

Hypergraph

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1 A hypergraph exploration

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This notebook explores a hypergraph using Dleto.

First need to load Julia

```
[1]: ## Uncomment if you do not have iJulia installed
# using Pkg
# Pkg.add("IJulia")
# This installs Julia's Jupyter kernel without Python dependencies
# println("IJulia installed! Restart VS Code and select Julia kernel.")

# Ensure Julia kernel is properly recognized
# This notebook requires Julia kernel for execution and export
using IJulia
println("Julia kernel is active!")
println("Julia version: ", VERSION) # Fix Jupyter/Julia setup - Install IJulia
    ↪for Julia notebooks
```

Julia kernel is active!

Julia version: 1.10.3

Next we load Dleto.

```
[7]: include("../Dleto.jl")
```

plotTensor (generic function with 2 methods)

Now let us load a hypergraph tensor.

```
[8]: hypgraph_ten = loadTensorFromFile("Hypergraph-Tensor.txt")
```

30×30×30 Array{Float64, 3}:

[:, :, 1] =

0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0

$$\begin{matrix} \cdot & \cdot & \cdot \\ ; & ; & ; \end{matrix} \dots$$

0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	1.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	1.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0

3

```

0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0  ... 0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  1.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  1.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
1.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0

```

`[:, :, 30] =`

```

0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0  ... 0.0  0.0  0.0  0.0  0.0  1.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0  ... 0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0

```

```

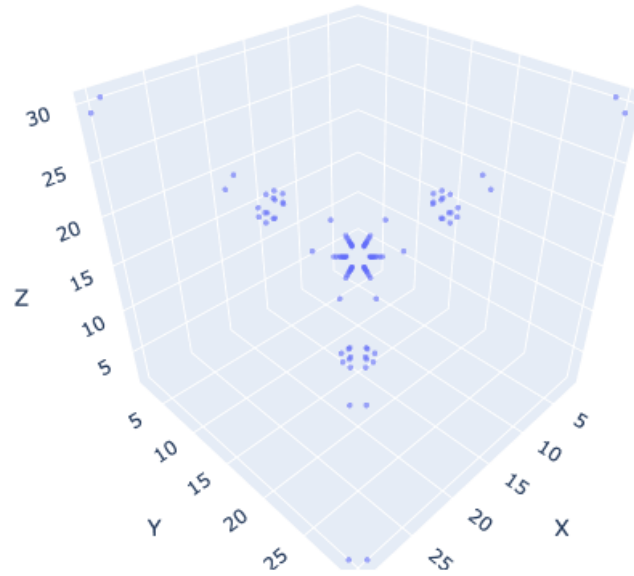
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0  ... 0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
1.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  0.0  0.0  0.0      0.0  0.0  0.0  0.0  0.0  0.0  0.0

```

We can better visualize this using 3D plotting software.

```
[9]: plotTensor(hypgraph_ten)
```

3D Tensor Visualization



```
[10]: strata = toSurfaceTensor(hypgraph_ten)
      plotTensor(strata.tensor)
```

Building linear system...

0.145867 seconds (149.11 k allocations: 315.448 MiB, 5.96% gc time, 40.52% compilation time)

Computing singular vectors for (1395, 27000)...

```
eigens[1] = [-7.88501156486917e-15, -2.9045899244935065e-15,
-7.839734147271726e-16, -7.586855218172284e-17, -5.754795872895732e-17,
-1.2806642811258756e-17, 8.958045186794124e-16, 2.1542020620676705e-15,
3.3223444125664425e-15, 1.0470421484944823e-14, 1.2589438657623908e-14,
0.06988742002834393, 0.06988742002834417, 0.10706415227280433,
0.16026685838154714, 0.1602668583815478, 0.5301293716857454, 0.530129371685757,
0.5613150924006317, 0.7212706098648767]
```

0.879807 seconds (1.09 M allocations: 87.888 MiB, 0.39% gc time, 33.12% compilation time)

Extracting matrices...

0.009716 seconds (7.76 k allocations: 584.750 KiB, 99.67% compilation time)

0.000003 seconds (2 allocations: 7.281 KiB)
0.000002 seconds (3 allocations: 7.297 KiB)

3D Tensor Visualization

