

MATH 5110: Lab 1a

Problem 1.

(a)

A =

$$\begin{array}{cccc} 1 & -1 & 2 & 1 \\ 2 & -2 & 4 & 1 \\ -3 & 3 & -6 & 1 \end{array}$$

ans =

$$\begin{array}{cccc} 1 & -1 & 2 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{array}$$

No solutions.

(b)

A =

$$\begin{array}{cccc} 1 & -1 & 2 & 1 \\ 1 & -4 & 1 & -1 \\ 3 & 3 & -2 & 2 \end{array}$$

ans =

$$\begin{array}{cccc} 1.0000 & 0 & 0 & 0.5000 \\ 0 & 1.0000 & 0 & 0.5000 \\ 0 & 0 & 1.0000 & 0.5000 \end{array}$$

$$x_1 = x_2 = x_3 = 0.5$$

(c)

A =

$$\begin{bmatrix} 1 & -1 & 2 & 1 \\ 4 & -2 & 1 & 1 \\ 2 & 0 & -3 & -1 \end{bmatrix}$$

ans =

$$\begin{bmatrix} 1.0000 & 0 & -1.5000 & -0.5000 \\ 0 & 1.0000 & -3.5000 & -1.5000 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$(x_1, x_2, x_3) = (-0.5, -1.5, 0) + t(1.5, 3.5, 1), \quad -\infty < t < \infty$$

Problem 2.

1) Let $c = \cos 60 = \frac{1}{2}$ and $s = \sin 60 = \frac{\sqrt{3}}{2}$. The equations are

A: $R_2 = T_5 + T_1 c$

$$R_1 = T_1 s$$

B: $T_1 c = T_2 c + T_7$

$$f_1 + T_1 s + T_2 s = 0$$

C: $T_2 s + T_3 s = 0$

$$T_5 + T_2 c = T_6 + T_3 c$$

D: $f_2 + T_7 + T_3 c = T_4 c$

$$T_3 s + T_4 s = 0$$

E: $T_4 s = R_3$

$$T_6 + T_4 c = 0$$

Matlab with variables in order (R_1, R_2, R_3, T_1, ... , T_7): last column is external forces:

```
c=cos(pi/3);
s=sin(pi/3);
f1=100;
f2=1000;
```

```
B=[0 1 0 -c 0 0 0 -1 0 0 0;
    1 0 0 -s 0 0 0 0 0 0 0;
    0 0 0 c -c 0 0 0 0 -1 0;
    0 0 0 s s 0 0 0 0 0 -f1;
    0 0 0 0 s s 0 0 0 0 0;
    0 0 0 0 c -c 0 1 -1 0 0;
    0 0 0 0 0 c -c 0 0 1 -f2;
    0 0 0 0 0 s s 0 0 0 0;
    0 0 1 0 0 0 -s 0 0 0 0;
    0 0 0 0 0 0 c 0 1 0 0]
```

Solution is

```
ans =
1.0e+03 *
-0.5080 -1.0000 0.4080 -0.5866 0.4711 -0.4711 0.4711 -0.7067 -0.2356 -0.5289
```

(2) f1 =100; use syms f2. Then solution for T_3 is

```
ans =
[ 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, (50*3^(1/2))/3 - f2/2]
```

Solve for T_3 = -1000 to get f2 = 2058.

(3) Use syms f1 and syms f2 to get

```
[ 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -(3^(1/2)*(f2 + 3^(1/2)*f1))/4]
[ 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, -f2]
[ 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, (3^(1/2)*f2)/4 - f1/4]
[ 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, -f2/2 - (3^(1/2)*f1)/2]
[ 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, f2/2 - (3^(1/2)*f1)/6]
[ 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, (3^(1/2)*f1)/6 - f2/2]
[ 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, -(3^(1/2)*(f1 - 3^(1/2)*f2))/6]
[ 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, (3^(1/2)*(f1 - 3^(1/2)*f2))/4]
[ 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, (3^(1/2)*(f1 - 3^(1/2)*f2))/12]
[ 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, -(3^(1/2)*(f1 + 3^(1/2)*f2))/6]
```

Set T_3 = -1000 to get

$$-1000 = f1/2\sqrt{3} - f2/2$$