

# day03

January 23, 2025

## 0.1 HW0

use `[q;q+1]` to get the  $(1, F)$  shape rather than `[q]` to get the  $(F, )$  shape

Be sure to vectorize the numpy object, don't write nested for loops > Great performance improvements

Try to start with for loops then move to vectorize

## 0.2 Linear Regression

Recall: MSE (mean square error)

Will be smooth everywhere (differentiable), unlike MAE (mean absolute error)

Goal: Minimize squared error

Objective function (J) - something we want to minimize

$\min_w(w)$  : means want to minimize objective w.r.t  $w$  (find the lowest  $w$ )

$J'(w) = 0$  (find the critical point)

Can use rise over run

Need to minimize the  $w$  by taking the derivative of the objective function w.r.t to  $w$ , and solving for  $w$  when  $J'$  is 0

When training for 1-dim no bias Linear regression, need 1  $x_i$  to be non-zero (or else zero in denominator)

$\Theta = [w_1 \dots w_F \ b] \sim x_n = [x_{n1} \dots x_{nF} \ 1]$

$\Theta^T \sim x_n$  is just dot product (inner product)

In “always holds”, we have  $(F+1, F+1) * (F+1, 1) = (F+1, N) * (N, 1)$  (dimensionality agrees)

if inverse exists: we have that  $\Theta$  has at least  $F + 1$  feature vectors that are linearly independent

Otherwise, many  $w, b$  will yield lowest possible training error