

# Analysis of Algorithms | Set 4 (Analysis of Loops) - GeeksforGeeks

We have discussed [Asymptotic Analysis](#), [Worst, Average and Best Cases](#) and [Asymptotic Notations](#) in previous posts. In this post, analysis of iterative programs with simple examples is discussed.

**1)  $O(1)$ :** Time complexity of a function (or set of statements) is considered as  $O(1)$  if it doesn't contain loop, recursion and call to any other non-constant time function.

```
// set of non-recursive and non-loop statements
```

For example [swap\(\) function](#) has  $O(1)$  time complexity.

A loop or recursion that runs a constant number of times is also considered as  $O(1)$ . For example the following loop is  $O(1)$ .

```
// Here c is a constant
for (int i = 1; i <= c; i++) {
    // some  $O(1)$  expressions
}
```

**2)  $O(n)$ :** Time Complexity of a loop is considered as  $O(n)$  if the loop variables is incremented / decremented by a constant amount. For example following functions have  $O(n)$  time complexity.

```
// Here c is a positive integer constant
for (int i = 1; i <= n; i += c) {
    // some  $O(1)$  expressions
}

for (int i = n; i > 0; i -= c) {
    // some  $O(1)$  expressions
}
```

**3)  $O(n^c)$ :** Time complexity of nested loops is equal to the number of times the innermost statement is executed. For example the following sample loops have  $O(n^2)$  time complexity

```
for (int i = 1; i <= n; i += c) {
    for (int j = 1; j <= n; j += c) {
        // some  $O(1)$  expressions
    }
}
```

```

    }
}

for (int i = n; i > 0; i += c) {
    for (int j = i+1; j <=n; j += c) {
        // some O(1) expressions
    }
}

```

For example [Selection sort](#) and [Insertion Sort](#) have  $O(n^2)$  time complexity.

**4)  $O(\text{Log}n)$**  Time Complexity of a loop is considered as  $O(\text{Log}n)$  if the loop variables is divided / multiplied by a constant amount.

```

for (int i = 1; i <=n; i *= c) {
    // some O(1) expressions
}
for (int i = n; i > 0; i /= c) {
    // some O(1) expressions
}

```

For example [Binary Search\(refer iterative implementation\)](#) has  $O(\text{Log}n)$  time complexity.

**5)  $O(\text{LogLog}n)$**  Time Complexity of a loop is considered as  $O(\text{LogLog}n)$  if the loop variables is reduced / increased exponentially by a constant amount.

```

// Here c is a constant greater than 1
for (int i = 2; i <=n; i = pow(i, c)) {
    // some O(1) expressions
}
//Here fun is sqrt or cuberoot or any other constant root
for (int i = n; i > 0; i = fun(i)) {
    // some O(1) expressions
}

```

See [this](#) for more explanation.

### How to combine time complexities of consecutive loops?

When there are consecutive loops, we calculate time complexity as sum of time complexities of individual loops.

```

for (int i = 1; i <=m; i += c) {

```

```
// some O(1) expressions
}
for (int i = 1; i <=n; i += c) {
    // some O(1) expressions
}
Time complexity of above code is  $O(m) + O(n)$  which is  $O(m+n)$ 
If  $m == n$ , the time complexity becomes  $O(2n)$  which is  $O(n)$ .
```

### How to calculate time complexity when there are many if, else statements inside loops?

As discussed [here](#), worst case time complexity is the most useful among best, average and worst. Therefore we need to consider worst case. We evaluate the situation when values in if-else conditions cause maximum number of statements to be executed.

For example consider the [linear search function](#) where we consider the case when element is present at the end or not present at all.

When the code is too complex to consider all if-else cases, we can get an upper bound by ignoring if else and other complex control statements.

### How to calculate time complexity of recursive functions?

Time complexity of a recursive function can be written as a mathematical recurrence relation. To calculate time complexity, we must know how to solve recurrences. We will soon be discussing recurrence solving techniques as a separate post.

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.