openmp_mpi_k-means

March 18, 2019

1 K-Means Clustering with OpenMP and MPI

1.0.1 Implement the k-means clustering algorithm in OpenMP/MPI, trying to maximize the performance (reduce the execution time) by carefully exploiting the resources within one computing node with multiple processing cores (OpenMP) and across computing nodes (MPI).

Optional: implement the same algorithm in Apache Flink and compare the performance of the two implementations (processing time and scalability) under various workloads.

```
In [1]: import csv
        import random
        import sys
        import numpy
        import os # We need this module
        import matplotlib.pyplot as plt
        import seaborn as sns;
        from sklearn.datasets.samples_generator import make_blobs
        sns.set() # for plot styling
        #Samples
        N_SAMPLES = 100000
        # Get path of the current dir, then use it to create paths:
        CURRENT_DIR = os.path.dirname("__file__")
        file_path = os.path.join(CURRENT_DIR, 'dataset_display/dataset.csv')
        initial_dataset_path = os.path.join(CURRENT_DIR, 'dataset_display/initialdataset.csv')
        initial_centroids_path = os.path.join(CURRENT_DIR, 'dataset_display/initialcentroids.csv
        new_dataset_path = os.path.join(CURRENT_DIR, 'dataset_display/newdataset.csv')
        new_centroids_path = os.path.join(CURRENT_DIR, 'dataset_display/newcentroids.csv')
        objfun_path = os.path.join(CURRENT_DIR, 'dataset_display/objfun.csv')
        exectimes_path = os.path.join(CURRENT_DIR, 'dataset_display/exectimes.csv')
        results_100_path = os.path.join(CURRENT_DIR, 'dataset_display/results_100/results.csv')
        results_1K_path = os.path.join(CURRENT_DIR, 'dataset_display/results_1K/results.csv')
```

```
results_10K_path = os.path.join(CURRENT_DIR, 'dataset_display/results_10K/results.csv')
results_100K_path = os.path.join(CURRENT_DIR, 'dataset_display/results_100K/results.csv')
results_1M_path = os.path.join(CURRENT_DIR, 'dataset_display/results_1M/results.csv')
results_10M_path = os.path.join(CURRENT_DIR, 'dataset_display/results_10M/results.csv')
fig_width = 12
fig_height = 10
```

2 Initial Dataset

2.1 Display the points in the Initial Dataset:

We have an Initial Dataset of 100000 points(later on we'll be using different sizes), randomly generated by a custom Python script. These points are already somehow divided in clusters so that we can more easily test the K-Means Clustering algorithm.

```
In [2]: print('X,Y')
        with open(initial_dataset_path) as csvfile:
            reader = csv.DictReader(csvfile)
            for i,row in enumerate(reader):
                print(row['X'], row['Y'])
                if(i >= 10):
                    break
        print("Total points: %s" % format(N_SAMPLES, 'd'))
X, Y
4.762006 -7.700549
4.490764 -8.202433
-1.384802 2.850730
-1.411994 -6.885759
0.045029 1.578344
-7.419469 9.258043
-6.915910 9.343622
-7.663262 8.672174
-2.618907 -6.364270
-1.369107 -8.103168
-7.965163 9.759896
Total points: 100000
```

2.2 And now we plot the initial dataset:

By plotting the Dataset, we can see that is indeed form by 4 clusters easily observable. We'll later test the K-Means Clustering algorithm and see if it can also individuate the clusters.

```
In [3]: x = numpy.zeros(N_SAMPLES)
y = numpy.zeros(N_SAMPLES)
```

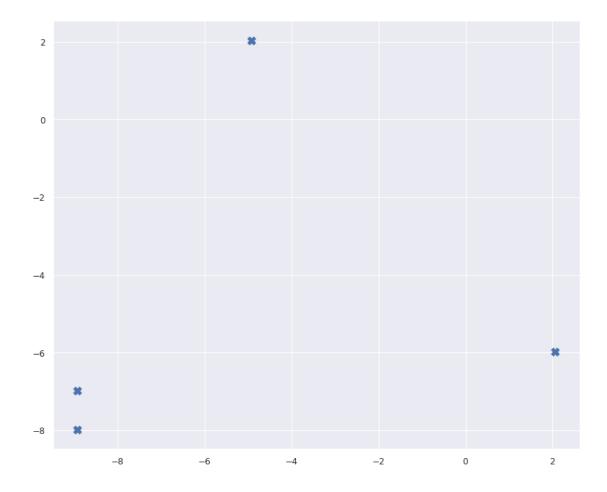
```
#Read the dataset from the CVS file
with open(initial_dataset_path) as csvfile:
    reader = csv.DictReader(csvfile)
   i = 0
    for row in reader:
        x[i] = row['X']
        y[i] = row['Y']
        \#print(x[i], y[i])
        i=i+1
#Plot the read dataset
plt.figure(figsize=(fig_width, fig_height), dpi= 80, facecolor='w', edgecolor='k')
plt.scatter(x[:], y[:], s=1)
plt.show()
```

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2.3 Initial Centroids

The Initial Centroids are randomply placed at runtime, however a centroids will be recreated if it is too close to another centroid. The initial placing of the centroids is of fundamental importance to the result of the K-Means Clustering algorithm execution on a given dataset. Lets print the centroids:

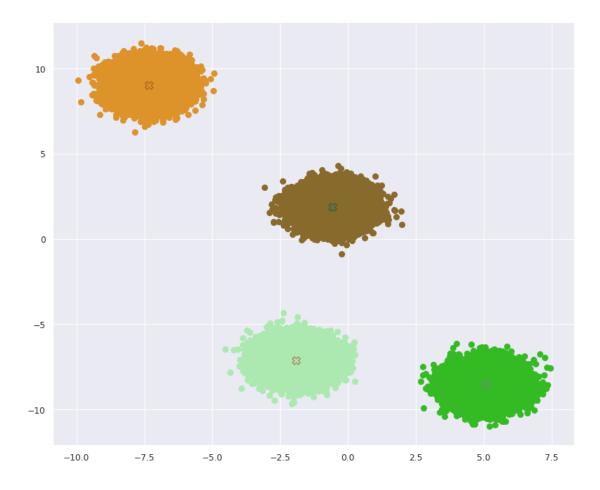
```
In [4]: print('Cluster, X, Y')
        centroids = 0
        with open(initial_centroids_path) as csvfile:
            reader = csv.DictReader(csvfile)
            for row in reader:
                print(centroids, row['X'], row['Y'])
                centroids = centroids + 1
        print("Total centroids: %d" % centroids)
Cluster, X, Y
0 -8.933069 -6.976418
1 -8.933069 -7.976418
2 2.066931 -5.976418
3 -4.933069 2.023582
Total centroids: 4
   And now we plot them:
In [5]: x = numpy.zeros(centroids)
        y = numpy.zeros(centroids)
        #Read the dataset from the CVS file
        with open(initial_centroids_path) as csvfile:
            reader = csv.DictReader(csvfile)
            i = 0
            for row in reader:
                x[i] = row['X']
                y[i] = row['Y']
                \#print(x[i], y[i])
                i=i+1
        #Plot the read dataset
        plt.figure(figsize=(fig_width, fig_height), dpi= 80, facecolor='w', edgecolor='k')
        plt.scatter(x[:], y[:], marker="X", s=100)
        plt.show()
```



3 Plotting both Dataset and Centroids

We've run the K-Means Clustering Algorithm on the initial dataset and got new centroids each associated to a cluster. So we now plot the resulting clusters separated by a random color and their centroids:

```
with open(new_centroids_path) as csvfile:
    reader = csv.DictReader(csvfile)
    for row in reader:
        cx.append(float(row['X']))
        cy.append(float(row['Y']))
# Read the new dataset from the CVS file
with open(new_dataset_path) as csvfile:
    reader = csv.DictReader(csvfile)
    i = 0
    for row in reader:
        x[i] = row['X']
        y[i] = row['Y']
        c[i] = row['Cluster']
        # print(x[i], y[i])
        i = i + 1
minK = c.min()
maxK = c.max()
k = (int)(maxK - minK + 1)
# plot the points for each cluster with a different color
for i in range(k):
    x2 = list()
    y2 = list()
    for j in range(N_SAMPLES):
        if c[j] == i:
            x2.append(x[j])
            y2.append(y[j])
    # Plot the read dataset
    color1 = random_color()
    color2 = random_color()
    plt.scatter(x2[:], y2[:], c=color1, s=50)
    plt.scatter(cx[i], cy[i], c=color1, marker="X", edgecolor=color2, s=100)
plt.show()
```



3.1 Running Modes: Normal, OpenMP, MPI, MPI + OpenMP

The program written in C actually executes four different versions of the K-Means Clustering Algorithm. They run sequentially one at a time, but they use the same initial dataset and the same random pair of initial centroids. The initial position of the centroids is of vital importance to the result of the execution so is important that all four versions use the same set of centroids so that we can have a meaningful comparison in performance. All four versions will produce the same result and same objective function value, but they will have different execution times.

We've set the maximum number of cores for the OpenMP verision (4 on this PC), and 4 parallel nodes for the MPI (and MPI+OpenMP) Version. As expected the OpenMP version perform much better that the sequential version, while with MPI is not always the case, here are the results of a single execution on this dataset:

```
In [8]: print('Execution Times:\n')
    t = numpy.zeros(4)
    with open(exectimes_path) as csvfile:
        reader = csv.DictReader(csvfile)
        for i,row in enumerate(reader):
        t[i] = row['Time']
```

```
print('Normal Execution --> ' + str(t[0]*1000) + 'ms')
       print('OpenMP Execution --> ' + str(t[1]*1000) + 'ms')
       print('MPI Execution --> ' + str(t[2]*1000) + 'ms')
       Execution Times:
Normal Execution --> 89.87299999999999ms
OpenMP Execution --> 43.09600000000004ms
MPI Execution --> 887.715ms
MPI + OpenMP Execution --> 2597.859ms
  While the value of the Objective Function is:
In [9]: objfun = numpy.zeros(4)
       with open(objfun_path) as csvfile:
          reader = csv.DictReader(csvfile)
          for i.row in enumerate(reader):
              objfun[i] = row['ObjFun']
       print('ObjectiveFunction value --> ' + str(objfun[0]))
ObjectiveFunction value --> 71883.648438
```

3.2 ———————

4 Amazon AWS Starcluster Results

All the executions and tests explained below were run on a cluster of **four c3.xlarge EC2 Nodes** on Amazon AWS by using the Starcluster open source cluster-computing toolkit. Each node (c3.xlarge) is a powerful machine with 4 cores and 8GB of RAM.

4.0.1 Cumulative Execution Results

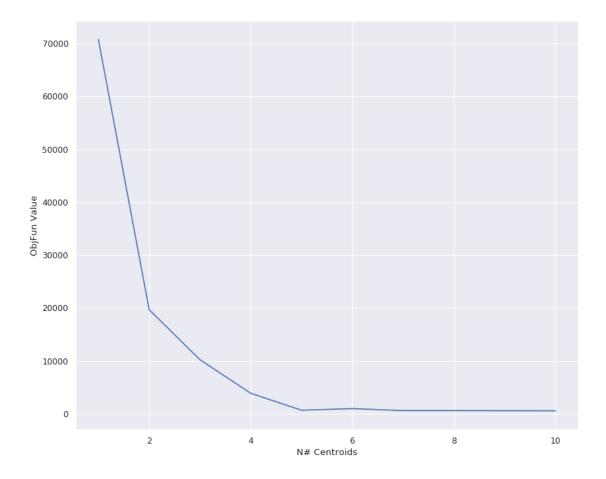
By running a bach script we were able cumulate a large quantity of execution results (more than 4000 executions). For consistency we've run all four different versions of the K-Means Clustering Algorithm sequentially one at a time on the same initial dataset and the same random pair of initial centroids (changing every cycle). That way the results of each execution can be compered with the executions of the other three versions of the algorithm. For each executions we've stored the number of centroids, the execution mode(algorithm version), the execution time and the obj function result.

4.0.2 1) Relation between number of centroids and obj function value

Let's average the executions results in the large dataset described above and plot the relation between the number of centroids and the obj function value. The execution were made with a number of centroids between 1 and 10.

```
In [10]: def getResultsData(fname):
             row_count = 0
             with open(fname) as csvfile:
                 row_count = sum(1 for line in csvfile)
             print ("Rows in the results file: " + str(row_count))
             EXECUTIONS = int((row_count - 1)/4)
             n_c
                      = numpy.zeros(EXECUTIONS)
             openmp_c = numpy.zeros(EXECUTIONS)
             mpi_c
                     = numpy.zeros(EXECUTIONS)
             mpi_mp_c = numpy.zeros(EXECUTIONS)
                      = numpy.zeros(EXECUTIONS)
             n_t
             openmp_t = numpy.zeros(EXECUTIONS)
                      = numpy.zeros(EXECUTIONS)
             mpi_mp_t = numpy.zeros(EXECUTIONS)
                       = numpy.zeros(EXECUTIONS)
             openmp_of = numpy.zeros(EXECUTIONS)
                      = numpy.zeros(EXECUTIONS)
             mpi_mp_of = numpy.zeros(EXECUTIONS)
             # Read the new centroids from the CVS file
             with open(fname) as csvfile:
                 reader = csv.DictReader(csvfile)
                 i1,i2,i3,i4=0,0,0,0
                 for i,row in enumerate(reader):
                     mode = int(row['Mode'])
                     #print(mode + "-" + str(i))
                     #Normal Execution
                     if mode == 0:
                         n_c[i1] = float(row['K'])
                         n_t[i1] = float(row['Time'])
                         n_of[i1] = float(row['ObjFun'])
                         i1 = i1 + 1
                     #OpenMP Execution
                     elif mode == 1:
                         openmp_c[i2] = float(row['K'])
                         openmp_t[i2] = float(row['Time'])
                         openmp_of[i2] = float(row['ObjFun'])
                         i2 = i2 + 1
                     #MPI Execution
                     elif mode == 2:
                         mpi_c[i3] = float(row['K'])
                         mpi_t[i3] = float(row['Time'])
                         mpi_of[i3] = float(row['ObjFun'])
                         i3 = i3 + 1
```

```
#MPI + OpenMP Execution
            elif mode == 3:
                mpi_mp_c[i4] = float(row['K'])
                mpi_mp_t[i4] = float(row['Time'])
                mpi_mp_of[i4] = float(row['ObjFun'])
                i4 = i4 + 1
    return EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c,
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
x_val = numpy.zeros(10)
y_val = numpy.zeros(10)
#Calc the mean values
for i in range(0,10):
    x_val[i] = i + 1
    #print(str(i))
    #Iterate all the executions for each centroid number
    for j in range(EXECUTIONS):
        if n_c[j] == i+1:
            y_val[i] = y_val[i] + n_of[j]
    #Obj Function values mean
    y_val[i] = y_val[i] / EXECUTIONS
    \#print(str(y_val[i]))
#Plot the between number of centroids and obj function value
plt.figure(figsize=(fig\_width, \ fig\_height), \ dpi=\ 80, \ facecolor='w', \ edgecolor='k')
plt.plot(x_val,y_val)
plt.suptitle('Number of Centroids - Obj. Function Value')
plt.xlabel('N# Centroids')
plt.ylabel('ObjFun Value')
plt.show()
```



4.0.3 Resulting plot analisys

Given the Plot above we can observe the way that the Obj. Function Values(Y-Axis) changes based on the Number of Centroids(X-Asis) used. And we can clearly notice that the Knee value is equal to "4". It's the Knee value because the successive numbers of centroids don't have an Obj. Function Value that decreases greatly. That means that the distances in between the data points and the centroids for each cluster don't decrease much after the value of 4 centroids used. So just by observing the above plot and chosing the knee value we can conclude that the Dataset is composed of 4 clusters witch is correct since we are the ones that generated the datased divided in four clusters in the first place.

4.0.4 2) Relation between Number of Centroids and the Execution Time (by varying the Dataset Size)

Let's now again average the executions results in five different Datasets as described above and plot the relation between the number of centroids and the Execution times. The execution were made with a number of centroids between 1 and 10.

We'll compare the results for each of the four execution modes: **Normal**, **OpenMP**, **MPI**, **MPI** + **OpenMP**

While the datasets that we'll be using have the following sizes: **100, 1K, 10K, 100K and 1M** datapoints (1K=1000 points, 1M = 1000000 points):

4.0.5 2.1) Dataset size: 100

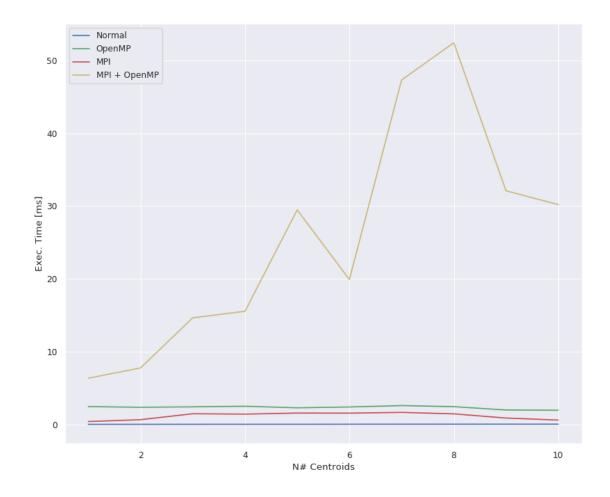
```
In [11]: def plotRealtionCentroidsExecTime():
                              = numpy.zeros(10) # Centroids
              x_valc
              y_val_n_et = numpy.zeros(10) # Normal Execution Time
y_val_mp_et = numpy.zeros(10) # OpenMP Execution Time
y_val_mpi_et = numpy.zeros(10) # MPI Execution Time
y_val_mpi_mp_et = numpy.zeros(10) # MPI + OpenMP Execution Time
               #Calc the mean values
              for i in range(0,10):
                   x_valc[i] = i + 1
                   #print(str(i))
                   #Iterate all the executions for each centroid number
                   for j in range(EXECUTIONS):
                       # Normal Execution
                       if n_c[j] == i+1:
                            y_val_n_{et}[i] = y_val_n_{et}[i] + n_t[j]
                       # OpenMP Execution
                       if openmp_c[j] == i+1:
                            y_val_mp_et[i] = y_val_mp_et[i] + openmp_t[j]
                       # MPI Execution
                       if mpi_c[j] == i+1:
                            y_val_mpi_et[i] = y_val_mpi_et[i] + mpi_t[j]
                       # MPI + OpenMP Execution
                       if mpi_mp_c[j] == i+1:
                            y_val_mpi_mp_et[i] = y_val_mpi_mp_et[i] + mpi_mp_t[j]
                   #Execution Time values mean
                   y_val_n_et[i] = (y_val_n_et[i] / EXECUTIONS) * 1000
                   y_val_mp_et[i] = (y_val_mp_et[i] / EXECUTIONS) * 1000
                   y_val_mpi_et[i] = (y_val_mpi_et[i] / EXECUTIONS) * 1000
                   y_val_mpi_mp_et[i] = (y_val_mpi_mp_et[i] / EXECUTIONS) * 1000
                   #print("n " + str(y_val_n_et[i]))
                   \#print("mp" + str(y_val_mp_et[i]))
                   \#print("mpi" + str(y_val_mpi_et[i]))
               #Plot the relation between number of centroids and obj function value
              plt.figure(figsize=(fig_width, fig_height), dpi= 80, facecolor='w', edgecolor='k')
```

```
plt.plot(x_valc,y_val_n_et, '-b', label='Normal')
plt.suptitle('Number of Centroids - Execution Time')
plt.xlabel('N# Centroids')
plt.ylabel('Exec. Time [ms]')
plt.plot(x_valc,y_val_mp_et, '-g', label='OpenMP')
plt.plot(x_valc,y_val_mpi_et, '-r', label='MPI')
plt.plot(x_valc,y_val_mpi_mp_et, '-y', label='MPI + OpenMP')
plt.plot(x_valc,y_val_mpi_mp_et, '-y', label='MPI + OpenMP')
plt.legend(loc='upper left')
plt.show()
```

EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
plotRealtionCentroidsExecTime()

Rows in the results file: 1201

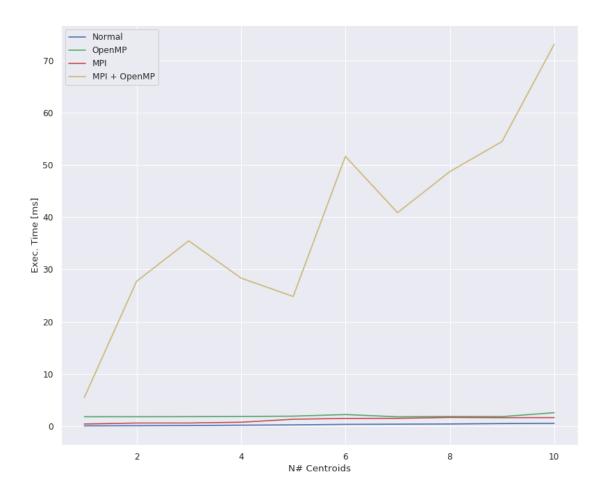
Number of Centroids - Execution Time



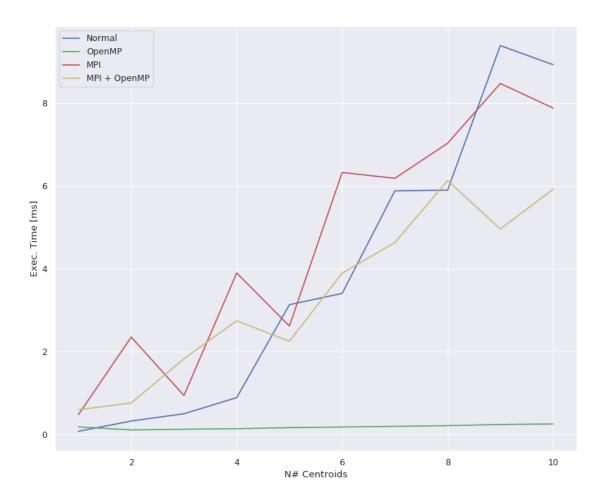
4.0.6 2.2) Dataset size: 1K

Rows in the results file: 1201

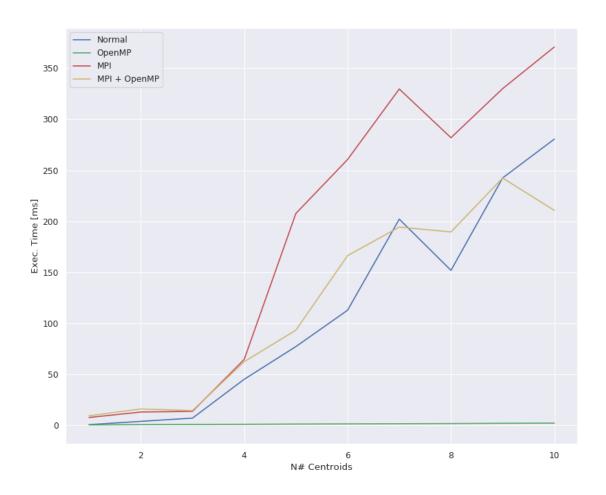
Number of Centroids - Execution Time



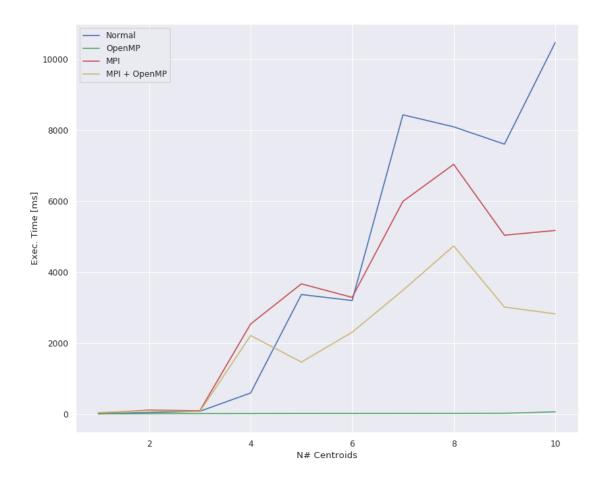
4.0.7 2.3) Dataset size: 10K



4.0.8 2.4) Dataset size: 100K



4.0.9 2.5) Dataset size: 1M



4.0.10 Resulting plots analisys - ExecutionTime

On the above plots we can observe the Execution Times(Y-Axis) for each execution mode base on the number of centroids(X-Axis). The executions were repeated a great number of times for each of the five different datasets dimensions, so that we can test the scalability of the system.

It's imeadiatly clear just by a glance that **OpenMP Mode(Green Line)** greatly outperforms the single-core and single-process **Normal Mode(Blue line)** once there is a resonable big dataset (> 1000 points). But it also outperforms the **MPI(Red Line)** and **MPI+OpenMP(Yellow Line) Modes**, the latter performing quite pourly on a small dataset. This is probably due to all the message exchange between the processes in MPI that are neccessary for managing the paralellization of the operations and due to the broadcasting/gathering of the data to/from the nodes. By adding OpenMP to MPI we can see indeed a big improvement (on a resonably big dataset) but due to the overhead caused by the messages exchanged between the nodes it's not enough to beat the OpenMP Mode on these tests.

However we notice that By increasing the size of the dataset and number of clusters, all three Modes (OpenMP, MPI, MPI+OpenMP) perform better that the single node and single

core version (Normal Mode).

Finally we remind the reader that the above plot is made by avareging the behavior of a large number of executions each with a different initial random centroids placement. And it has beed noticed that if the initial placement of the centroids is a good one, then the MPI and MPI+OpenMP Modes perform better, so by engaging in a more sophisticated algorithms for centroids placement we could improve overall performance.

4.0.11 3) Relation between the Dataset Size and the Execution Time

```
In [20]:
           def getCentroidsExecTime():
                                = numpy.zeros(10)  # Centroids
= numpy.zeros(10)  # Normal Execution Time
               x_valc
               y_val_n_et
               y_val_mp_et = numpy.zeros(10)  # OpenMP Execution Time
y_val_mpi_et = numpy.zeros(10)  # MPI Execution Time
y_val_mpi_mp_et = numpy.zeros(10)  # MPI + OpenMP Execution Time
               #Calc the mean values
               for i in range(0,10):
                    x_valc[i] = i + 1
                    #print(str(i))
                    #Iterate all the executions for each centroid number
                    for j in range(EXECUTIONS):
                         # Normal Execution
                         if n_c[j] == i+1:
                              y_val_n_et[i] = y_val_n_et[i] + n_t[j]
                         # OpenMP Execution
                         if openmp_c[j] == i+1:
                              y_val_mp_et[i] = y_val_mp_et[i] + openmp_t[j]
                         # MPI Execution
                         if mpi_c[j] == i+1:
                              y_val_mpi_et[i] = y_val_mpi_et[i] + mpi_t[j]
                         # MPI + OpenMP Execution
                         if mpi_mp_c[j] == i+1:
                              y_val_mpi_mp_et[i] = y_val_mpi_mp_et[i] + mpi_mp_t[j]
                    #Execution Time values mean
                    y_val_n_et[i] = (y_val_n_et[i] / EXECUTIONS) * 1000
y_val_mp_et[i] = (y_val_mp_et[i] / EXECUTIONS) * 1000
                    y_val_mpi_et[i] = (y_val_mpi_et[i] / EXECUTIONS) * 1000
                    y_val_mpi_mp_et[i] = (y_val_mpi_mp_et[i] / EXECUTIONS) * 1000
```

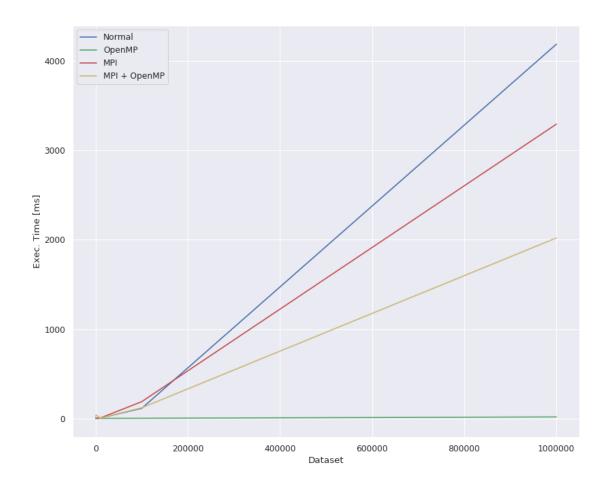
return y_val_n_et, y_val_mp_et, y_val_mpi_et, y_val_mpi_mp_et

```
x_valds
            = numpy.zeros(5)
                               # Dataset sizes
                               # Normal Execution Time
            = numpy.zeros(5)
y_val_n
            = numpy.zeros(5) # OpenMP Execution Time
y_val_mp
                               # MPI Execution Time
           = numpy.zeros(5)
y_val_mpi
                               # MPI + OpenMP Execution Time
y_val_mpi_mp = numpy.zeros(5)
def calcMeanExecTime(j):
   for i in range(1,10):
        y_val_n[j]
                      += y_val_n_et[i]
       y_val_mp[j]
                      += y_val_mp_et[i]
        y_val_mpi[j]
                      += y_val_mpi_et[i]
        y_val_mpi_mp[j] += y_val_mpi_mp_et[i]
    y_val_n[j]
                   /= 10
   y_val_mp[j]
                   /= 10
                   /= 10
   y_val_mpi[j]
   y_val_mpi_mp[j] /= 10
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
y_val_n_et, y_val_mp_et, y_val_mpi_et, y_val_mpi_mp_et = getCentroidsExecTime()
calcMeanExecTime(0)
x_valds[0]=100
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
y_val_n_et, y_val_mp_et, y_val_mpi_et, y_val_mpi_mp_et = getCentroidsExecTime()
calcMeanExecTime(1)
x_valds[1]=1000
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
y_val_n_et, y_val_mp_et, y_val_mpi_et, y_val_mpi_mp_et = getCentroidsExecTime()
calcMeanExecTime(2)
x valds[2]=10000
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
y_val_n_et, y_val_mp_et, y_val_mpi_et, y_val_mpi_mp_et = getCentroidsExecTime()
calcMeanExecTime(3)
x_valds[3]=100000
EXECUTIONS, n_t, openmp_t, mpi_t, mpi_mp_t, n_c, openmp_c, mpi_c, mpi_mp_c, n_of = getF
y_val_n_et, y_val_mpi_et, y_val_mpi_et = getCentroidsExecTime()
calcMeanExecTime(4)
x_valds[4]=1000000
#Plot the relation between the dataset size and mean executin time for each mode
plt.figure(figsize=(fig_width, fig_height), dpi= 80, facecolor='w', edgecolor='k')
plt.plot(x_valds,y_val_n, '-b', label='Normal')
plt.suptitle('Dataset Size - Execution Time')
```

```
plt.xlabel('Dataset')
plt.ylabel('Exec. Time [ms]')
plt.plot(x_valds,y_val_mp, '-g', label='OpenMP')
plt.plot(x_valds,y_val_mpi, '-r', label='MPI')
plt.plot(x_valds,y_val_mpi_mp, '-y', label='MPI + OpenMP')
plt.legend(loc='upper left')
plt.show()
```

Rows in the results file: 1201 Rows in the results file: 1201 Rows in the results file: 801 Rows in the results file: 801 Rows in the results file: 401

Dataset Size - Execution Time



4.0.12 Resulting plots analisys - Scalability

On the above plot we can observe that the Scalability of the four Modes on the given datasets and cluster of nodes seems to be Linear. Moreover, by increasing the size of the datasets the performance gap between the single core and single node mode and the other modes is more pronounced. Note on the figure that with a small dataset the Normal Mode might perform better. While later on the best performing mode is OpenMP Mode followed by the MPI+OpenMP Mode.

However, the outstanding performance of the OpenMP mode we think that is not going to continue to scale linearly by increasing the size of the dataset and the number of clusters. That is beacause there is a limit on how many cores and computational power a machine can have. At some point the computational power will saturate and the execution time of the OpenMP mode will rise exponentially.

The only Modes that will continue Scale Linearly are the MPI and MPI+OpenMP nodes. That is because you can always add more nodes to your cluster to increase performance. However that is a supposition since we couldn't actually run tests on much larger datasets and larger clusters of nodes on Amazon AWS because of the large costs and computational time needed for such feat. (for example to run the script on a 10M points dataset would have required approximately a week with the four on demand c3.xlarge nodes)