the improbable, yet elementary, case: making sense of an incoherent species, by deriving, and applying, the common primitives, of a coherent universe - @causalmechanics 1 - 2023-03-09

1 paradigm, measure, common measures, incommensurability

$$(Pa, Me, \bigcap_{Me}, \bigcap_{Me})$$

A reinterpretation of Thomas Kuhn's 'On The Structure of Scientific Revolutions', through the lens of set-theory(-ish) mathematics.

. . .

note: consider all set-theory as pseudo-set-theory; a means for a novice mathematician to express ideas in less time and fewer words than a similarly novice writer might, in prose ².

1.1 a gentle introduction

(Pa, Me) introducing paradigm and measure

Let us consider a paradigm Pa, as a set of measures Me:

$$Pa = \{Me, \ldots\}$$

or 3 :

$$Pa = \{\ldots\}_{Me}$$

. .

1.2 totality, commonality

 (\cup, \cap) introducing all, and common

If paradigm Pa_1 , contains measures $Me_{1,2,3}$:

$$Pa_1 = \{Me_1, Me_2, Me_3\}$$

And paradigm Pa_2 , contains measures $Me_{2,3,4}$:

$$Pa_2 = \{Me_2, Me_3, Me_4\}$$

. . .

The set-of-all measures \bigcup_{Me} , across Pa_1 and Pa_2 , can be found by union \cup :

$$_{Me}^{\cup_{1,2}}=Pa_{1}\cup Pa_{2}=\{Me_{1},Me_{2},Me_{3},Me_{4}\}$$

. . .

The set-of-common measures \bigcap_{Me} , between Pa_1 and Pa_2 , can be found by intersection \cap :

$$\bigcap_{Me}^{\cap_{1,2}} = Pa_1 \cap Pa_2 = \{Me_2, Me_3\}$$

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note: remember, this is a simplification, and an introduction

¹mastodon — twitter

 $^{^2 {\}rm all}$ terms are tentative. corrections $\land \lor$ advice, welcome.

³is this alternate form acceptable?

1.3 cardinality

(n) counting elements

The cardinality of any set, refers to the number of contained elements, expressed $|\{...\}| = n$.

So where:

$$A = \{a, b, c\}$$

cardinality is:

$$|A| = 3$$

. . .

1.4 incommensurability

 $(\cap \varnothing)$ introducing incommensurable paradigms ⁴

Consider paradigms Pa_3 and Pa_4 , whereby:

$$Pa_3 = \{Me_1, Me_2, Me_3\}$$

$$Pa_4 = \{Me_4, Me_5, Me_6\}$$

. . .

When paradigms Pa_3 and Pa_4 , do not share common measures, then \bigcap_{Me} , is an empty set ({} or \varnothing):

$$_{Me}^{\cap} = Pa_3 \cap Pa_4 = \varnothing$$

$$_{Me}^{\cap_{3,4}}=\varnothing$$

. .

and paradigms Pa_3 and Pa_4 , can be said to be incommensurable $\frac{\cap \varnothing}{Me}$:

$$_{Me}^{\cap} = Pa_3 \cap Pa_4 = \varnothing : _{Me}^{\cap} \to _{Me}^{\cap \varnothing}$$

$$|Pa_3 \cap Pa_4| = |\varnothing| = |^{\cap \varnothing_{3,4}}_{Me}| = 0$$

. . .

note: while any two paradigms may appear incommensurable as an isolated pair ⁵, we will later discover that there exists a universally special paradigm, which by analysis or composition, renders all paradigms reconcilable, and as such, commensurable

⁴famously, two paradigms which share no common measures are incommensurable.

⁵from an unified scientific endeavour