Clustering

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Libraries

Reading in Data

```
setwd("~/harvard-summer-biostats")
df <- read_csv("data/wide_illinois.csv") #read in data</pre>
## Parsed with column specification:
## cols(
##
     .default = col_double(),
##
     well_id = col_character(),
     site = col_character(),
     disposal_area = col_character(),
##
     type = col_character(),
##
     gradient = col_character()
## )
## See spec(...) for full column specifications.
df1 <- na.omit(df) #get rid of na's
df1 <- df1[-69,]
```

Hierarchical Methods

If we want to look for cereal groups via hierarchical clustering, we need to construct a distance matrix. Distances are constructed with the *dist* function, and we need to choose whether we compute them on scaled or unscaled variables (standardize or not).

```
df.dist <- dist(df1[, -c(1:5)])</pre>
```

Now we look at how hierarchical clustering is applied. The relevant function is hclust. We can look at the dendrogram, also.

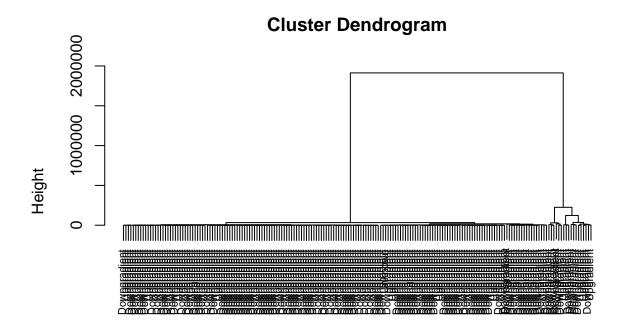
The options for helust in terms of linkages are provided in the help under options for method. The following options are listed: "ward.D", "ward.D2", "single", "complete", "average", "mcquitty", "median" or "centroid".

In order to obtain cluster labels, we need to *cut* our dendrograms.

To learn more details about the clusters we found:

Arsenic, Lithium, Boron are some widely found contaminants whose concentrations are often above the thresholds considered to be safe.

```
hcward <- hclust(df.dist, method = "ward.D")
plot(hcward, labels = df1$gradient, cex = 0.7) #cex adjusts size of label</pre>
```



df.dist hclust (*, "ward.D")

```
wardSol <- (cutree(hcward, k = 2)) #cluster labels are numeric, k= # clusters
knitr::kable(table(summary(as.factor(wardSol)))) #as factor to get table</pre>
```

```
Var1 Freq
18 1
172 1
```

```
favstats(Boron ~ wardSol, data = df1) #can choose any variable
```

```
Q1
##
     wardSol
                  min
                                       median
                                                      QЗ
                                                           max
                                                                      mean
## 1
             0.01000 0.06881944
                                    0.3486667
                                                1.787194 60.9
           2 31.28651 86.09861111 118.7777778 144.569444 195.0 114.489150
## 2
                 n missing
            sd
## 1 5.221868 172
```

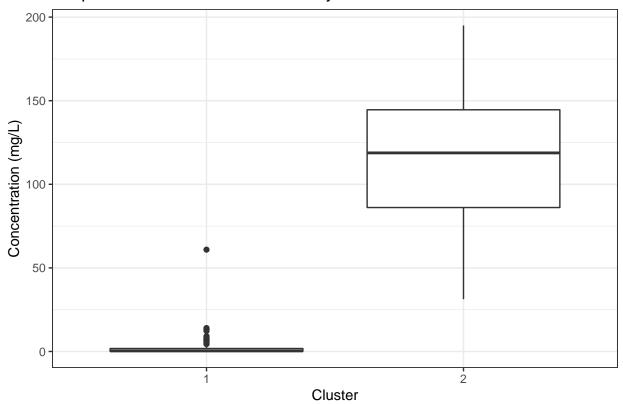
```
## 2 41.134146 18
```

xlab("Cluster") +

ylab("Concentration (mg/L)")

```
ggplot(df1, aes(x = as.factor(wardSol), y = Boron)) +
  geom_boxplot() +
  theme_bw() +
  ggtitle("Boxplot of Concentration of Boron by Cluster") +
  xlab("Cluster") +
  ylab("Concentration (mg/L)")
```

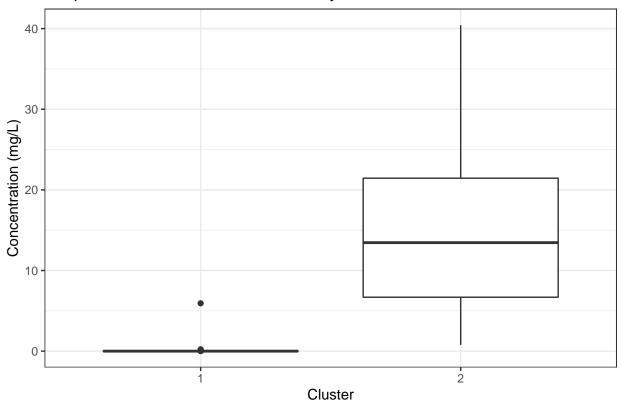
Boxplot of Concentration of Boron by Cluster



```
favstats(Arsenic ~ wardSol, data = df1) #can choose any variable
```

```
wardSol
                  min
                             Q1
                                   median
                                                   QЗ
                                                         max
## 1
           1 0.0005250 0.001015 0.0021125 0.00843125 5.936 0.04588403
           2 0.7757625 6.687500 13.4565000 21.44687500 40.425 15.48252257
                 n missing
## 1 0.4526302 172
## 2 13.1701676 18
ggplot(df1, aes(x = as.factor(wardSol), y = Arsenic)) +
  geom_boxplot() +
  theme_bw() +
  ggtitle("Boxplot of Concentration of Arsenic by Cluster") +
```

Boxplot of Concentration of Arsenic by Cluster

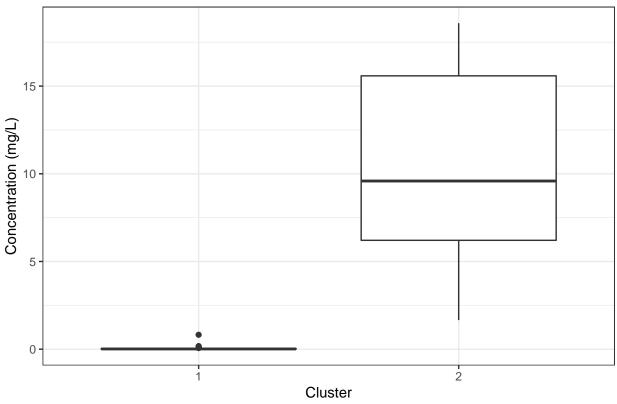


```
favstats(Lithium ~ wardSol, data = df1) #can choose any variable
```

```
##
     wardSol
                  \min
                            Q1
                                   median
                                                   QЗ
                                                             max
                                                                      mean
           1 0.000875 0.010000 0.01185938 0.03080625 0.8207778 0.0285163
           2 1.657163 6.206403 9.58750000 15.58437500 18.5875000 9.9628625
## 2
             sd
                  n missing
## 1 0.06644773 172
                          0
## 2 5.56052280 18
```

```
ggplot(df1, aes(x = as.factor(wardSol), y = Lithium)) +
  geom_boxplot() +
  theme_bw() +
  ggtitle("Boxplot of Concentration of Lithium by Cluster") +
  xlab("Cluster") +
  ylab("Concentration (mg/L)")
```



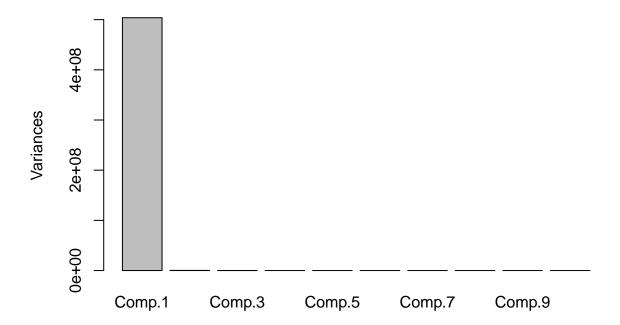


Our cluster sizes are extremely uneven... Our first clsuter has 172 wells and the second has 19.

We can view the solution in the PC space (say 2-D) to see how well-separated the clusters are in that space. Because we used an unstandardized distance, we will run the PCA on the covariance matrix.

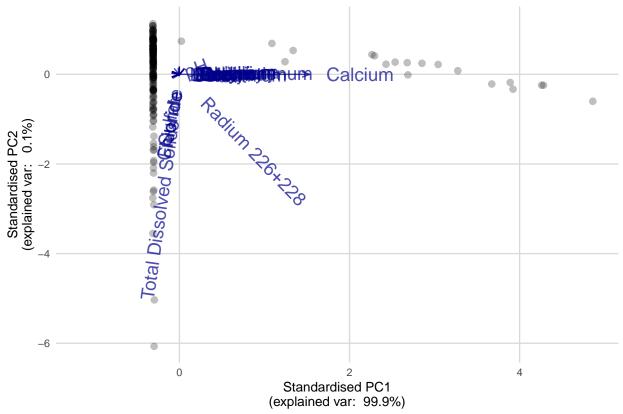
```
dfPCA <- princomp(df1[, -c(1:5)], cor = FALSE)
plot(dfPCA)</pre>
```

dfPCA



From the scree plot we generated above, we can see that the first PC captures essentially all the variation within our dataset.

AMR::ggplot_pca(dfPCA, base_textsize = 10, arrows_textsize = 5, arrows_alpha = 0.7)



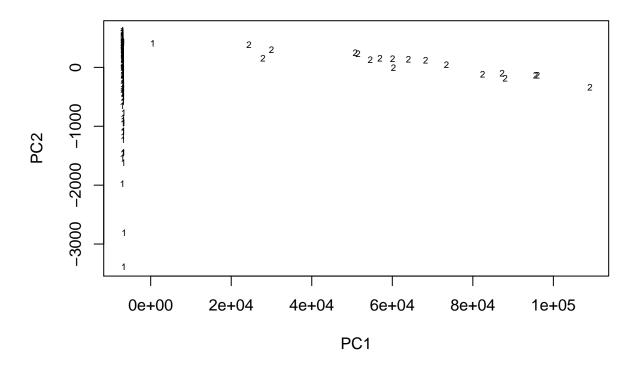
Total explained variance: 100.0%

Like we expected from our scree plot, all of the variance is explained in the first principal component. Since PC1 was heavily dominated by almost every single variable in the dataset - it could potentially indicate that it explains some sort of weighted average.

When two vectors are close, forming a small angle, the two variables they represent are positively correlated – we can see that every variable seems to be positively correlated with one another, except for radium 226+228 and Total Dissolved Solids. The right angle that the Total Dissolved Solids vector has with all the other contaminants gives us reason to believe that it has no correlation to any of the contaminants apart from Raidum 226+228.

```
plot(dfPCA$scores[, 1:2], type = "n", xlab = "PC1", ylab = "PC2", main = "Ward's cluster solution") #bl
text(dfPCA$scores[, 1:2], labels = wardSol, cex = 0.6) #add the text
```

Ward's cluster solution



A plot of our Ward's cluster solution shows that these wells do seem to be well separated from one another.

We may want to go into investigation to see what sort of traits/attributes are shared by the wells in each cluster and seeing if we can find meaning in them.

K-means Methods

For k-means, we don't need to compute the distance matrix ourselves. We feed the function the data set to operate on:

```
Ksol1 <- kmeans(scale(df1[, -c(1:5)]), centers = 2) #centers is the # of clusters desired list(Ksol1) #so you can see what it gives you
```

```
## [[1]]
## K-means clustering with 2 clusters of sizes 15, 175
##
## Cluster means:
##
       Antimony
                   Arsenic
                               Barium
                                       Beryllium
                                                      Boron
                                                               Cadmium
## 1
     3.3166216 2.5185136
                           2.7542737
                                       3.3165006 3.2073866
                                                            3.3164884 3.2539443
## 2 -0.2842818 -0.2158726 -0.2360806 -0.2842715 -0.2749189 -0.2842704 -0.2789095
##
        Chloride
                   Chromium
                                Cobalt
                                          Fluoride
                                                         Lead
                                                                 Lithium
## 1 -0.39372731
                 2.0374723
                             2.4266397 -0.13992310
                                                    2.3798126
##
     0.03374806 -0.1746405 -0.2079977
                                        0.01199341 -0.2039839 -0.2633415
##
        Mercury Molybdenum
                                    pH Radium 226+228
                                                        Selenium
## 1 3.3164896 2.5553332 0.58147104
                                           0.32016443 3.2236298 -0.54045694
```

```
## 2 -0.2842705 -0.2190286 -0.04984037
                      -0.02744267 -0.2763111 0.04632488
##
   Thallium Total Dissolved Solids
## 1 3.3151785
              -0.47664690
## 2 -0.2841582
              0.04085545
## Clustering vector:
  ##
 ## [186] 1 2 2 2 2
##
## Within cluster sum of squares by cluster:
## [1] 576.1418 1227.0094
 (between_SS / total_SS = 54.6 %)
##
## Available components:
##
## [1] "cluster"
           "centers"
                   "totss"
                           "withinss"
                                   "tot.withinss"
## [6] "betweenss"
           "size"
                   "iter"
                           "ifault"
```

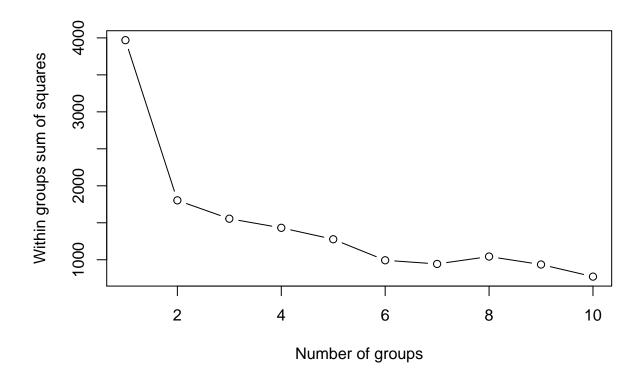
The list option provides us with lots of information. We can pull out the cluster means as:

Ksol1\$centers

```
Barium Beryllium
                                                              Cadmium
##
      Antimony
                  Arsenic
                                                     Boron
                                                                         Calcium
## 1 3.3166216 2.5185136 2.7542737
                                      3.3165006 3.2073866 3.3164884
                                                                       3.2539443
## 2 -0.2842818 -0.2158726 -0.2360806 -0.2842715 -0.2749189 -0.2842704 -0.2789095
                  Chromium
       Chloride
                               Cobalt
                                         Fluoride
                                                        I.ead
                                                                Lithium
## 1 -0.39372731 2.0374723 2.4266397 -0.13992310 2.3798126 3.0723177
## 2 0.03374806 -0.1746405 -0.2079977 0.01199341 -0.2039839 -0.2633415
                                   pH Radium 226+228
       Mercury Molybdenum
                                                       Selenium
## 1 3.3164896 2.5553332 0.58147104
                                          0.32016443 3.2236298 -0.54045694
                                         -0.02744267 -0.2763111 0.04632488
## 2 -0.2842705 -0.2190286 -0.04984037
##
      Thallium Total Dissolved Solids
## 1 3.3151785
                          -0.47664690
## 2 -0.2841582
                           0.04085545
```

In order to determine if we have chosen a "good" value of the number of clusters, we can look at the within cluster sum of squares for this solution and a few other options for k, the number of clusters. This runs the solution from 1 to 10 clusters and pulls the within group sum of squares from each.

```
n <- nrow(df1) #number of observations
wss <- rep(0, 10) #creates 10 copies of 0 to create an empty vector
for(i in 1:10){
   wss[i] <- sum(kmeans(scale(df1[, -c(1:5)]), centers = i)$withinss)
}
plot(1:10, wss, type = "b", xlab = "Number of groups", ylab = "Within groups sum of squares")</pre>
```



We look for elbows in the plot - here there are elbows at 2 and 6 (ish?), maybe these values will be good to use?

With two clusters, we should see if there is any relationship with sites...

There does seem to be something of interest here... The first cluster has a varied mix between all types with the majority in SI, while wells in cluster 2 seem to only consist of L.

We can compare clustering solutions with similar tables. How do the K-means and Ward's solutions overlap?

```
tally(Ksol1$cluster ~ wardSol, data = df1, format = "count")

## wardSol
## Ksol1$cluster 1 2
## 1 0 15
## 2 172 3
```

They seem to match up fairly well!

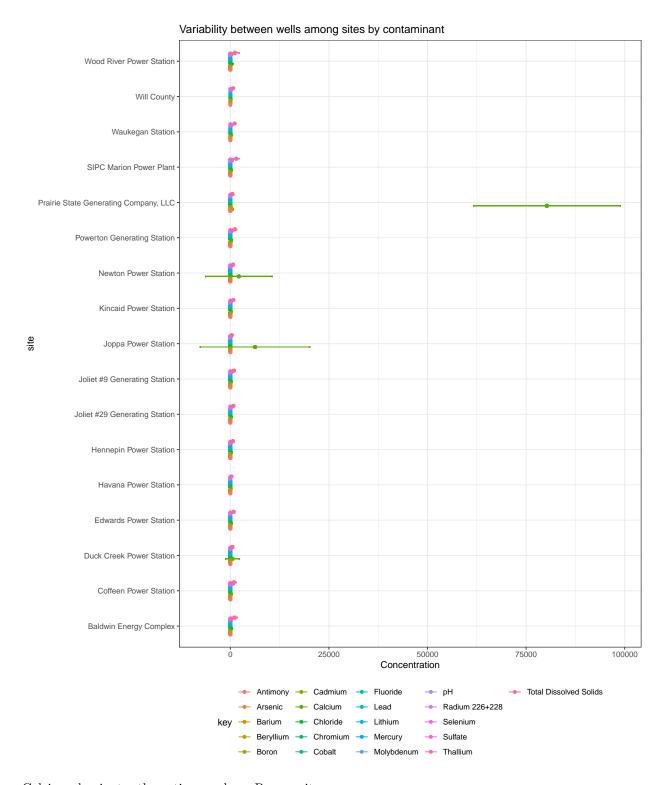
Can we try some sort of clustering algorithm where we don't have the specifiy the number of clusters (it automatically detects it for us? so that it might be able to differentiate between different severity/intensity levels of contamination)

Alternative Approaches

"If you haven't already, you can try some alternative filtering approaches: there might be a lot of contaminants that don't vary that much among the wells, so one thing you could do is find the contaminants with the highest between-well variability. For each chemical you can compute the variance across wells within a site, and take only the some number of contaminants (10? 20? Or 30?) with the highest variance, and then use those chemicals to do the PCA/k-means/hierarchical clustering."

```
df2 <- df1 %>%
  gather(key, value, c(6:26)) %>%
  group_by(site, key) %>%
  mutate(m = mean(value), sd = sd(value)) %>%
  arrange(desc(sd)) %>%
  print
## # A tibble: 3,990 x 9
## # Groups:
               site, key [357]
     well_id site
##
                          disposal area
                                          type gradient key
                                                                                  sd
                                                                 value
##
      <chr>
              <chr>>
                          <chr>
                                          <chr> <chr>
                                                          <chr>
                                                                <dbl>
                                                                        <dbl>
   1 G03D
                                                Upgradi~ Calc~ 5.85e4 80252. 18610.
##
              Prairie St~ Near Field Lan~ L
##
   2 G04D
              Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 1.03e5 80252. 18610.
##
  3 G05D
             Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 7.53e4 80252. 18610.
##
   4 G07D
             Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 9.43e4 80252. 18610.
  5 G08D
             Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 7.10e4 80252. 18610.
##
              Prairie St~ Near Field Lan~ L
##
   6 G10D
                                                Downgra~ Calc~ 1.03e5 80252. 18610.
              Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 9.51e4 80252. 18610.
##
  7 G13D
##
   8 G15D
              Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 1.16e5 80252. 18610.
## 9 G17D
              Prairie St~ Near Field Lan~ L
                                                Downgra~ Calc~ 8.94e4 80252. 18610.
              Prairie St~ Near Field Lan~ L
## 10 G19D
                                                Downgra~ Calc~ 6.16e4 80252. 18610.
## # ... with 3,980 more rows
df2 %>%
  ggplot(.) +
  theme_bw() +
  aes(x = site, y = m, ymin = m - sd, ymax = m + sd, color = key) +
  geom_point(position = position_dodge(width = 0.5)) +
  geom errorbar(position = position_dodge(width = 0.5)) +
  ylab("Concentration") +
  ggtitle("Variability between wells among sites by contaminant") +
  coord flip() +
  theme(legend.position="bottom")
```

Warning: Removed 21 rows containing missing values (geom_errorbar).



Calcium dominates the entire graph... Remove it...

```
df2 %>%
filter(key != "Calcium") %>%
ggplot(.) +
theme_bw() +
```

```
aes(x = site, y = m, ymin = m - sd, ymax = m + sd, color = key) +
geom_point(position = position_dodge(width = 0.5)) +
geom_errorbar(position = position_dodge(width = 0.5)) +
ylab("Concentration") +
ggtitle("Variability between wells among sites by contaminant (no calcium)") +
coord_flip() +
theme(legend.position="bottom")
```

Warning: Removed 20 rows containing missing values (geom_errorbar).

