

Rated voltage	9.0V (DC)
Temperature range	-20°C~+60°C
Humidity range	0%-90%
No-load current	≤ 200 mA
No-load speed	185±10% rpm
Rated load	0.9 Kgf.cm
Rated current	≤ 550mA
Rated speed	135±10% rpm
Starting torque	4.5kgf.cm
Locked-rotor current	≥ 2.0 A
Parts List	1 x Me Encoder Motor Driver 2 x Optical Encoder Motor-25 9V/185RPM 2 x Encoder Motor Wire
Package Dimension	200 x 140 x 30mm (7.9 x 5.5 x 1.2inch)
Net Weight	222g (7.83oz)
Gross Weight	228g (8.04oz)

Figure 1: Enter Caption

I am doing the time system response to see if my model actually represents the system
here is the model

$$I_{\theta}\ddot{\theta} + b\dot{\theta} - \frac{hmg}{2} \sin \theta = k_{gr}k_t \left(\frac{V - k_e\omega}{R} \right) \tag{1}$$

$$I_{\theta} = \left(\frac{m}{12}(h^2 + w^2) \right) \tag{2}$$

$$I_{\phi} = \left(\frac{m}{12}(l^2 + w^2) \right) \tag{3}$$

$$q = \begin{pmatrix} \theta \\ \psi \end{pmatrix} \quad (4)$$

$$M = \begin{pmatrix} I & 0 \\ 0 & I \end{pmatrix} \quad (5)$$

$$B = \begin{pmatrix} b & 0 \\ 0 & b \end{pmatrix} \quad (6)$$

$$G = \begin{pmatrix} dm g \sin \theta + \frac{k_t k_{gr}}{R} \omega \\ \frac{k_t k_{gr}}{R} \omega \end{pmatrix} \quad (7)$$

$$F = \begin{pmatrix} k_{gr} \left(\frac{k_t}{R} (u_1 + u_2) \right) \\ k_{gr} \left(\frac{k_t}{R} (u_1 - u_2) \right) \end{pmatrix} \quad (8)$$

$$h = .11m \quad (9)$$

$$w = .135m \quad (10)$$

$$m = 0.725748kg \quad (11)$$

$$g = 9.81 \frac{N}{s^2} \quad (12)$$

$$b = 0.0493 \frac{Nm \cdot s}{rad} \quad (13)$$

$$I_\theta = \frac{m(h^2 + w^2)}{36} kg \cdot m^2 \quad (14)$$

$$I_\psi = \frac{m(w^2 + h^2)}{18} kg \cdot m^2 \quad (15)$$

$$m_w = .06m \quad (16)$$

$$r = .031m \quad (17)$$

$$R = 4.5\Omega \quad (18)$$

$$I_w = \frac{m_w r^2}{2} \quad (19)$$

motor consts now:

$$k_t = \frac{\tau_{rated}}{I_{rated}} = \frac{0.08825985Nm}{.55A} = .1604 \frac{N \cdot m}{A} \quad (20)$$

$$k_e = k_t = .1604 \frac{V \cdot s}{rad} \quad (21)$$

$$R = \frac{k_t(V_{rated} - k_e \omega_{rated})}{\tau_{rated}} = \frac{.1604 \frac{Nm}{A} (9.0V - .1604 \frac{V \cdot s}{rad} \cdot 14.137166924999999 \frac{rad}{s})}{0.08825985Nm} = 12.23519763\Omega \quad (22)$$

$$k_{gr} = 1/46 \quad (23)$$

Ok, my state variables and control inputs are

$$X = \begin{pmatrix} \theta \\ \dot{\theta} \\ \omega_1 \\ \omega_2 \end{pmatrix} \quad (24)$$

$$U = \begin{pmatrix} V_1 \\ V_2 \end{pmatrix} \quad (25)$$

so my model for pitch is

$$\dot{X} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ -\frac{hmg}{2} & -\frac{b}{I_\theta} & -\frac{k_{gr}k_t k_e}{2RI_\theta} & -\frac{k_{gr}k_t k_e}{2RI_\theta} \\ 0 & 0 & -\frac{k_{gr}k_t k_e}{2RI_\theta} & 0 \\ 0 & 0 & 0 & -\frac{k_{gr}k_t k_e}{2RI_\theta} \end{pmatrix} X + \begin{pmatrix} 0 & 0 \\ \frac{k_{gr}k_t}{2RI_\theta} & \frac{k_{gr}k_t}{2RI_\theta} \\ \frac{k_{gr}k_t}{2RI_w} & 0 \\ 0 & \frac{k_{gr}k_t}{2RI_w} \end{pmatrix} U \quad (26)$$

$$Y = \begin{pmatrix} 1 & 0 & 0 & 0 \end{pmatrix} X \quad (27)$$

so, here's my state variables for yaw, control inputs stay the same

$$X_\psi = \begin{pmatrix} \psi \\ \dot{\psi} \\ \omega_1 \\ \omega_2 \end{pmatrix} \quad (28)$$

$$\dot{X}_\psi = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -\frac{b_\psi}{I_\psi} & -\frac{k_{gr}k_t}{2RI_\theta} & \frac{k_{gr}k_t}{2RI_\theta} \\ 0 & 0 & -\frac{k_{gr}k_t}{2RI_\theta} & 0 \\ 0 & 0 & 0 & \frac{k_{gr}k_t}{2RI_\theta} \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ -\frac{k_{gr}k_t}{2RI_\theta} & \frac{k_{gr}k_t}{2RI_\theta} \\ -\frac{k_{gr}k_t}{2RI_\theta} & 0 \\ 0 & \frac{k_{gr}k_t}{2RI_\theta} \end{pmatrix} U \quad (29)$$

$$Y = \begin{pmatrix} 1 & 0 & 0 & 0 \end{pmatrix} X \quad (30)$$

Where $b_\psi \approx 0$