Lag Penalized Weighted Correlation (LPWC)
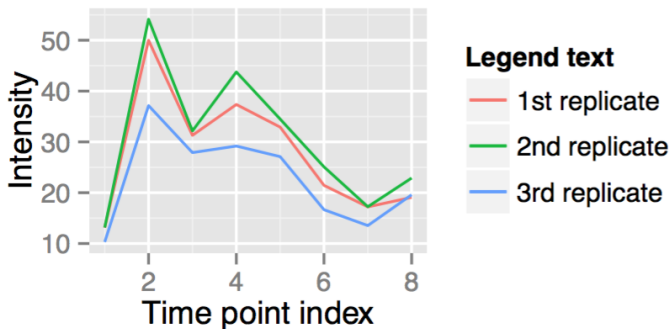
Thevaa Chandereng, Anthony Gitter

Figure 1: Simple time series plot with 8 time points and 3 replicates
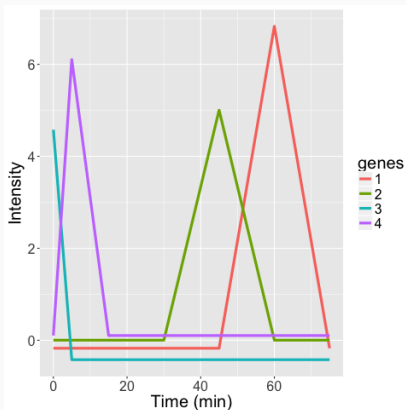
Existing Time Series Clustering Methods

Partition-based

- Short Time-series Expression Miner (STEM)
- Graphical Query Language (GQL)
- Cluster Analysis of Gene Expression Dynamics (CAGED)

Hierarchical-based

- Dynamic Time Warping (DTW)
- Short Time Series Distance (STS)

Toy Example: Algorithmic Clustering

(a) Hypothetical example with 4 genes

Clustering Algorithm	Cluster 1	Cluster 2
hLPWC/lLPWC	● ●	● ●
DTW	●	● ● ●
STS	●	● ● ●
heuc	●	● ● ●

(b) Cluster assignment of the 4 genes

Figure 2: Existing methods do not group early and late genes

Irregular time sampling

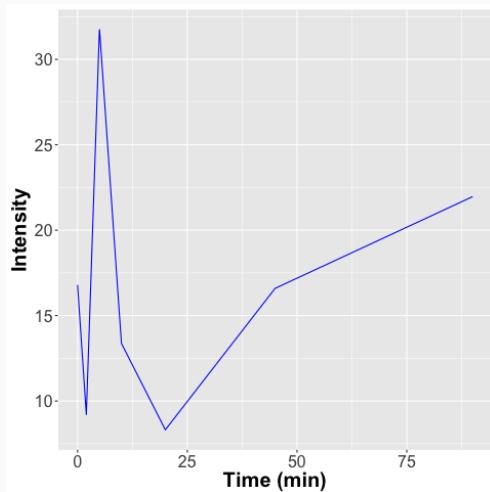**Figure 3:** Irregularly sampled time series data
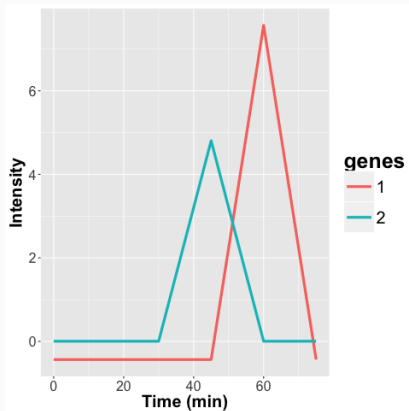
Motivation

Delayed response (lags)
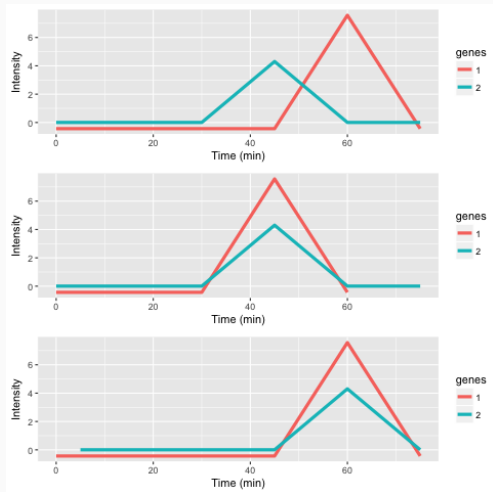

Figure 4: Gene 1 spikes after gene 2

Figure 5: This plot shows two genes that are lagged. The upper plot shows the actual intensity of the genes. The middle plot shows a -1 lag for gene 1 and the lower plot shows a lag of 1 for gene 2.

Method Overview

LPWC is composed of two steps:

- computing optimal lags for each gene
- computing final correlation matrix for all gene

General Formula

$$corr_{LPWC}(i, j, X_i, X_j) = exp(\frac{-E(w)}{C}) * corr_w(L^{X_i} Y_i, L^{X_j} Y_j, exp(\frac{-w}{C}))$$

Algorithm

Computing optimal lag

$$score_j = \max_{X_i \in \{-m,\ldots,m\}} corr_{LPWC}(i, j, X_i, 0) \quad \forall j \neq i$$

$$lag_j = \arg\max_{X_i \in \{-m,\ldots,m\}} corr_{LPWC}(i, j, X_i, 0) \quad \forall j \neq i$$

Then, a best lag $\hat{X}_i$ for gene i assigned by

$$\hat{X}_i = \arg\max_{k \in \{-m,\ldots,m\}} \sum_{j \neq i} I(lag_j = k) * score_j$$

This is repeated to select a best lag for all genes.

Computing final correlation matrix

$$corr_{LPWC}(i, j, \hat{X}_i, \hat{X}_j) = exp(\frac{-E(w)}{C}) * corr_w(L^{\hat{X}_i} Y_i, L^{\hat{X}_j} Y_j, exp(\frac{-w}{C}))$$
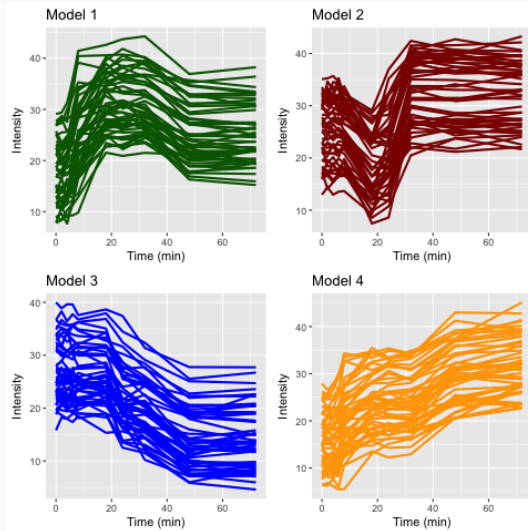
Figure 6: Four models simulated using ImpulseDE. Random noise was added to the model parameters to induce variation around a common trend.

Clustering Accuracy

- Adjusted Rand Index (ARI): similarity between two data clusterings and adjusted for chance
- ARI score close to 1 indicates similar clusterings, score close to 0 otherwise
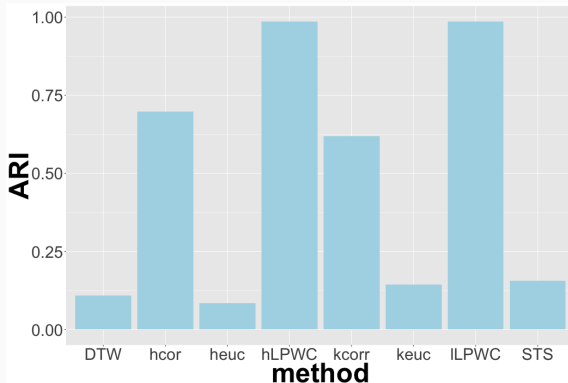
ARI Score for Simulated Data

Figure 7: ARI score for different clustering methods for the simulated data where the real clusters are known.

Conclusion & Future Work

- Algorithm tackles the issue of irregular time samples and delayed responses
- Preference for distance-based or correlation-based clustering is subjective
- R package available on CRAN (LPWC) and preprint on Bioarxiv
- Allow missing data (imputation)
- Support clustering a mixed dataset with different time points
- Improve the optimal lag assignments

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