

Reinforcement Learning Fundamentals

Lecture 3: RL Framework

Dr Sandeep Manjanna

Assistant Professor, Plaksha University

sandeep.manjanna@plaksha.edu.in

Some material in this lecture is taken from

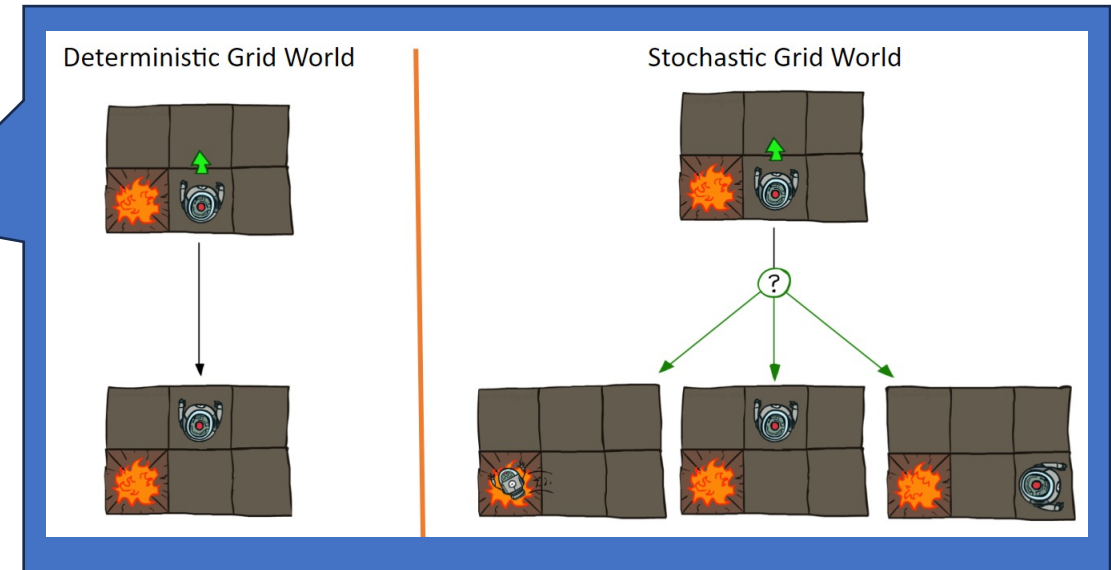
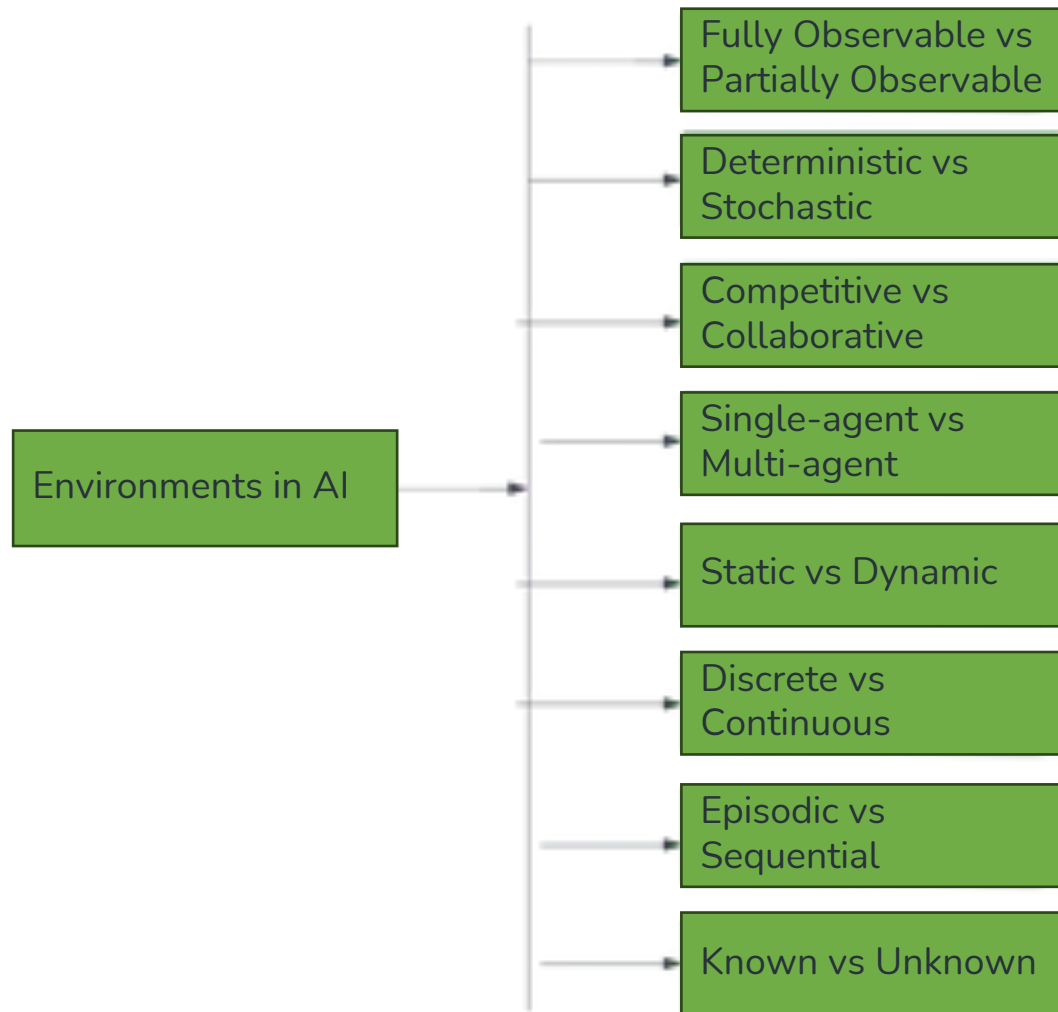
1. Prof. Ravindran's course: "Reinforcement Learning."
2. Dr Silver's course: "Reinforcement Learning."



In today's class...

- RL Framework
- What is a State?
- Special cases: Fully and Partially Observable environments
- Temporal Difference
- Components of an RL agent
 - Value function
 - Policy
 - Model
- Categories of RL

Types of Environments



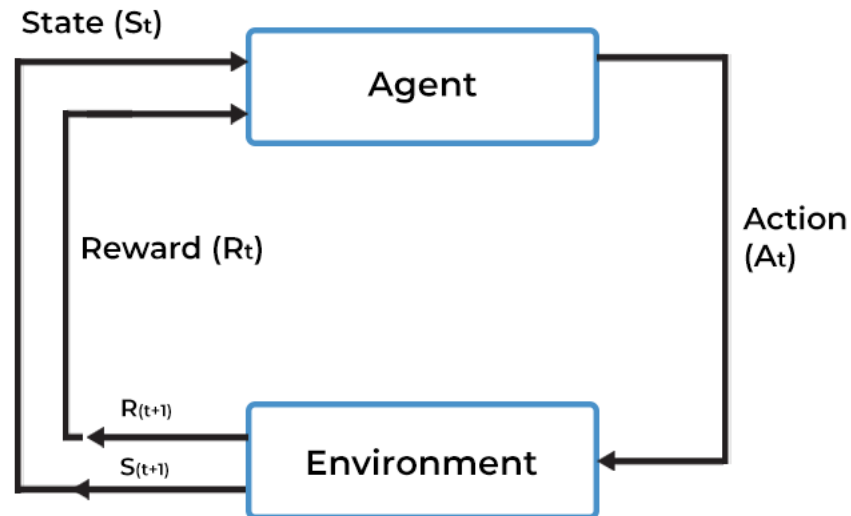
Fully Observable Environments

... extent to which the **agent has access to information about the current state of the environment.**

- A fully observable environment is one in which the **agent has complete information about the current state of the environment.**
- The agent has direct access to all environmental features that are necessary for making decisions.
- Example?

Board games like chess or checkers.

Full observability: agent **directly** observes environment state



$$O_t = S_t^a = S_t^e$$

- Agent state = environment state = information state
- Formally, this is a **Markov decision process** (MDP)

Partially Observable Environments

- A partially observable environment is one in which the **agent does not have complete information about the current state of the environment**.
- The agent can only observe a subset of the environment, and some aspects of the environment may be hidden or uncertain.
- Examples?
 - driving a car in traffic.
 - A trading agent only observes current prices.

Now agent state \neq environment state

Formally this is a **partially observable Markov decision process** (POMDP)

Agent must construct its own state representation S_t^a , e.g.

- Complete history: $S_t^a = H_t$
- **Beliefs** of environment state: $S_t^a = (\mathbb{P}[S_t^e = s^1], \dots, \mathbb{P}[S_t^e = s^n])$
- Recurrent neural network: $S_t^a = \sigma(S_{t-1}^a W_s + O_t W_o)$

Inside an RL Agent

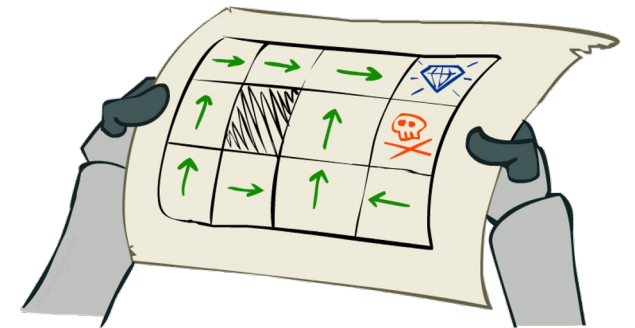
An RL agent may include one or more of these components:

- **Policy:** agent's behavior function
- **Value function:** how good is each state and/or action
- **Model:** agent's representation of the environment

Inside an RL Agent

Policy

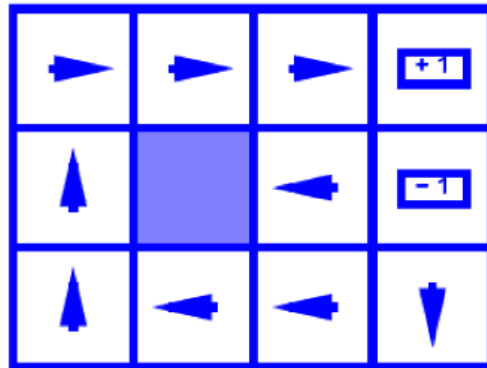
- A **policy** is the agent's behaviour
 - It is a map from state to action, e.g.
 - Deterministic policy: $a = \pi(s)$
 - Stochastic policy: $\pi(a|s) = \mathbb{P}[A_t = a|S_t = s]$
-
- In deterministic single-agent search problems, we wanted an optimal **plan**, or sequence of actions, from start to a goal
 - For MDPs, we want an optimal **policy** $\pi^*: S \rightarrow A$
 - A policy π gives an action for each state
 - An optimal policy is one that maximizes expected utility / value if followed
 - An explicit policy defines a reflex agent



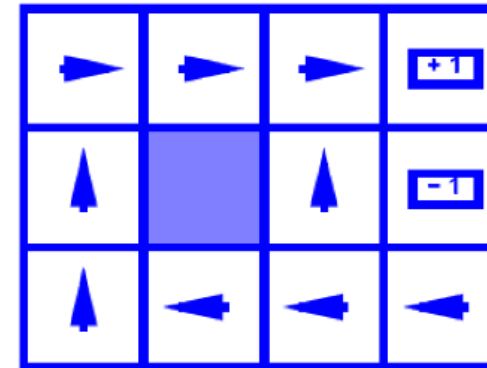
Inside an RL Agent

Policy

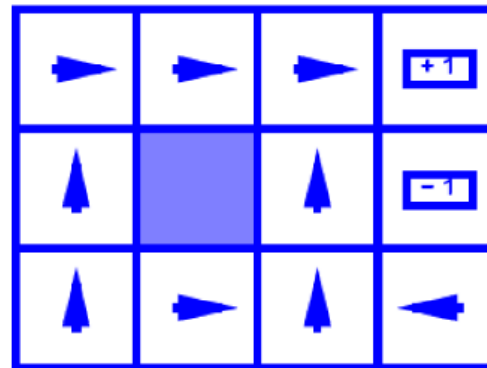
Optimal Policies



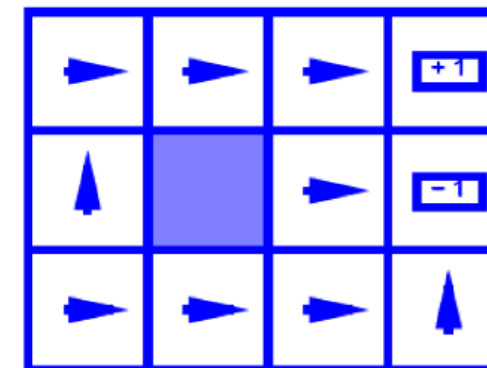
$$R(s) = -0.01$$



$$R(s) = -0.03$$



$$R(s) = -0.4$$



$$R(s) = -2.0$$

Inside an RL Agent

Value function

- Value function is a prediction of future reward
- Used to evaluate the goodness/badness of states
- And therefore to select between actions, e.g.

$$v_{\pi}(s) = \mathbb{E}_{\pi} [R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots \mid S_t = s]$$

Why Discounting?

- It's reasonable to maximize the sum of rewards
- It's also reasonable to prefer rewards now to rewards later
- One solution: values of rewards decay exponentially



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Worth Now



γ

Worth Next Step



γ^2

Worth In Two Steps

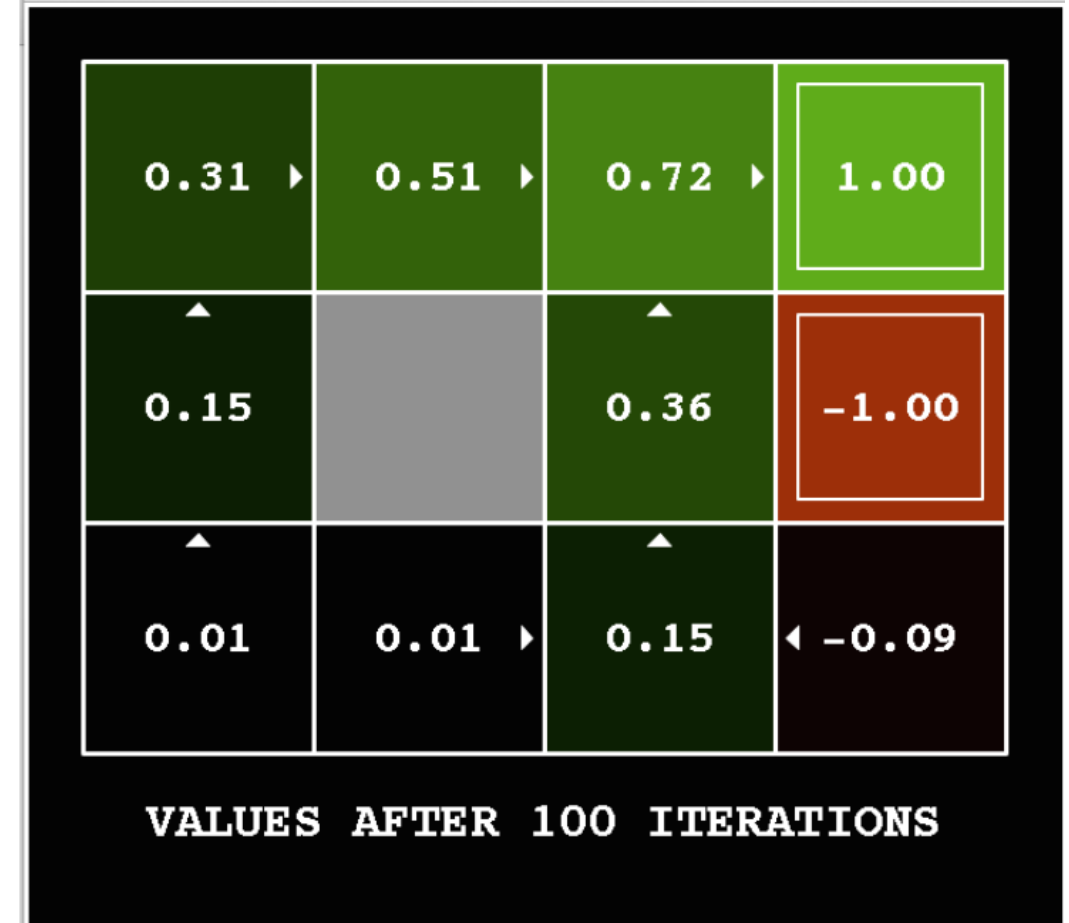
Inside an RL Agent

Value function

Living reward = 0



Living reward = -0.1



Inside an RL Agent Model

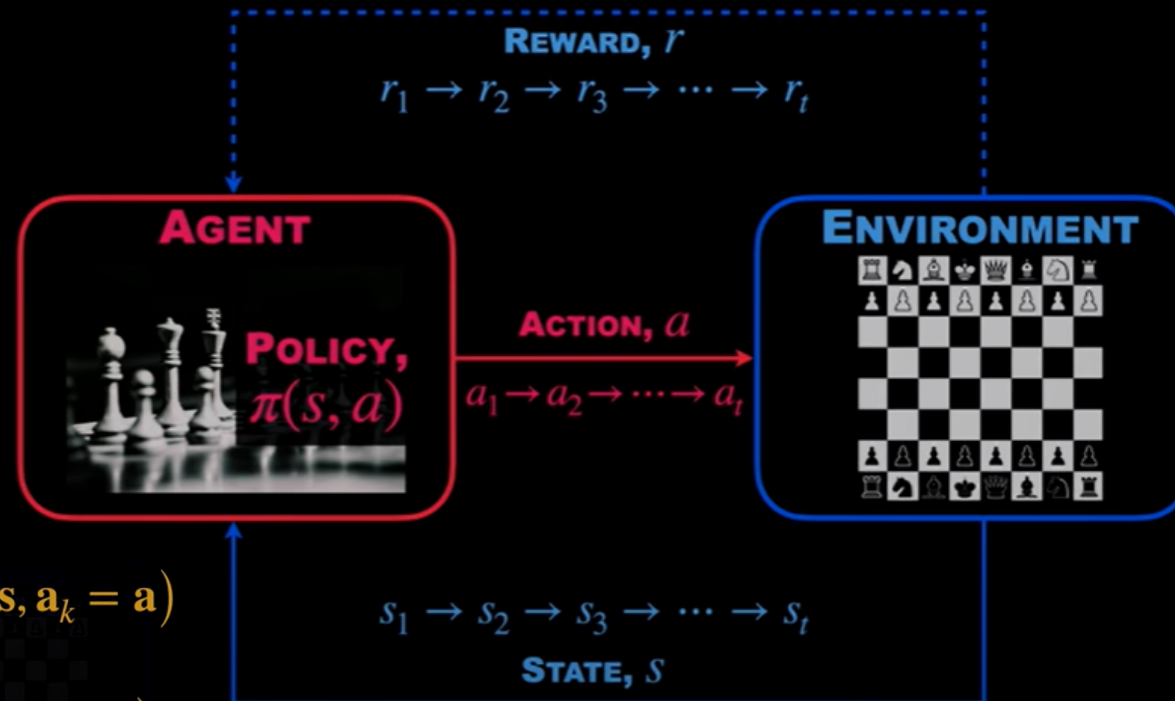
- A **model** predicts what the environment will do next
- \mathcal{P} predicts the next state
- \mathcal{R} predicts the next (immediate) reward, e.g.

Transition Model $\rightarrow \mathcal{P}_{ss'}^a = \mathbb{P}[S_{t+1} = s' \mid S_t = s, A_t = a]$

Reward Model $\rightarrow \mathcal{R}_s^a = \mathbb{E}[R_{t+1} \mid S_t = s, A_t = a]$

Inside an RL Agent

POLICY $\pi(s, a) = \Pr(a = a | s = s)$

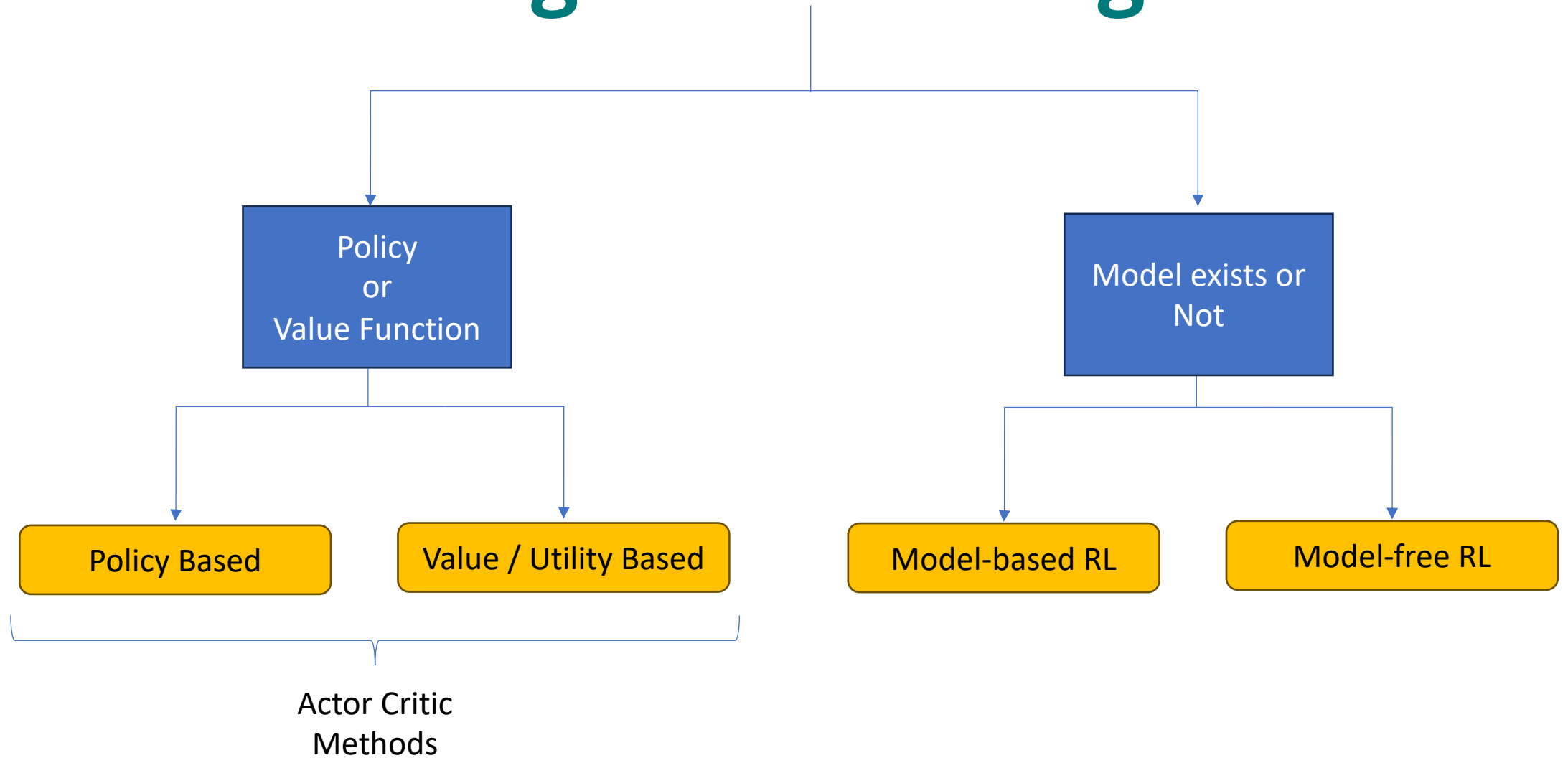


$$R(s', s, a) = \Pr(r_{k+1} | s_{k+1} = s', s_k = s, a_k = a)$$

$$P(s', s, a) = \Pr(s_{k+1} = s' | s_k = s, a_k = a),$$

VALUE $V_{\pi}(s) = \mathbb{E} \left(\sum_t \gamma^t r_t | s_0 = s \right)$
 DISCOUNT RATE

Categories of RL Agent



REINFORCEMENT LEARNING

Model-based RL

Markov Decision Process $P(s', s, a)$

Policy Iteration $\pi_{\theta}(s, a)$

Value Iteration $V(s)$

Actor
Critic

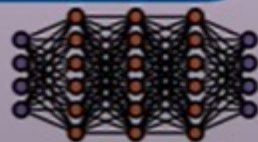
Dynamic programming
& Bellman optimality

Nonlinear Dynamics

$$\frac{d}{dt}\mathbf{x} = \mathbf{f}(\mathbf{x}(t), \mathbf{u}(t), t) dt$$

Optimal Control & HJB

Deep
MPC



Deep RL

Model-free RL

Gradient free

Off Policy

DQN

$Q(s, a)$

Q Learning

On Policy

TD(0)

\vdots

TD(∞) \equiv MC

TD- λ

SARSA

Gradient based

Deep
Policy
Network

$$\theta^{\text{new}} = \theta^{\text{old}} + \alpha \nabla_{\theta} R_{\Sigma, \theta}$$

Policy Gradient Optimization