

## WarmUp Class

# Advanced Variables & Operators

[Code - Data](#)

Quiz-Feedback

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# Objectives

## Review

- ❖ Variable
- ❖ Built-in Functions
- ❖ Basic Operators

## Advanced Operators

- ❖ Assignment Operator
- ❖ Relation Operator
- ❖ Logical Operator
- ❖ Precedence and Associativity

## Advanced Variable

- ❖ Overflow and Underflow
- ❖ Inf and NaN
- ❖ Floating point

## Exercise

- ❖ Velocity calculation
- ❖ Derivative definition
- ❖ Application
- ❖ Approximating derivative

# Outline

SECTION 1

## Review

SECTION 2

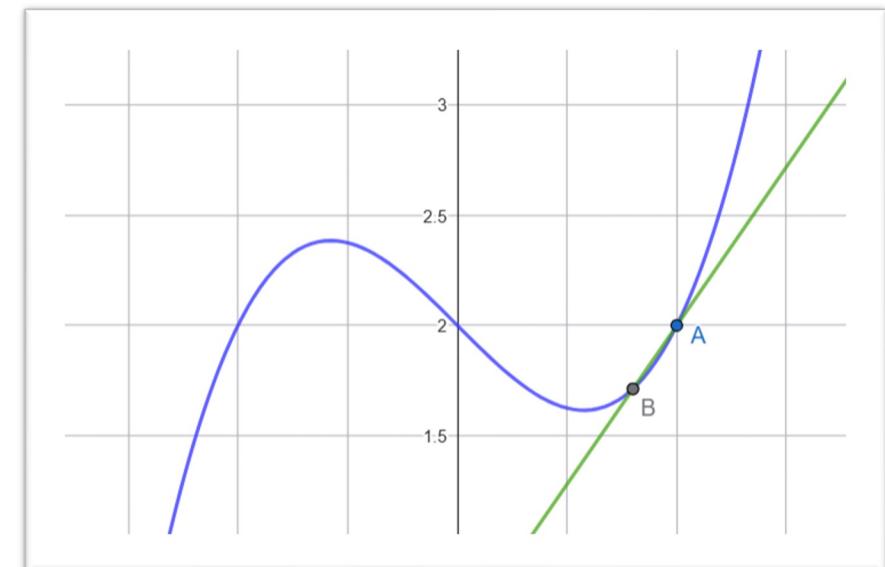
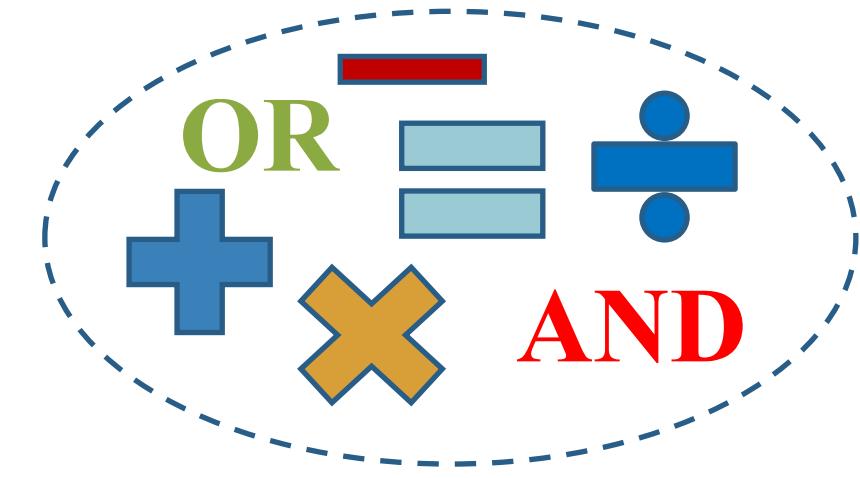
## Advanced Operators

SECTION 3

## Advanced Variable

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## Exercise



# Review



## Basics of Python



```
# An example of int
a = 5

# An example of float
b = 0.5

# An example of string
c = "AI Viet Nam"

# An example of bool
d = True
```

Variable\_name = Value

| Type    | Possible values         |
|---------|-------------------------|
| Int     | -3; 0; 5; 100;...       |
| Float   | 0.05; 3.5; 3.0;...      |
| String  | "AI", "AI Viet Nam";... |
| Boolean | True, False             |

# Review



## Basics of Python: Variables

**Notes:** Avoid variables' name that:

- Are Python keywords: print, return,...
- Start with numeric characters: 1, 2, 3...

```
▶ return = "Hello World"  
...   File "/tmp/ipython-input-2170012169.py", line 1  
      return = "Hello World"  
           ^  
SyntaxError: invalid syntax
```

```
▶ 1a = "Hello World"  
...   File "/tmp/ipython-input-3567537076.py", line 1  
      1a = "Hello World"  
           ^  
SyntaxError: invalid decimal literal
```

**Good practice:** Declaring meaningful names when possible!

```
▶ ● ○ ●  
a = 5 # km  
  
b = 2 # hours  
  
c = a/b # km/h
```

```
▶ ● ○ ●  
distance = 5 # km  
  
time = 2 # hours  
  
velocity = distance / time # km/h
```

# Review



## Basics of Python: Builtin-functions

### Print



```
a = 10
print(a)

b = 0.5
print(b)

c = "AI Viet Nam"
print(c)

d = True
print(d)
-----
10
0.5
AI Viet Nam
True
```

### Type



```
a = 10
print(type(a))

b = 0.5
print(type(b))

c = "AI Viet Nam"
print(type(c))

d = True
print(type(d))
-----
<class 'int'>
<class 'float'>
<class 'str'>
<class 'bool'>
```

# Review



## Basics of Python: Builtin-functions

### Type Conversion



```
a = 10.5
b = int(a)
print(b)
```

```
c = -1
d = bool(c)
print(d)
```

```
e = 0
f = bool(e)
print(f)
----
```

10  
True  
False

### Input



```
name = input("What is your name? ")
print("Hello, ", name)
----
```

What is your name? AI Viet Nam  
Hello, AI Viet Nam

Why!?

# Review



## Basics of Python: Operators

### Basic operators



```
A = 10
B = 4

print(A + B)
print(A - B)
print(A * B)
print(A / B)
print(A // B)
print(A % B)
-----
14
6
40
2.5
2
2
```

| Arithmetic Operator | Meaning          |
|---------------------|------------------|
| +                   | Addition         |
| -                   | Subtraction      |
| *                   | Multiplication   |
| /                   | Division (Float) |
| //                  | Division (Int)   |
| %                   | Modulo           |
| **                  | Power            |

# Outline

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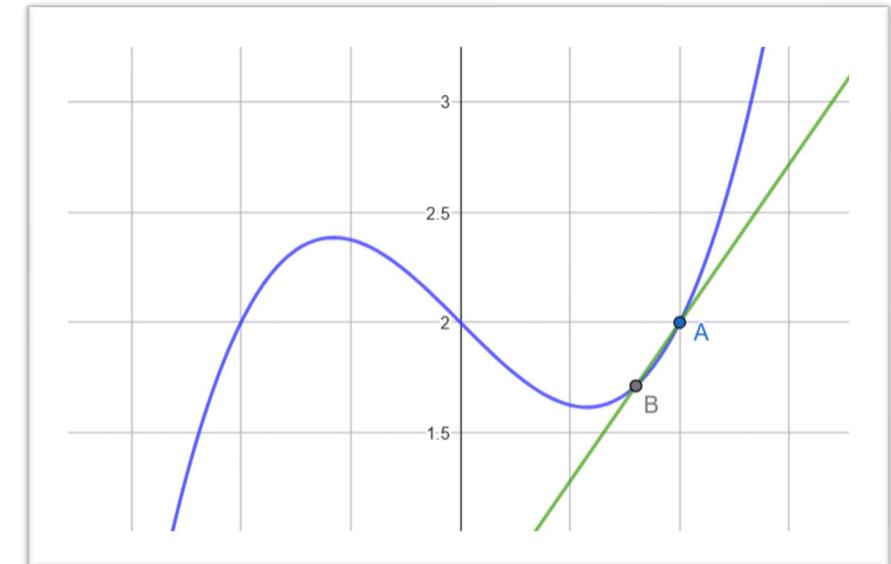
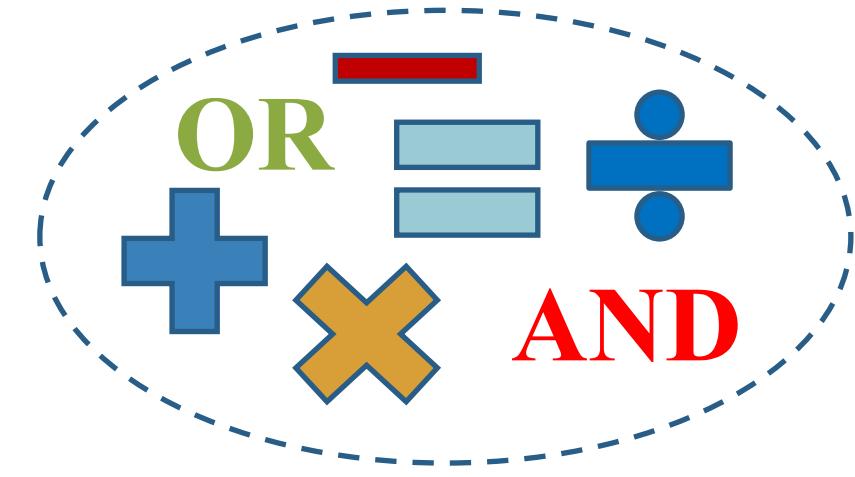
## Advanced Operators

SECTION 3

## Advanced Variable

SECTION 3

## Exercise



# Operators



## Operator overview

| Operator type        | Examples                        |
|----------------------|---------------------------------|
| Arithmetic operators | +,-, *, /, //, %, **            |
| Relational operators | <, <=, >, >=, ==, !=            |
| Logical operators    | AND, OR, NOT                    |
| Bitwise operators    | &,  , ^, ~, <<, >>              |
| Assignment operators | =, +=, -=, *=, /=, //=, %=, **= |

There are many types of operators in Python

# Assignment Operator



## Some assignment operators



```
a = 10  
b = 20
```

```
a += b  
print(a)
```

```
a -= b  
print(a)
```

```
a *= b  
print(a)
```

```
a /= b  
print(a)
```

```
30  
10  
200  
10.0
```

| Arithmetic Operator | Equivalent Assignment Operator |
|---------------------|--------------------------------|
| +                   | +=                             |
| -                   | -=                             |
| *                   | *=                             |
| /                   | /=                             |
| //                  | //=                            |
| %                   | %=                             |
| **                  | **=                            |

# Assignment Operator



## Why use assignment operators?

Correct but  
too long!



```
a_very_long_variable_name = 10
a_very_long_variable_name = a_very_long_variable_name + 10
print(a_very_long_variable_name)
-----
20
```

Much faster!



```
a_very_long_variable_name = 10
a_very_long_variable_name += 10
print(a_very_long_variable_name)
-----
20
```

# Relational Operator



## Some relational operators



```
a = 10  
b = 5
```

```
print(a > b)  
print(a >= b)  
print(a < b)  
print(a <= b)  
print(a == b)  
print(a != b)  
----  
True  
True  
False  
False  
False  
True
```

| Relational Operator | Meaning             | Example                                |
|---------------------|---------------------|--|
| >                   | Greater             | $10 > 5 \rightarrow \text{True}$       |
| $\geq$              | Greater or equal to | $10 \geq 10 \rightarrow \text{True}$   |
| <                   | Smaller             | $10 < 5 \rightarrow \text{False}$      |
| $\leq$              | Smaller or equal to | $10 \leq 5 \rightarrow \text{False}$   |
| $\equiv$            | Equal               | $10 \equiv 5 \rightarrow \text{False}$ |
| $\neq$              | Different           | $10 \neq 5 \rightarrow \text{True}$    |

# Relational Operator



## Example: Check if two number is the same

```
a = int(input("Enter the first number: "))
b = int(input("Enter the second number: "))

print("Two number is the same: ", a = b)
```

```
Enter the first number: 10
Enter the second number: 20
```



```
TypeError                                     Traceback (most
/tmp/ipython-input-2310854366.py in <cell line: 0>()
      2 b = int(input("Enter the second number: "))
      3
----> 4 print("Two number is the same: ", a = b)

TypeError: 'a' is an invalid keyword argument for print()
```

```
a = int(input("Enter the first number: "))
b = int(input("Enter the second number: "))

print("Two number is the same: ", a == b)
```

```
Enter the first number: 10
Enter the second number: 20
Two number is the same: False
```

What is the difference?

Common mistake in programming!

# Logical Operator



## Some logical operator



T = True

F = False

print(T and F)

print(T or F)

print(not T)

----

False

True

False

| A     | B     | A and B | A or B |
|-------|-------|---------|--------|
| True  | True  | True    | True   |
| True  | False | False   | True   |
| False | True  | False   | True   |
| False | False | False   | False  |

| A     | Not A |
|-------|-------|
| True  | False |
| False | True  |

- **And:** Only True when both A and B are True
- **Or:** Only False when both A and B are False
- **Not:** Reverse True and False

# Logical Operator



## Example: XOR operator



A = True  
B = True

```
print((A and (not B)) or ((not A) and B))
```

Result?

Fun fact: The above equation is equivalent to another operator in Python: XOR (^)



A = True  
B = True

```
print(A ^ B)  
-----  
False
```

**XOR:** Only True when A and B are different

| A     | B     | $A \wedge B$ |
|-------|-------|--------------|
| True  | True  | False        |
| True  | False | True         |
| False | True  | True         |
| False | False | False        |

# Order of operation



## How to calculate?

P

()

Parentheses

E

A<sup>2</sup>

Exponents

M

x

Multiplication

D

÷

Division

A

+

Addition

S

-

Subtraction



```
print(4 > 5 * 3)
```

----  
19

Easy calculation! Multiplication first,  
then addition later



```
print(4 + 5 * 3 ** 2 > 5 % 2 + 1)
```

!??

# Order of operation



## Precedence and Associativity



```
print(4 + 5 * 3 ** 2 > 5 % 2 + 1)
# 4 + 5 * 9 > 5 % 2 + 1
# 4 + 45 > 1 + 1
# 49 > 2
---
True
```

| Priority | Operator                            | Example                         |
|----------|-------------------------------------|---------------------------------|
| 1        | Power                               | **                              |
| 2        | Multiplication,<br>Division, Modulo | *, /, //, %                     |
| 3        | Addition, Subtraction               | +, -                            |
| 4        | Comparison                          | >, >=, <, <=                    |
| 5        | Equality comparison                 | ==, !=                          |
| 6        | Assignment operators                | =, +=, -=, *=, /=, //=, %=, **= |

# Outline

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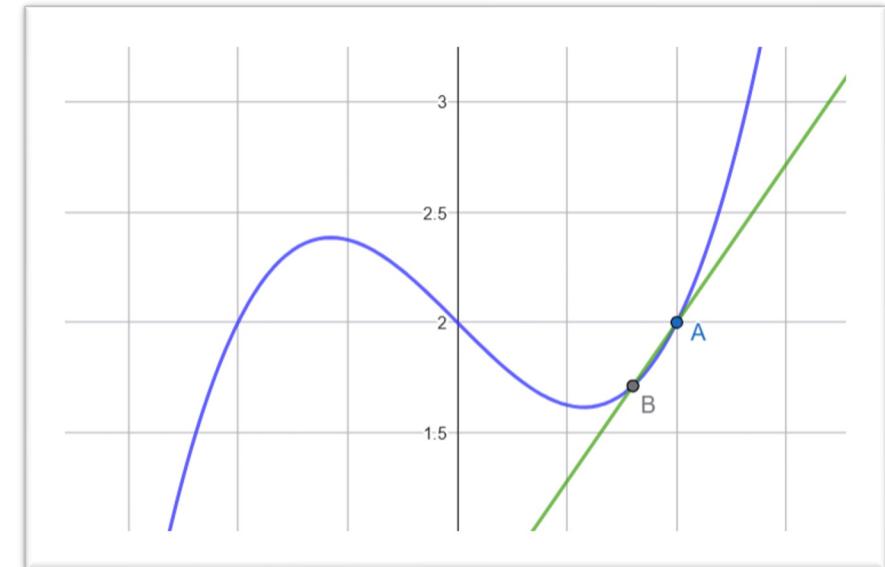
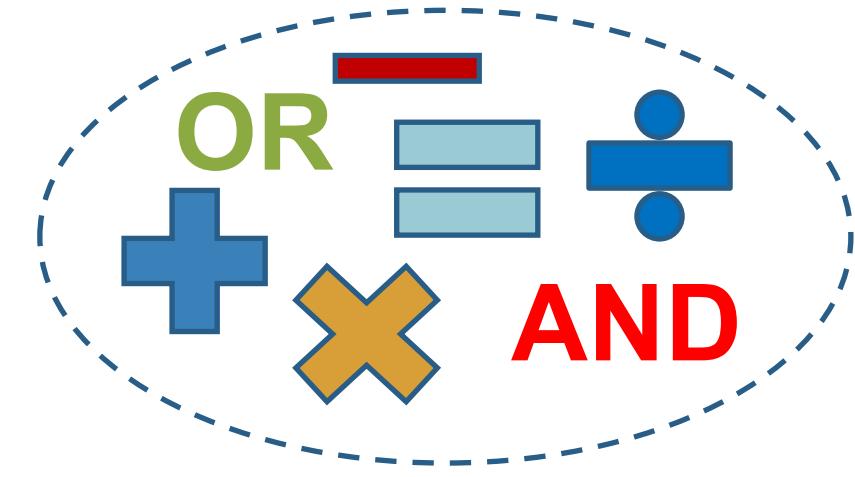
## Advanced Operators

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## Advanced Variable

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## Exercise



# Mutable and Immutable



## What are mutable and immutable objects?

Mutable objects: Objects that can be changed: list, set or dict

New item is added to the list

```
a = [1, 2, 3]
a.append(4)
print(a)
-----
[1, 2, 3, 4]
```

Immutable objects: Objects that cannot be changed: int, float, bool or string

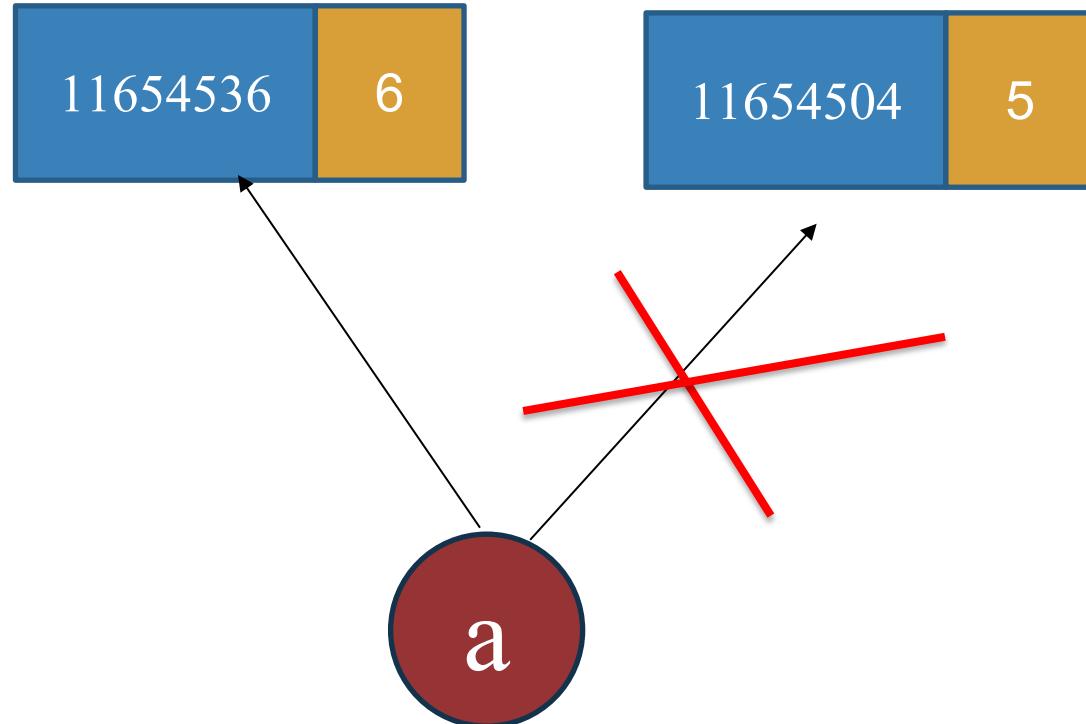
Wait, how can int, float or bool be immutable?

```
a = 10
a += 10
print(a)
-----
20
```

# Mutable and Immutable



## Immutable Object



Python does not change the value  
but create a new one instead



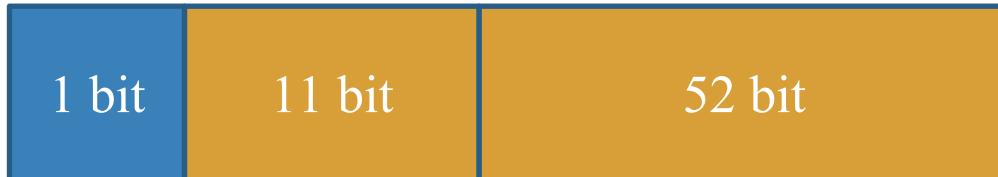
```
a = 5
print(id(a))
a = 6
print(id(a))
-----
11654504
11654536
```

ID: A number that indicates  
the address of the object

# Overflow and Underflow



## Underflow and Overflow in Python



```
a = 1e-400  
print(a)  
---  
0.0
```



```
a = 1e400  
print(a)  
---  
inf
```

Float in Python has its capacity

Underflow! The value becomes 0

Overflow! But what is that value?

# Inf



## Overflow in Python



```
a = 1e-400 # 10^400
print(a)
-----
0.0
```

Larger than the capacity of float in Python!



```
print(1e200, "*", 1e200, "=", 1e200 * 1e200)
-----
1e200 * 1e200 = inf
```

Be careful while doing calculation

Inf usually happens when overflow

# Inf



## Operator with inf

```
print(float('inf'))  
print(type(float('inf')))  
----  
inf  
<class 'float'>
```



```
print(float('inf')/100)  
print(float('inf') * float('inf'))  
print(float('inf') > 1e200)  
print(float('inf') == float('inf'))  
----  
inf  
inf  
True  
True
```



```
print(float('inf') * 0)
```

Inf in Python is considered as a float value

Can perform normal calculation

How about this? The result is 0 or inf?

# NaN



## What is NaN?



```
print(float('inf')*0)
print(float('inf') / float('inf'))
print(float('inf') - float('inf'))
print(pow(float('inf'), 0))
print(pow(1, float('inf')))
```

---

nan

nan

nan

1

1

NaN = Not a number

$\frac{0}{0}$ ,  $\frac{\infty}{\infty}$ ,  $\infty - \infty$ ,  $0 \cdot \infty$ ,  $0^0$ ,  $1^\infty$ ,  $\infty^0$ .

Usually happens when we perform “meaningless” calculation that leads to non-determinant form

But not all non-determinant form in Math will lead to NaN

## NaN



## NaN in raw data

|     | PassengerId | Survived | Pclass | Name                                     | Sex    | Age  | SibSp | Parch | Ticket           | Fare    | Cabin | Embarked |
|-----|-------------|----------|--------|--|--------|------|-------|-------|------------------|---------|-------|----------|
| 0   | 1           | 0        | 3      | Braund, Mr. Owen Harris                  | male   | 22.0 | 1     | 0     | A/5 21171        | 7.2500  | NaN   | S        |
| 2   | 3           | 1        | 3      | Heikkinen, Miss. Laina                   | female | 26.0 | 0     | 0     | STON/O2. 3101282 | 7.9250  | NaN   | S        |
| 4   | 5           | 0        | 3      | Allen, Mr. William Henry                 | male   | 35.0 | 0     | 0     | 373450           | 8.0500  | NaN   | S        |
| 5   | 6           | 0        | 3      | Moran, Mr. James                         | male   | NaN  | 0     | 0     | 330877           | 8.4583  | NaN   | Q        |
| 7   | 8           | 0        | 3      | Palsson, Master. Gosta Leonard           | male   | 2.0  | 3     | 1     | 349909           | 21.0750 | NaN   | S        |
| ... | ...         | ...      | ...    | ...                                      | ...    | ...  | ...   | ...   | ...              | ...     | ...   | ...      |
| 884 | 885         | 0        | 3      | Suthehall, Mr. Henry Jr                  | male   | 25.0 | 0     | 0     | SOTON/OQ 392076  | 7.0500  | NaN   | S        |
| 885 | 886         | 0        | 3      | Rice, Mrs. William (Margaret Norton)     | female | 39.0 | 0     | 5     | 382652           | 29.1250 | NaN   | Q        |
| 886 | 887         | 0        | 2      | Montvila, Rev. Juozas                    | male   | 27.0 | 0     | 0     | 211536           | 13.0000 | NaN   | S        |
| 888 | 889         | 0        | 3      | Johnston, Miss. Catherine Helen "Carrie" | female | NaN  | 1     | 2     | W./C. 6607       | 23.4500 | NaN   | S        |
| 890 | 891         | 0        | 3      | Dooley, Mr. Patrick                      | male   | 32.0 | 0     | 0     | 370376           | 7.7500  | NaN   | Q        |

Can also be found in raw data with missing/NaN values

# Approximation in Float



## How float is stored in Python



```
print(0.1 + 0.2 == 0.3)
-----
False
```

How!?



```
print(0.1 + 0.2)
-----
0.3000000000000004
```

Python only stored an approximation of the value, not the exact value

# Outline

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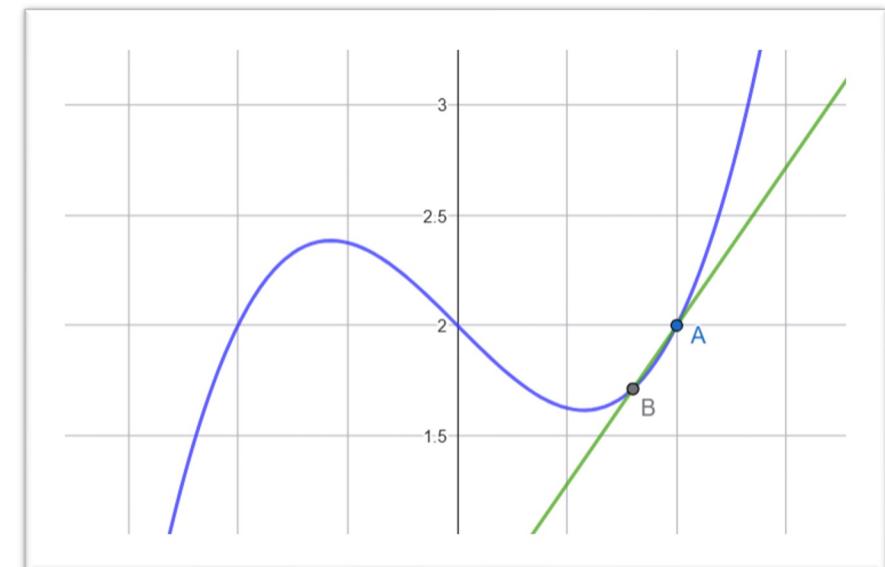
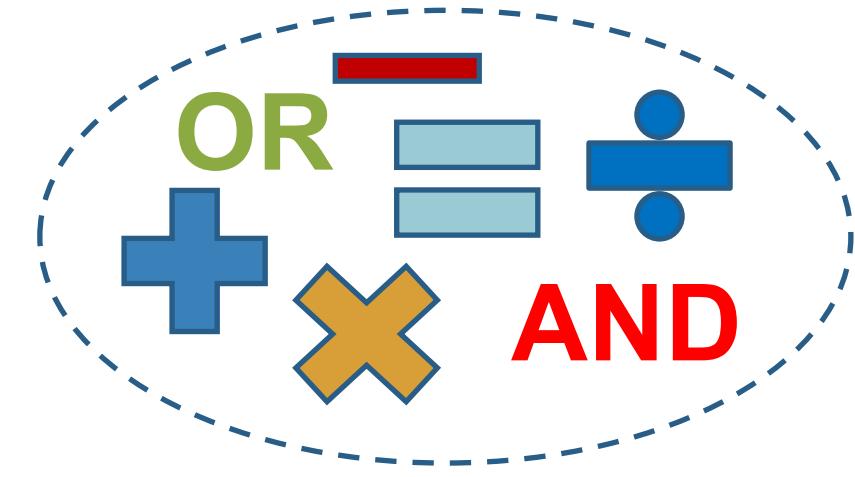
## Advanced Operators

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## Advanced Variable

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## Exercise



# Velocity calculation



## Problem #1

Calculating the average velocity from  $t = 1$  to  $t = 2$



Problem: A person travels from A to B with the following formula:

$$s(t) = t^2 + 2t$$



t1 = 1

t2 = 2

s1 = t1\*t1 + 2\*t1

s2 = t2\*t2 + 2\*t2

velocity = (s2 - s1) / (t2 - t1)

print(velocity)

-----

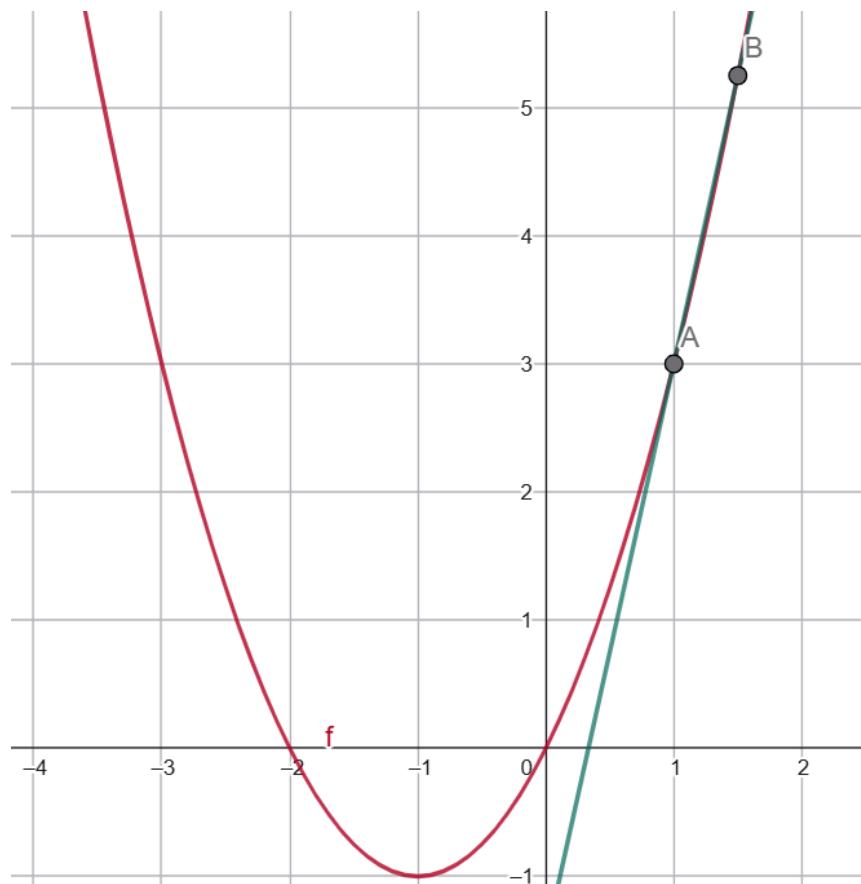
5.0

# Velocity calculation



## Problem #2

Calculating the average velocity from  $t = 1$  to  $t = 1.5$



Problem: A person travels from A to B with the following formula:

$$s(t) = t^2 + 2t$$



`t1 = 1  
t2 = 1.5`

```
s1 = t1*t1 + 2*t1  
s2 = t2*t2 + 2*t2  
velocity = (s2 - s1)/(t2 - t1)  
print(velocity)
```

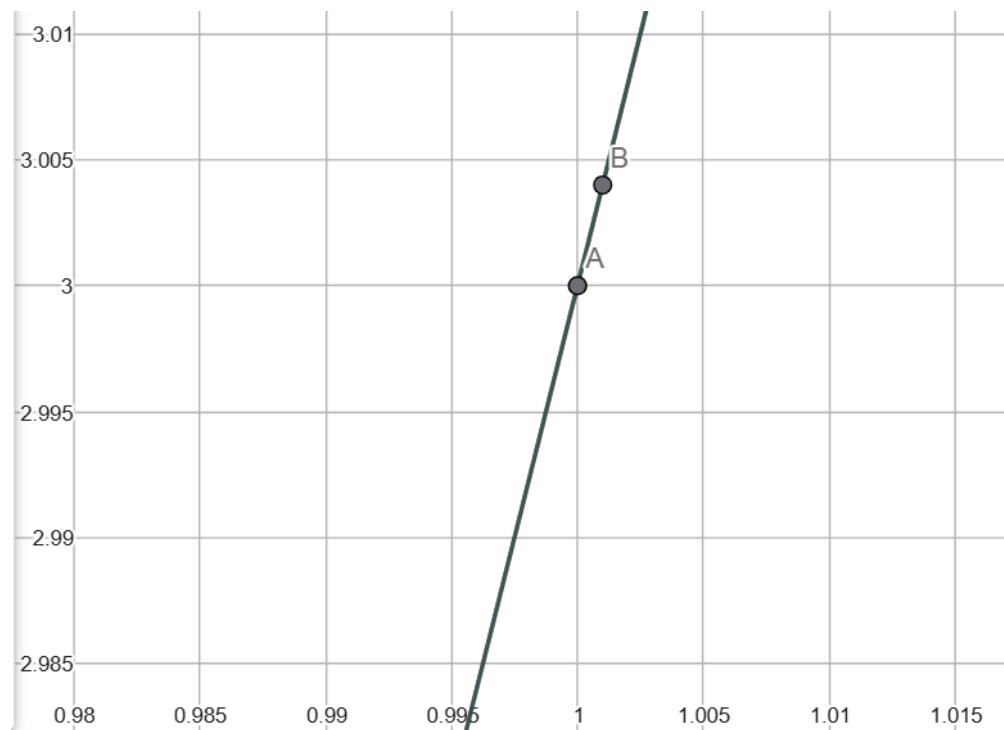
----  
4.5

# Velocity calculation



## Problem #3

Calculating the average velocity from  $t = 1$  to  $t = 1.001$



Problem: A person travels from A to B with the following formula:

$$s(t) = t^2 + 2t$$



`t1 = 1`  
`t2 = 1.001`

`s1 = t1*t1 + 2*t1`  
`s2 = t2*t2 + 2*t2`  
`velocity = (s2 - s1) / (t2 - t1)`  
`print(velocity)`

----

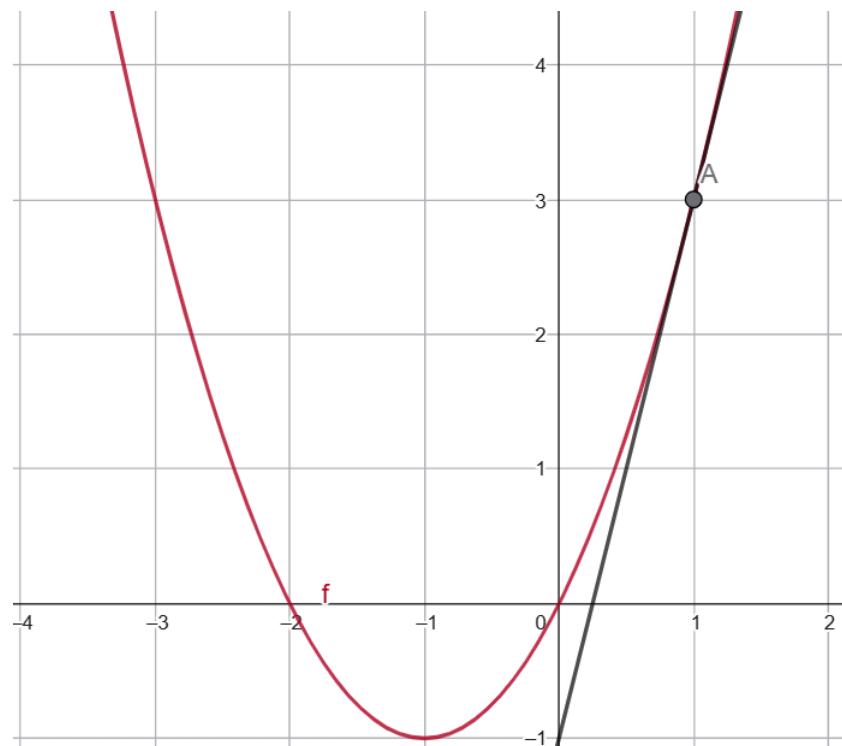
`4.00100000000014`

# Velocity calculation



## Problem #4

Calculating the instantaneous velocity at  $t = 1$ ?



Problem: A person travels from A to B with the following formula:

$$s(t) = t^2 + 2t$$

```
t1 = 1  
t2 = 1
```

```
s1 = t1*t1 + 2*t1  
s2 = t2*t2 + 2*t2  
velocity = (s2 - s1)/(t2 - t1)  
print(velocity)
```

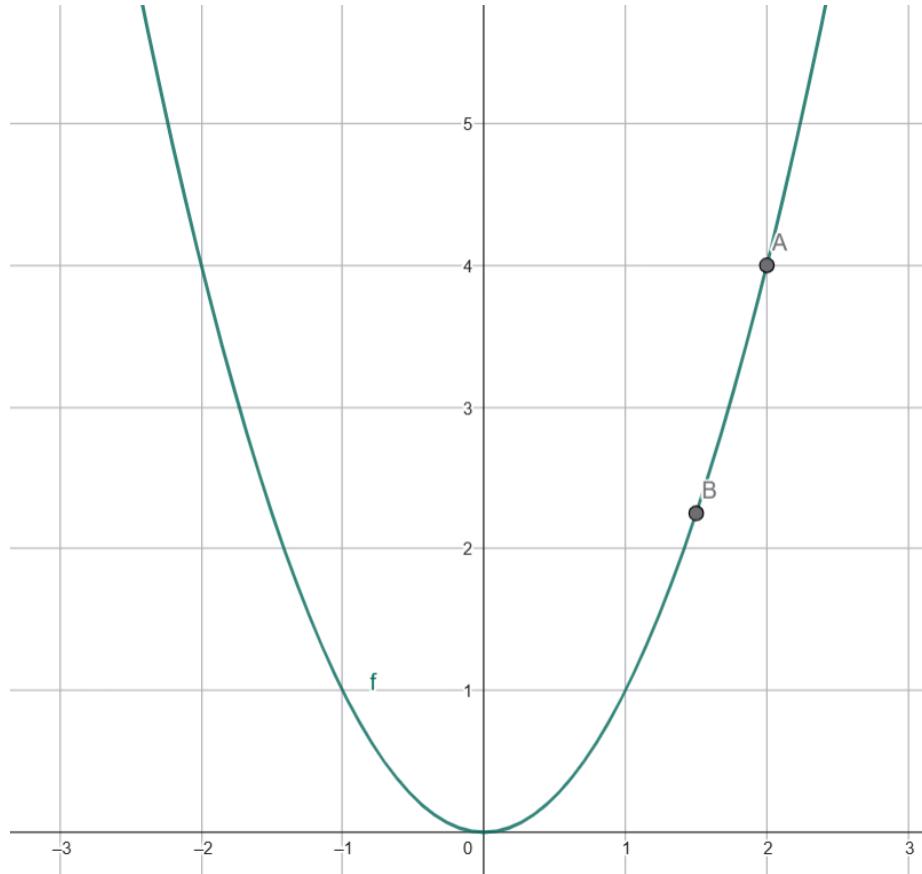
```
ZeroDivisionError  
/tmp/ipython-input-1802911845.py in <cell line: 0>()  
    4 s1 = t1*t1 + 2*t1  
    5 s2 = t2*t2 + 2*t2  
----> 6 velocity = (s2 - s1)/(t2 - t1)  
    7 print(velocity)
```

```
ZeroDivisionError: division by zero
```

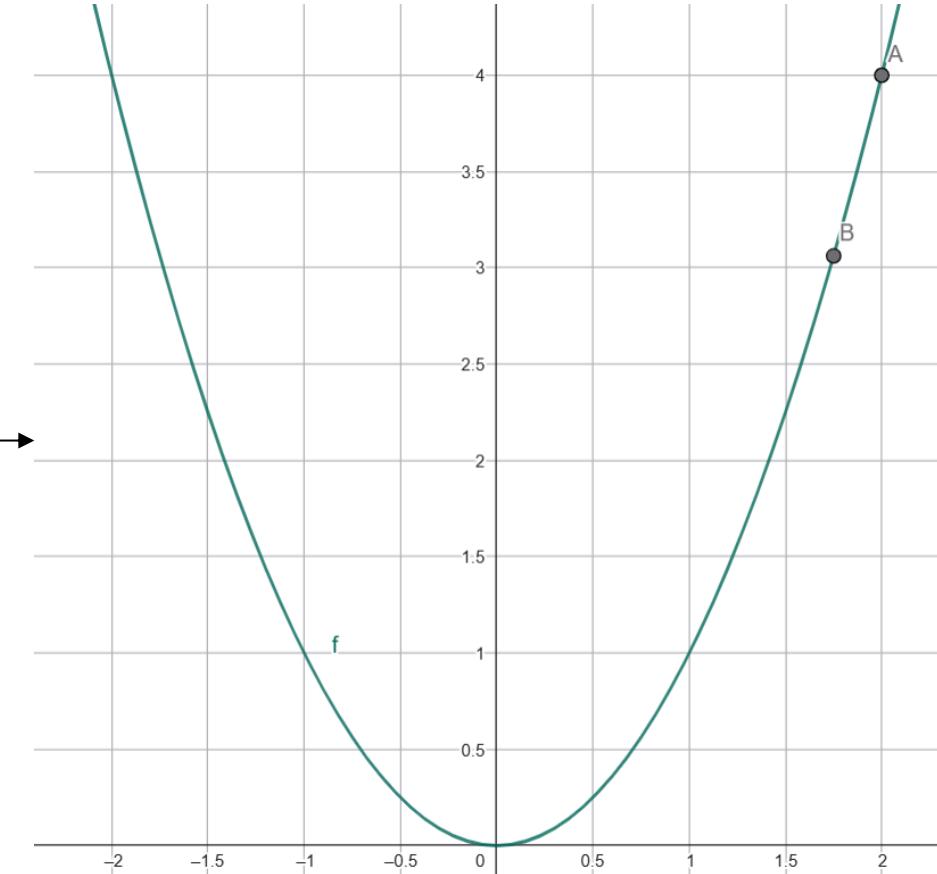
# Derivative



## Derivative illustration



Let B approach A

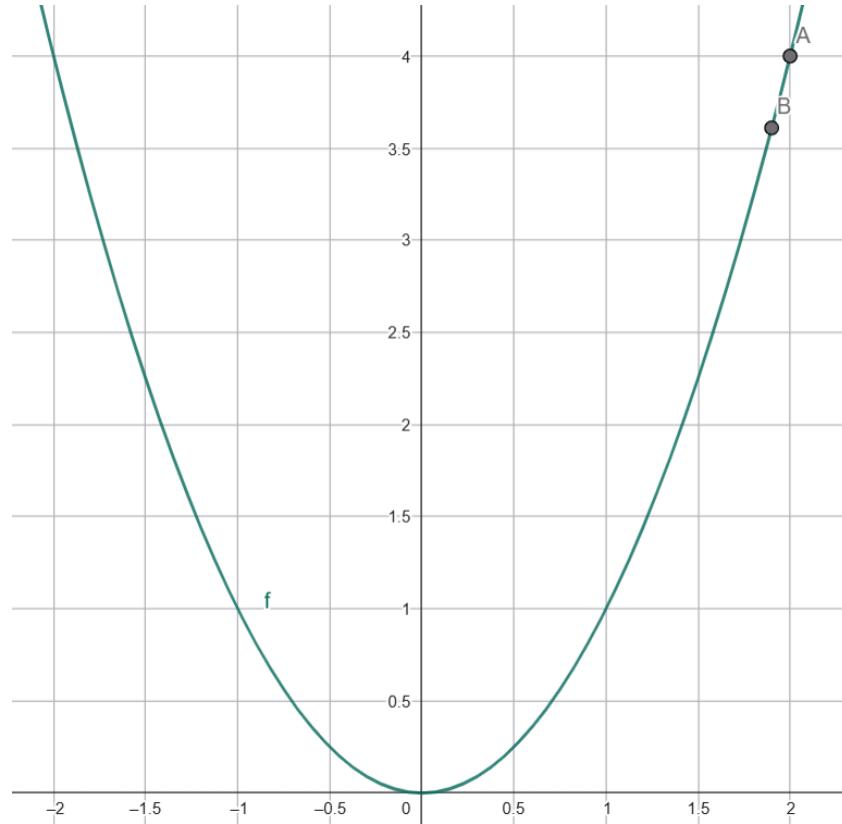


Let B approach closer

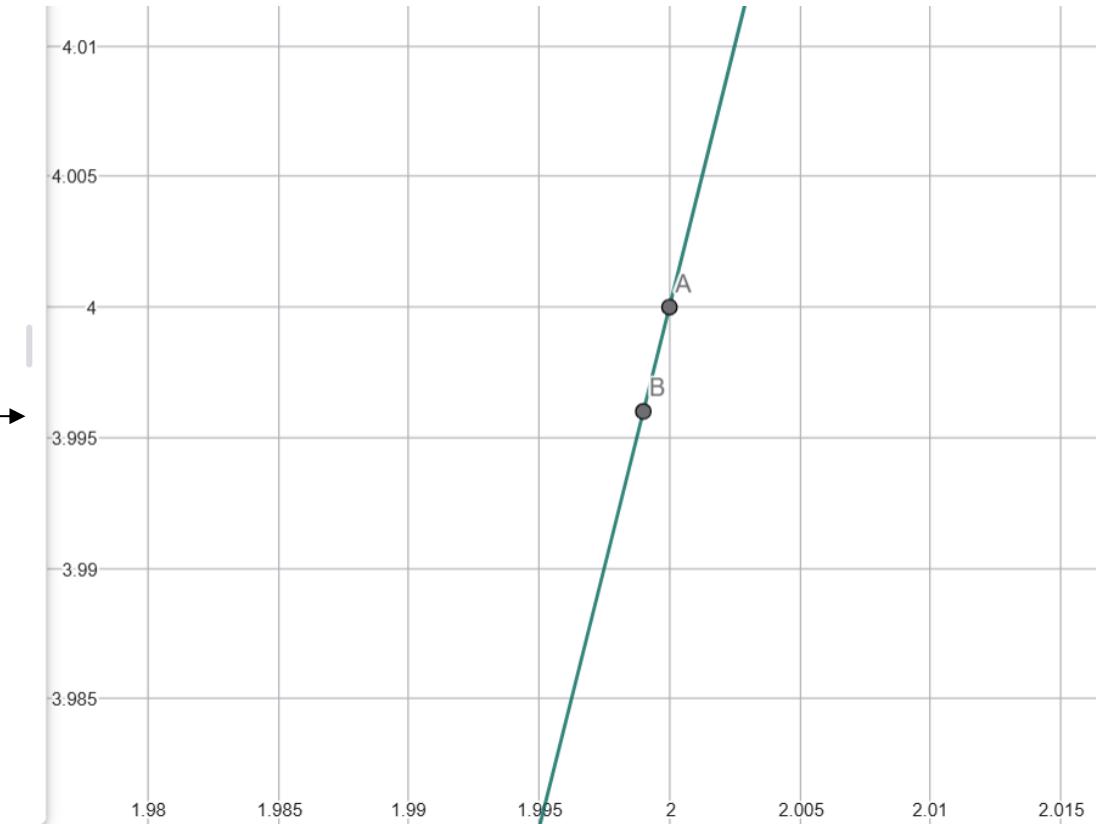
# Derivative



## Derivative illustration



Closer

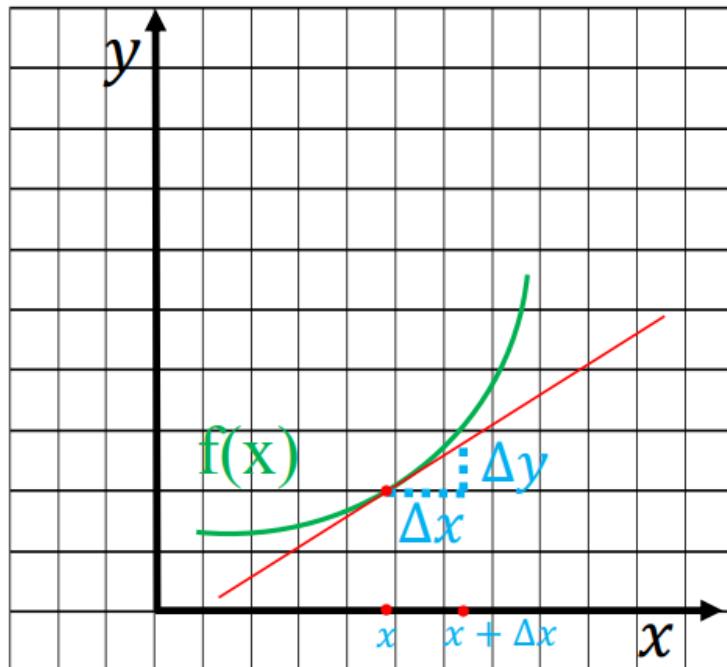


Can we make B even closer?

# Derivative



## Definition



$$\frac{d}{dx} f(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

Make  $\Delta x$  approaches 0.

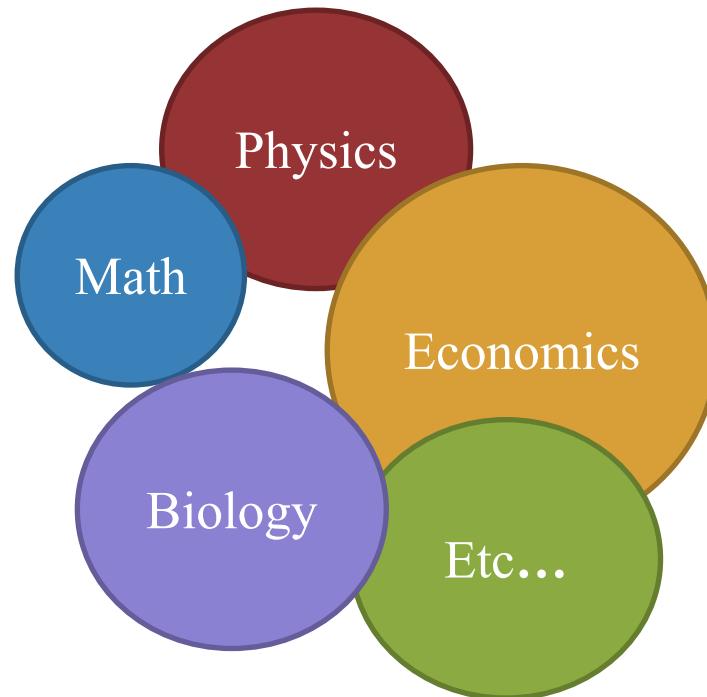
Notes: Approaches 0, not equal to 0

$$\frac{d}{dx} f(x), \frac{dy}{dx}, y', f'(x)$$

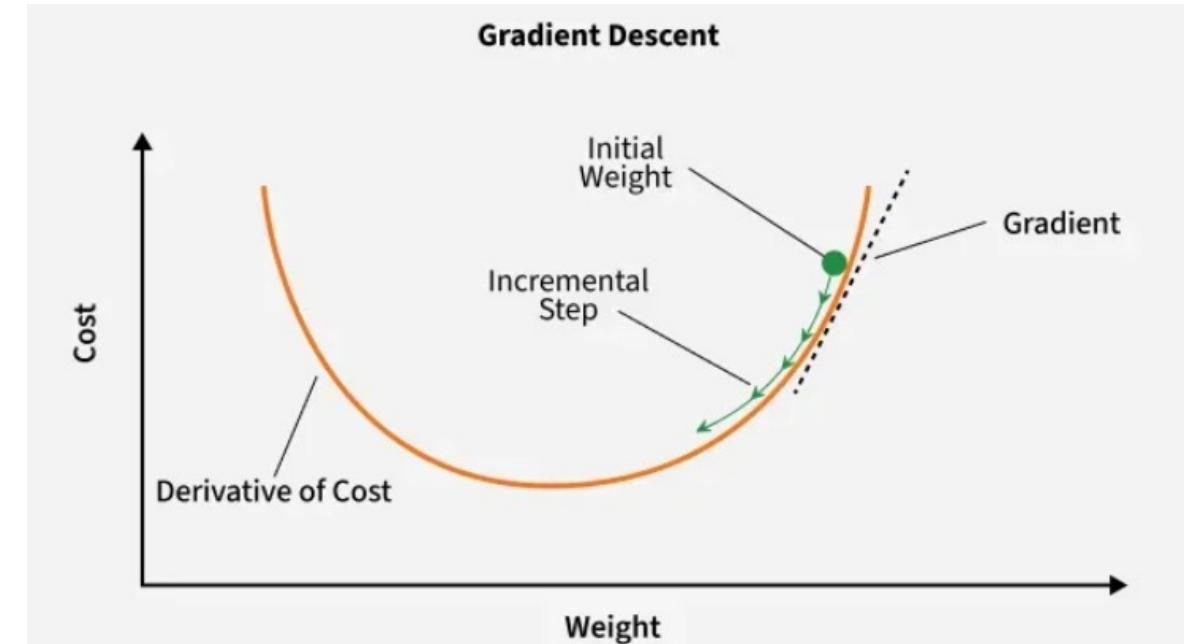
# Derivative



## Applications



Have applications in many fields



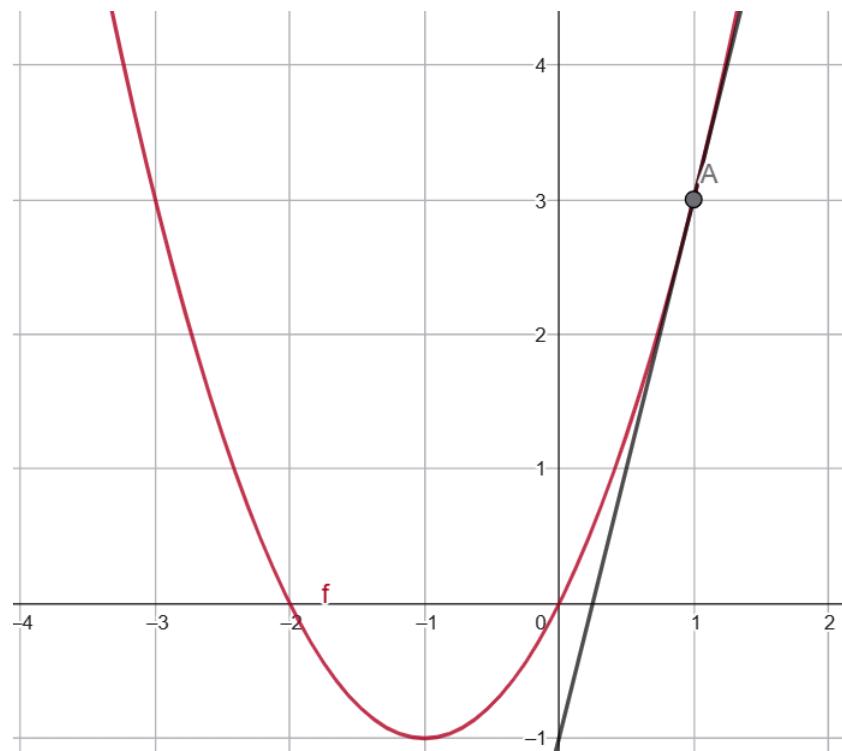
In AI: Gradient descent,...

# Velocity calculation



## Problem #4

Calculating the instantaneous velocity at  $t = 1$ ?



Problem: A person travels from A to B with the following formula:

$$s(t) = t^2 + 2t \rightarrow s'(t) = 2t + 2$$

Approximation

```
● ● ●  
t1 = 1  
t2 = 1.001  
  
s1 = t1*t1 + 2*t1  
s2 = t2*t2 + 2*t2  
velocity = (s2 - s1)/(t2 - t1)  
print(velocity)  
----  
4.00010000000014
```

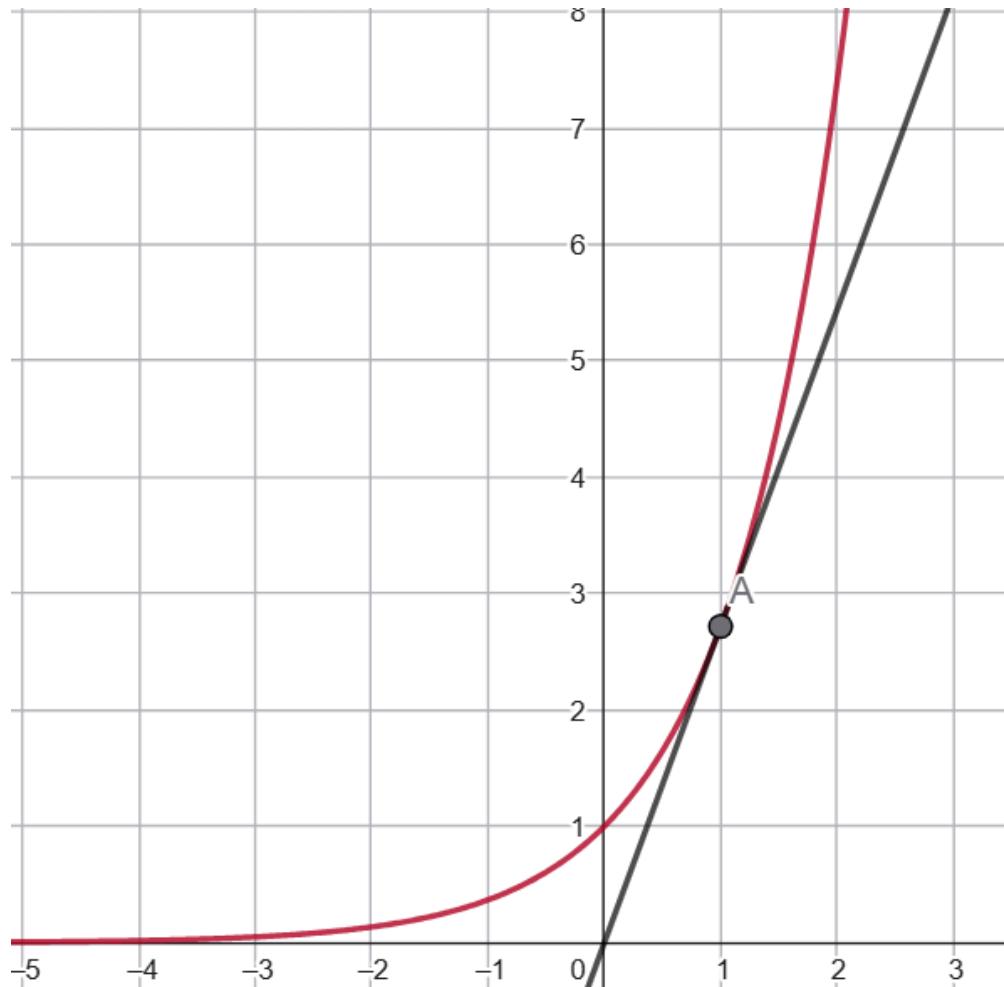
Correct result

```
● ● ●  
derivative = 2*t1 + 2  
print(derivative)  
----  
4
```

# Derivative



## Exercise: Approximating derivative



$$\frac{d}{dx} e^x = e^x$$

```
print(math.exp(x))
```

```
2.718281828459045
```



```
x = 1  
h = 0.5
```

```
f_x = math.exp(x)  
f_x_h = math.exp(x + h)
```

```
derivative = (f_x_h - f_x) / h  
print(derivative)
```

```
-----  
3.526814483758039
```



```
x = 1  
h = 0.1
```

```
f_x = math.exp(x)  
f_x_h = math.exp(x + h)
```

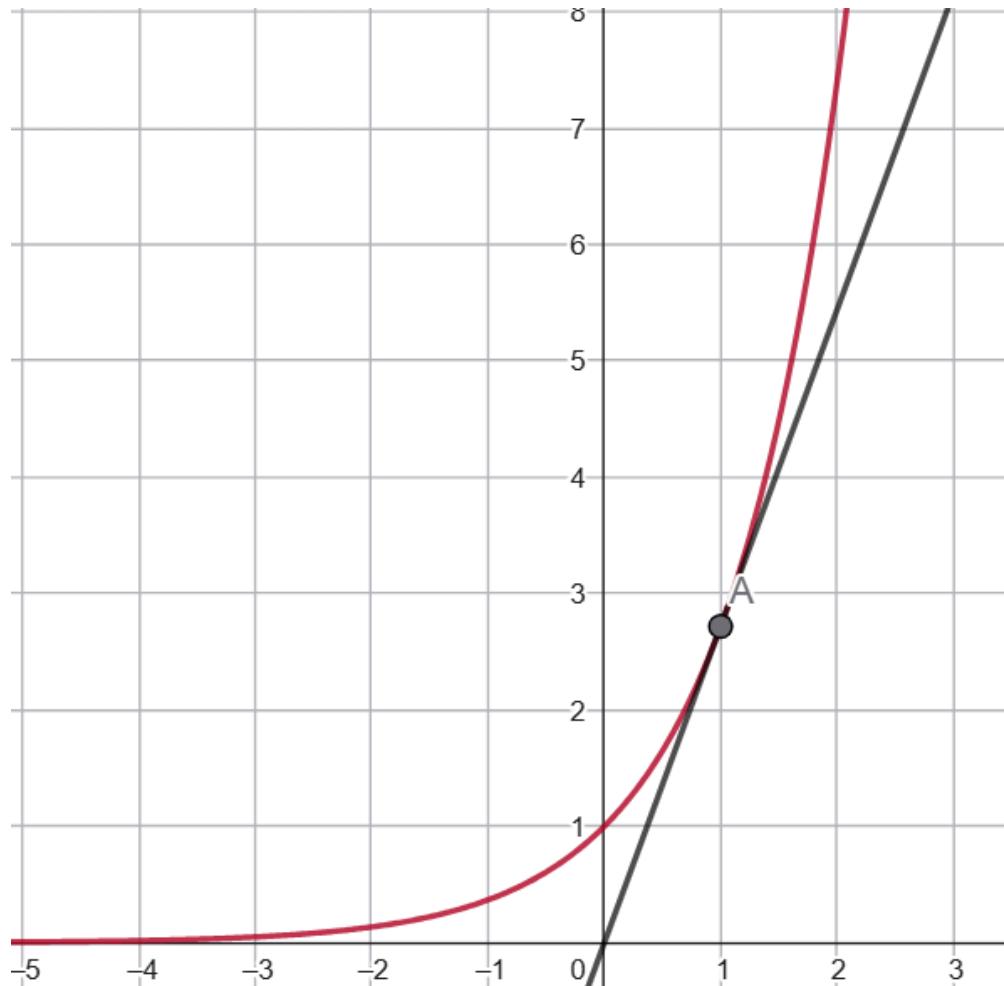
```
derivative = (f_x_h - f_x) / h  
print(derivative)
```

```
-----  
2.858841954873883
```

# Derivative



## Exercise: Approximating derivative



$$\frac{d}{dx} e^x = e^x$$



x = 1  
h = 0.01

```
f_x = math.exp(x)  
f_x_h = math.exp(x + h)
```

```
derivative = (f_x_h - f_x) / h  
print(derivative)  
----  
2.7319186557871245
```

```
print(math.exp(x))
```

```
2.718281828459045
```



x = 1  
h = 1e-20

```
f_x = math.exp(x)  
f_x_h = math.exp(x + h)
```

```
derivative = (f_x_h - f_x) / h  
print(derivative)  
----  
0.0
```

Why!?

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# QUIZ TIME

# Objectives

## Review

- ❖ Variable
- ❖ Built-in Functions
- ❖ Basic Operators

## Advanced Operators

- ❖ Assignment Operator
- ❖ Relation Operator
- ❖ Logical Operator
- ❖ Precedence and Associativity

## Advanced Variable

- ❖ Overflow and Underflow
- ❖ Inf and NaN
- ❖ Floating point

## Exercise

- ❖ Velocity calculation
- ❖ Derivative definition
- ❖ Application
- ❖ Approximating derivative

# Thanks!

Any questions?