

the improbable, yet elementary, case: *making sense of an incoherent species, by deriving, and applying, the common primitives, of a coherent universe* - @causalmechanics <sup>1</sup> - 2023-03-09

# 1 paradigm, measure, common measures, incommensurability

$(Pa, Me, \bigcap_{Me}, \bigcap_{\emptyset})$

A reinterpretation of Thomas Kuhn's 'On The Structure of Scientific Revolutions', through the lens of set-theory(-ish) mathematics.

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*note: consider all set-theory as pseudo-set-theory; a means for a novice mathematician to express ideas in less time and fewer words than a similarly novice writer might, in prose* <sup>2</sup>.

## 1.1 a gentle introduction

$(Pa, Me)$

Let us consider a paradigm  $Pa$ , as a set of two measures  $Me_1$  and  $Me_2$ :

$$Pa = \{Me_1, Me_2\} : |Pa| = 2$$

...

## 1.2 totality, commonality

$(\cup, \cap)$

If paradigm  $Pa_1$ , contains measures  $Me_{1,2,3}$ :

$$Pa_1 = \{Me_1, Me_2, Me_3\}$$

And paradigm  $Pa_2$ , contains measures  $Me_{2,3,4}$ :

$$Pa_2 = \{Me_2, Me_3, Me_4\}$$

...

The *set-of-all* measures  $\bigcup_{Me}$ , across  $Pa_1$  and  $Pa_2$ , can be found by union  $\cup$ :

$$\bigcup_{Me} = Pa_1 \cup Pa_2 = \{Me_1, Me_2, Me_3, Me_4\}$$

...

The *set-of-common* measures  $\bigcap_{Me}$ , between  $Pa_1$  and  $Pa_2$ , can be found by intersection  $\cap$ :

$$\bigcap_{Me} = Pa_1 \cap Pa_2 = \{Me_2, Me_3\}$$

...

Observing:

$$|\bigcup_{Me}| = 4, \quad |\bigcap_{Me}| = 2, \quad |\bigcap_{Me}| < |\bigcup_{Me}|$$

...

*note: remember, this is a simplification, and an introduction*

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## 1.3 incommensurability

$(\cap_{\emptyset})$  <sup>3</sup>

Consider paradigms  $Pa_3$  and  $Pa_4$ , whereby:

$$Pa_3 = \{Me_1, Me_2, Me_3\}$$

$$Pa_4 = \{Me_4, Me_5, Me_6\}$$

...

When paradigms  $Pa_3$  and  $Pa_4$ , do not share common measures, then  $\bigcap_{Me}$ , is an empty set  $\emptyset$ :

$$\bigcap_{Me} = Pa_3 \cap Pa_4 = \emptyset : |\emptyset| = 0$$

and paradigms  $Pa_3$  and  $Pa_4$ , can be said to be incommensurable  $\bigcap_{Me}^{\cap_{\emptyset}}$ :

$$\bigcap_{Me} = Pa_3 \cap Pa_4 = \emptyset : \bigcap_{Me} \rightarrow \bigcap_{Me}^{\cap_{\emptyset}}, \quad |\bigcap_{Me}^{\cap_{\emptyset}}| = 0$$

...

*note: while any two paradigms may appear incommensurable as an isolated pair* <sup>4</sup>, *we will later discover that there exists a universally special paradigm, which by analysis or composition, renders all paradigms reconcilable, and as such, commensurable*

□