

Solving TSP using Genetic Algorithm

Genetic Algorithms can be used for the TSP problem as follows:

Create a population of candidate TSP solutions. Let the fitness ^{function} of the tour be the Cost.

It is a minimization problem.

we will use Path Representation, to start

In the Path Representation the tour is represented by a permutation of the cities, with the assumption that one returns from the last city in the permutation to the first.
 order of the cities visited.

Selection: Clone each tour in proportion to fitness. The cheapest tours are the fittest.

Crossover: Randomly pair the resulting population and perform crossover.

Mutation: Randomly permute a tour once in a while.

3 | 8 | 4 | 3 | 7 | 2 | 2 | 2 | 0 | 11 | A | J | M | 2 | 0

TSP: Single point crossover does not work

P₁:

O	D	G	L	A	H	K	M	B	J	F	C	N	I	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

P₂:

H	G	M	F	O	A	D	K	I	C	N	E	L	B	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

C₁:

O	D	G	L	A	H	K	M	B	J	N	E	L	B	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

C₂:

H	G	M	F	O	A	D	K	I	C	F	C	N	I	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Both offspring are not valid tours.

TSP: cycle crossover

P₁:

O	D	G	L	A	H	K	M	B	J	F	C	N	I	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

P₂:

H	G	M	F	O	A	D	K	I	C	N	E	L	B	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Step 1: Identify cycles

P₁:

O	D	G	L	A	H	K	M	B	J	F	C	N	I	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

1 2 2 3 1 1 2 2 4 5 3 5 3 4 5

P₂:

H	G	M	F	O	A	D	K	I	C	N	E	L	B	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Step 2: { C₁ gets even numbered cycles from P₂
C₁ gets odd numbered cycles from P₁

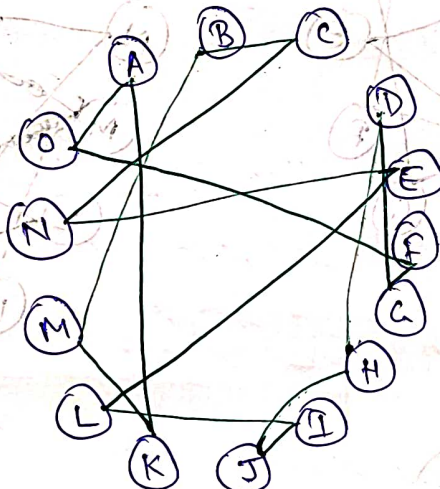
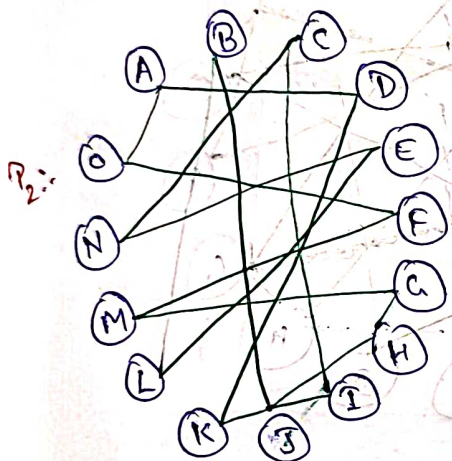
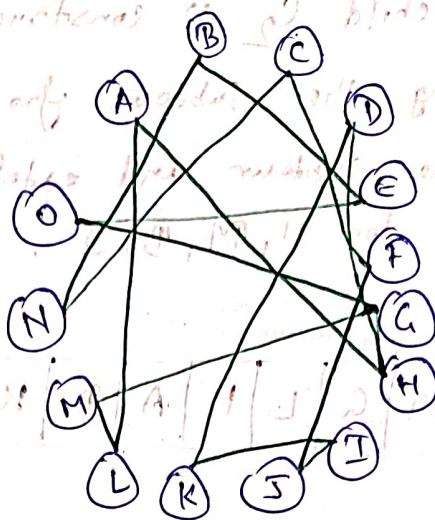
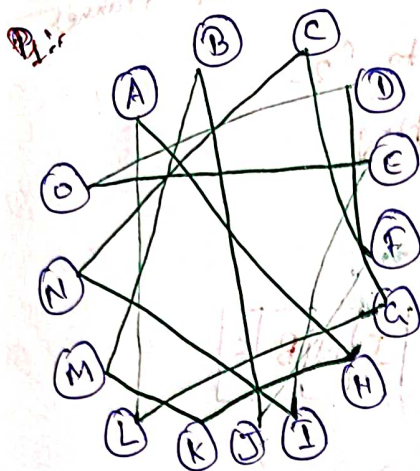
C₁:

O	G	M	L	A	H	D	K	I	J	F	C	N	B	E
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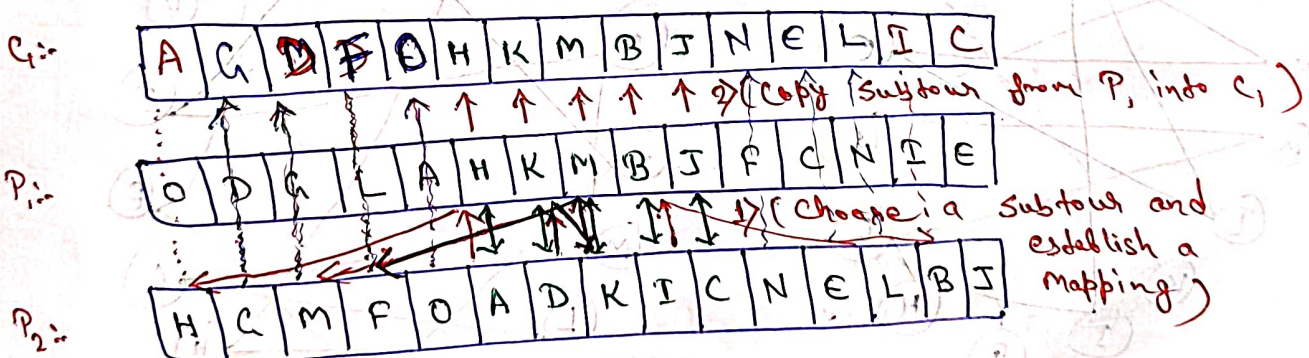
{ C₂ gets odd numbered cycles from P₂
C₂ gets even numbered cycles from P₁

C₂:

H	D	G	F	O	A	K	M	B	C	N	E	L	I	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---



TSP :: Partially Mapped Crossover (PMX)

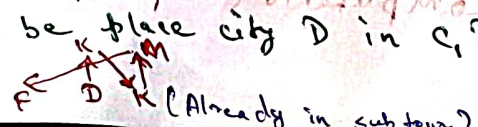


3) would like to copy remaining cities from P2, but the locations for cities A, D, I, C are occupied by cities H, K, B, J respectively

a) Where should city A be in G1?
Follow partial map...



b) Where should be place city D in G1?



c) Similarly do for I and C.

d) Remember that city K is already in G1.

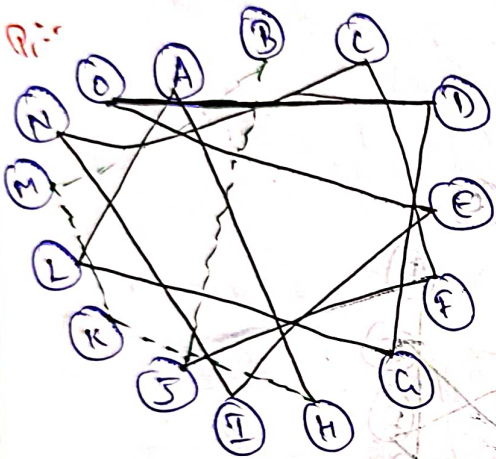
e) Copy the remaining cities from P2.

- The second child C_2 is constructed in a similar manner:
- 1) first copying the subtown from P_2 into C_2
 - 2) choose the subtown and establish mapping.
 - 3) Now, map from H, M, B, J.

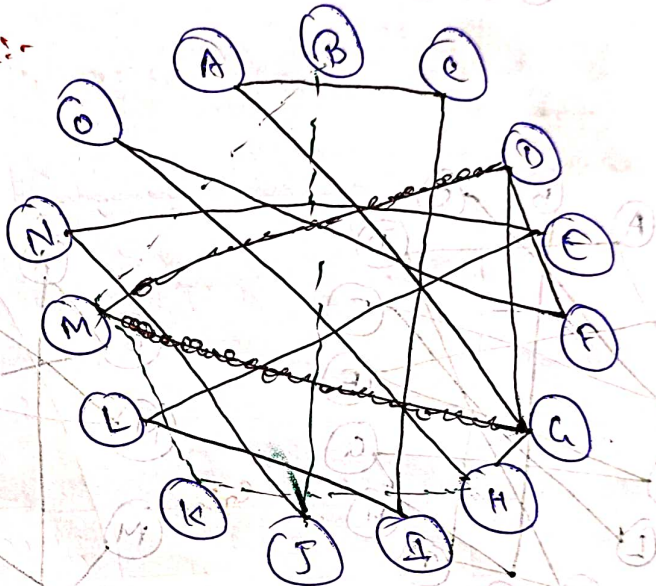
C_2 :-

O	M	G	L	H	A	D	K	E	C	F	J	N	B	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

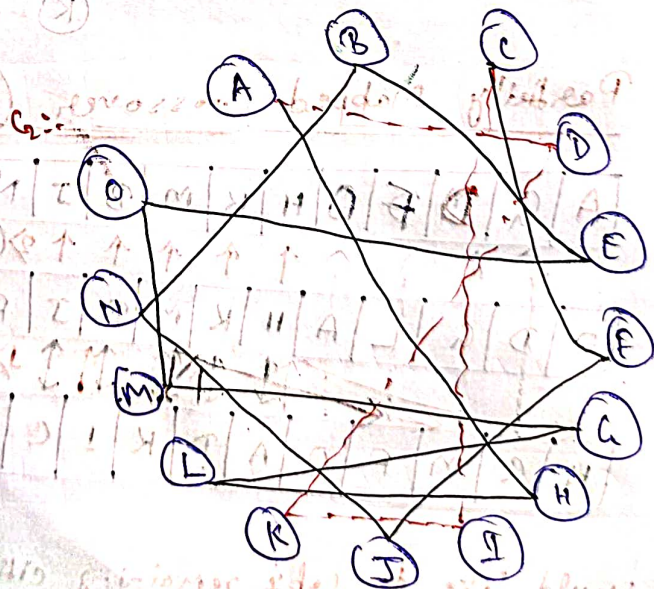
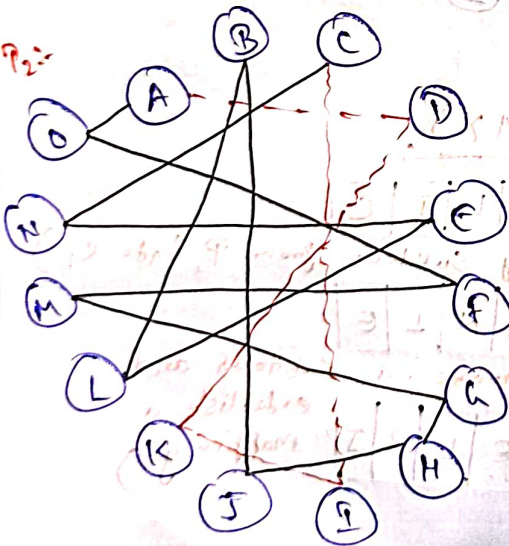
P_1 :-



C_1 :-



P_2 :-



Note :- Instead of choosing random subtown, we can use heuristic value to choose subtown and do the computation.

Minimum cost

PSP :: order crossover, not to be used for permutation A :: 921

P₁ ::

O	D	G	L	A	H	K	M	B	J	F	C	N	E
---	---	--------------	---	---	---	---	---	---	---	---	---	---	---

P₂ ::

H	G	M	F	O	A	D	K	I	C	N	E	L	B	J
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

C₁ ::

G	F	O	A	D	H	K	M	B	J	I	C	N	E	L
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

C₂ ::

O	G	L	H	M	A	D	K	I	C	B	J	F	N	E
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

1) Copy subtown from P₁ to C₁
 2) The remaining from P₂ in the order they occur in P₂.

1) Copy subtown from P₂ to C₂
 2) The remaining from P₁ in the order they occur in P₁.

I	B	J	E	H	O	I	K	D	A	O	F	M	D	H
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

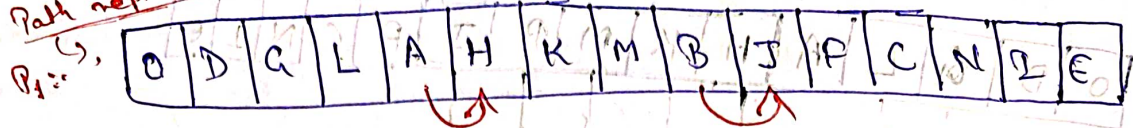
Order crossover is better than permutation crossover for permutation A because of order of elements.

D	I	H	I	M	F	E	K	L	C	O	L	A	B
O	M	L	J	I	D	H	O	F	E	C	B	A	

Heuristic for PSP not to be used for permutation A

TSP :- Adjacency Representation

Path representation

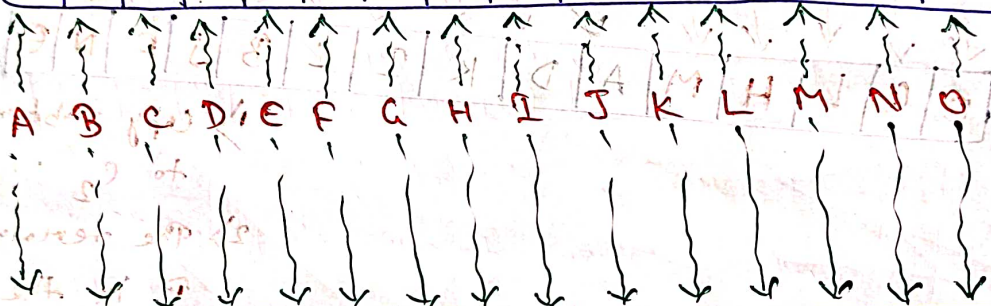
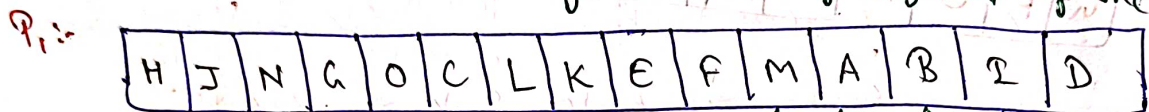


Adjacency Representation

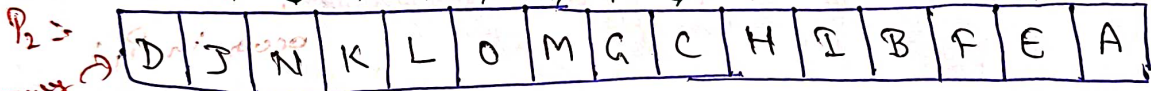
The cities are arranged based on where they come from with the index.

EX:- A → H, B → J

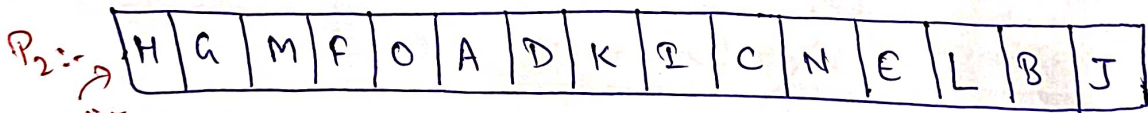
Advantage :- You can easily access any segment of the tour by index.



Cities Index

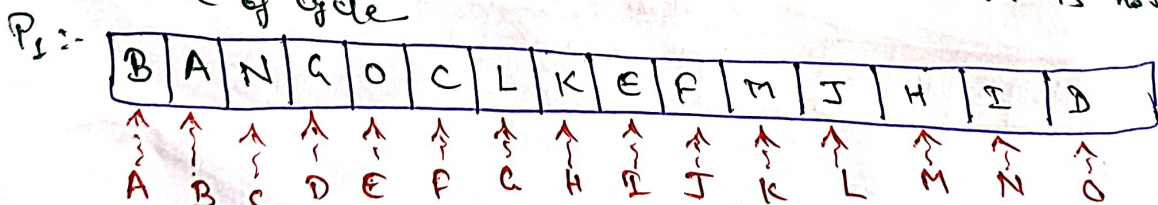


Adjacency representation



Path representation

Note :- Suppose example of Adjacency Representation that is not valid because of cycle



A → B → A

cycle :- Not valid permutation of tour for TSP as candidate solution.

Adjacency Representation: Crossover, Operations

1) Alternating Edges Crossover

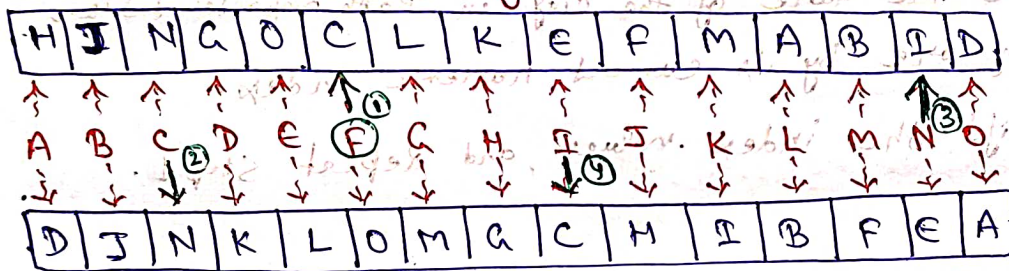
- construct a child as follows
- From a given city A choose the next city B from P_1
- from the city B choose the next city from P_2
- Repeat the processing.

2) Heuristic Crossover

- for each city choose from that parent (P_1 or P_2) which is closer / less cost.

Note:-

Alternating Edges - Careful.



Ex: let's say we start with city F

- from P_1 $F \rightarrow C$
- from P_2 $C \rightarrow N$
- from P_1 $N \rightarrow I$
- from P_2 $I \rightarrow C$ cycle

Solution:- Choose random next city.