
D 34

+ 48 ✓

+ 16 ✓

1 ✓

65 ✓



Question

How many zeroes would be at the end in the answer of $50!$?

12 zeroes

$$1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \dots 50$$

$$50 \times 49 \times 48 \dots 1$$

A 12

B 15

C 23

D 24

$$\begin{aligned} 1-10 &\rightarrow 2 \\ 11-20 &\rightarrow 2 \\ 21-30 &\rightarrow 3 \\ 31-40 &\rightarrow 2 \\ 41-50 &\rightarrow 3 \end{aligned}$$

$$\begin{array}{rcl} \frac{50}{5} & \rightarrow & 10 \\ \frac{10}{5} & \rightarrow & 2 \\ \frac{2}{5} & \rightarrow & 0 \\ \hline & & 12 \end{array}$$

Question

If $123!$ can be denoted maximum 7^x , then the value of x is?

$$\frac{123}{7} \rightarrow 17$$

$$\frac{17}{7} \rightarrow 2$$

$$\frac{2}{7} \rightarrow 0$$

19

$$123! \rightarrow 7^{19}$$

A

17

B

16

C

22

D

19

Question



$$5 \rightarrow \underline{\underline{12}} \quad 2 \rightarrow \underline{\underline{8}}$$

Find the number of zeroes in following multiplication:

$$5 \times 10 \times 15 \times 20 \times 25 \dots \times 50$$

$$5 \times 1 \times 5 \times 2 \times 5 \times 3 \times 5 \times 4 \dots \times 5 \times 10$$

$$= \underline{\underline{5^{10}}} \times \underline{\underline{10!}}$$

$$\text{B } 8$$

$$\text{D } 24$$

$$\frac{10}{5} = 2$$
$$\frac{2}{2} = 1$$

$$\frac{10}{2} = 5$$
$$\frac{5}{2} = 2$$
$$\frac{2}{2} = 1$$

$$\text{A } 12$$

$$\text{C } 48$$

Question



Which of the following correspond to x, y and z, respectively in the following square where sum of elements in each column, row, and diagonal is the same?

A (17, 15, 13)

B (18, 15, 12)

C (12, 15, 17)

D (17, 16, 14)

16	11	x ¹⁸
17	y ¹⁵	13
z	19	14

= 45

= 45

Question



If the difference between the two-digit numbers made from digits a and b is 27, the difference between a and b is ?

A 2

C 1

$$\begin{array}{cc} \text{'a'} & \text{'b'} \\ \boxed{10a + b} - \boxed{10b + a} = 27 \end{array}$$

B 4

D 3

$$\Rightarrow 10a + b - 10b - a = 27$$

$$\Rightarrow 9a - 9b = 27$$

$$9(a - b) = 27$$

$$\therefore a - b = \frac{27}{9} = \underline{\underline{3}}$$

$$\begin{array}{r} \underline{46} \\ 4 \times 10 + 6 + 1 = 46 \end{array}$$

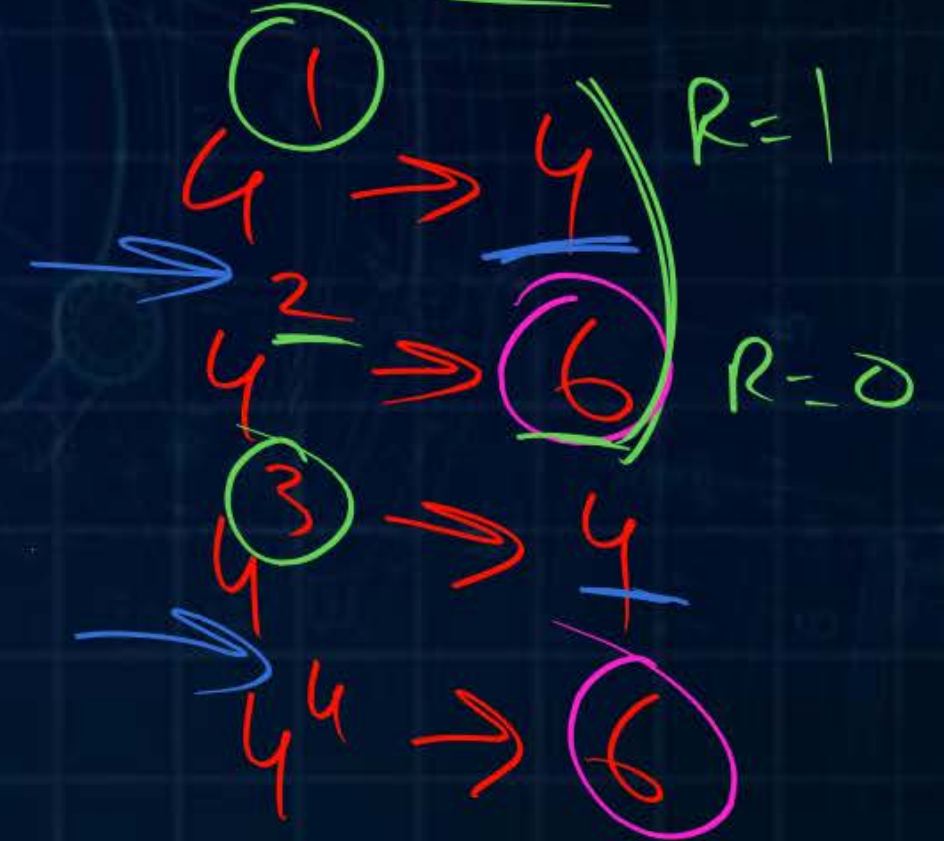
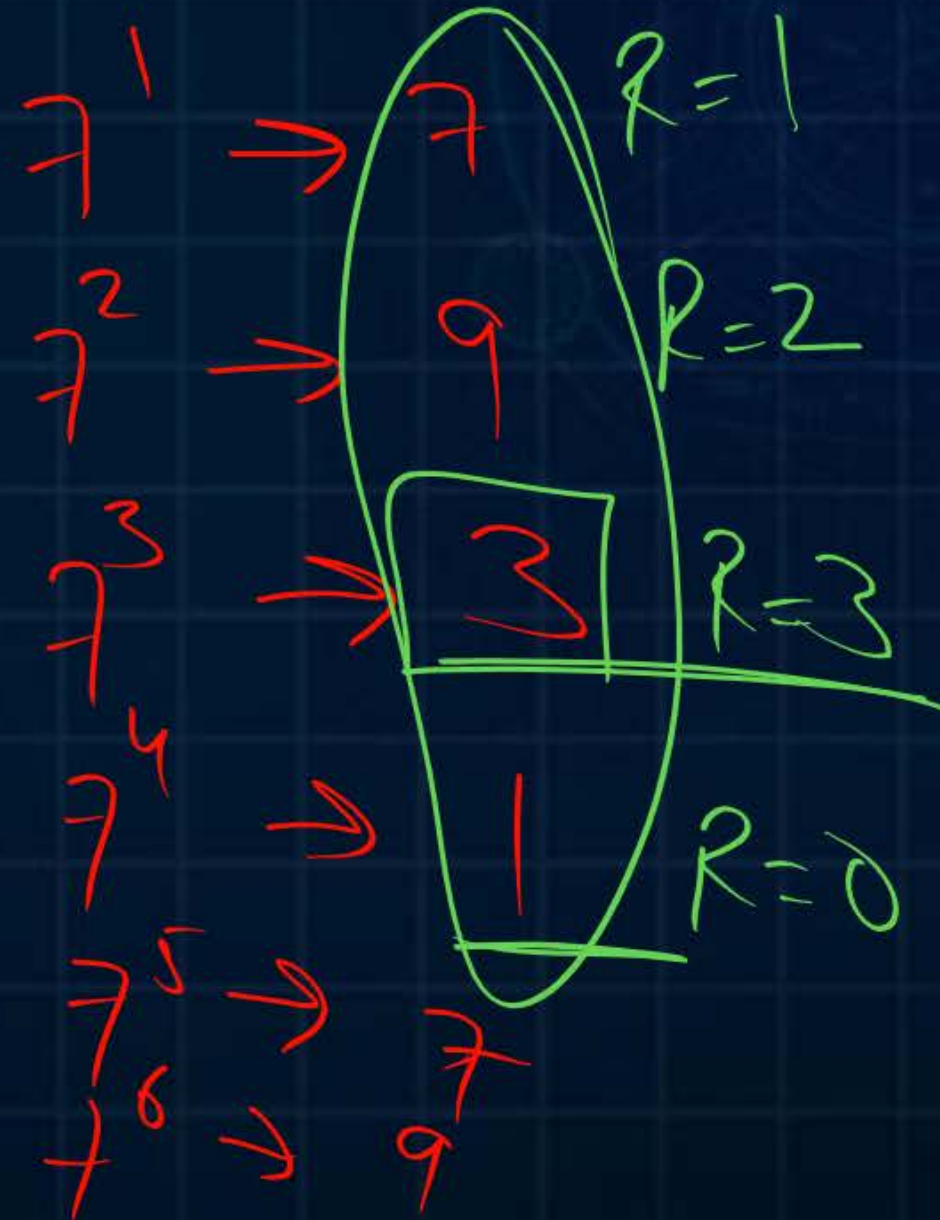
Question

What would be the unit digit in the answer of:

$$\begin{array}{r} 49 \\ \times 7 \\ \hline \end{array}$$

$$\begin{array}{r} 2367^{911} + 1414^{216} \\ \hline \end{array}$$

$$3 + 6 = 9$$



Question

What would be the unit digit in the answer of:

$$\underline{2913}^{1902} + \underline{1647}^{460} \quad ?$$

$$9 + 1 = 10$$

$$\begin{array}{l} 3^1 \rightarrow 3 \\ 3^2 \rightarrow 9 \\ 3^3 \rightarrow 7 \\ 3^4 \rightarrow 1 \\ 3^5 \rightarrow 3 \end{array} \quad \begin{array}{c} \text{---} \\ R=2 \end{array}$$

$$\begin{array}{l} 7^1 \rightarrow 7 \\ 7^2 \rightarrow 9 \\ 7^3 \rightarrow 3 \\ 7^4 \rightarrow 1 \end{array} \quad \begin{array}{c} \text{---} \\ R=0 \end{array}$$

A

0

B

2

C

3

D

5

Question



What would be the unit digit in the answer of:

$$\boxed{9326}^{397} + 147\underline{5}^{363}$$

$$6 + 5$$

$$= \underline{11}$$

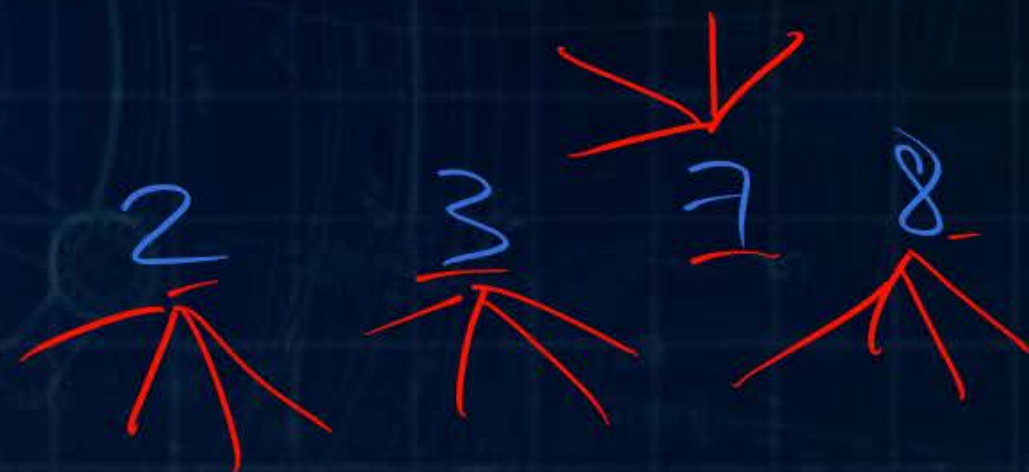
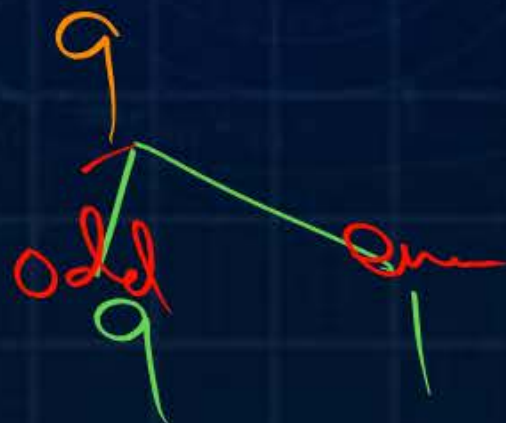
✓
0

✓
1

✓
5

✓
6

abcd ^{par}





Divisibility Rule:



$$\times 68 \overline{29} \mid = 26$$

A 2

0 OR Multiple of 2
2, 4, 6, 8

B 3

Sum of digits should be divisible by 3.

$$\underline{\underline{8}} = 2^{\textcircled{3}}$$

C 4

000 OR Multiple of 8

00 OR Multiple of 4

✓ **D** 5

→ 0 OR Multiple of 5



Divisibility Rule:

A 6 = 2×3

B 7

C 8 $\rightarrow 2^3$

D 9 \rightarrow Sum of digit.

$125 = 5 \times \textcircled{3}$

\downarrow

48965

000

OR

000 OR Multiple of 125

Multiple of 8

① Any two consecutive

② Any two distinct
Prime No.

Co-prime

✓ 27 → 1, 3, 9, 27

✓ 4 → 1, 2, 4

~~16~~ → ~~1, 2, 4, 8, 16~~

~~28~~ → ~~1, 2, 4, 7, 14, 28~~



Divisibility Rule:



A 10

B 11

C 12

D 14

$$\begin{array}{cccccc} & 8 & + & 3 & = & 11 \\ & | & & | & & \\ \times & 9 & 8 & 6 & 3 & 2 \\ & | & & | & & | \\ & 9 & + & 6 & + & 2 & = & 17 \end{array}$$

6

difference between sum of odd place digits &

even place digits should be 0 or multiple of 11



Divisibility Rule:

A

15

3×5

B

16



$2^{\textcircled{4}}$

○○○○○ OR Multiple of 16

C

18



2×9

D

20,

$\rightarrow 4 \times 5$

40,

$\rightarrow 5 \times 8$

80,

$\rightarrow 16 \times 5$
etc....

Question

Which largest number of 5 digits is divisible by 99 ?

A 99990

B 99981

C 99909

D 99999

$$\begin{array}{r} 11 \times 9 \\ \hline \end{array}$$

$$\begin{array}{r} 18 \\ 18 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 19 \\ 17 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 27 \\ 18 \\ \hline 9 \end{array}$$

$$\begin{array}{r} 27 \\ 18 \\ \hline 9 \end{array}$$

Question



Find the least perfect cube divisible by 2, 3, 4 and 6.

A

216

C

1728

B

~~512~~

D

~~360~~

12

Question (PYQ GATE Exam 2024 CE/CH)

In the 4×4 array shown below, each cell of the first three columns has either a cross (X) or a number, as per the given rule.

Rule: The number in a cell represents the count of crosses around its immediate neighboring cells (left, right, top, bottom, diagonals).

As per this rule, the maximum number of crosses possible in the empty column is

A 3

B 1

C 0

D 2

1	1	2	X
2	X	3	X
2	X	4	X
1	2	X	X

Question (PYQ GATE Exam 2019 CS)



Ten friends planned to share equally the cost of buying a gift for their teacher. When two of them decided not to contribute, each of the other friends had to pay Rs. 150 more. The cost of the gift was Rs_____

$$T = 2x \Rightarrow 6000$$

$$\frac{x}{8} - \frac{x}{10} = 150$$

A 12000

B 666

C 6000

D 3000

$$\frac{x}{10}$$

$$\frac{x}{8}$$



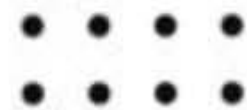
Summary



Numbers

The word 'Thank' is written in a large, yellow, cursive script. A yellow arrow starts at the top of the 'T', extends horizontally to the right, and then curves downwards to point at the end of the word.

THANK



Keep Hustling!