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# Non-binary codes for c-VEP-based BCI systems

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# Contents



- 1. Introduction**
  1. Binary c-VEPs: pros and cons
  2. Addressing user convenience
    1. Higher stimulation rates
    2. High-frequency codes
    3. Non-binary codes
- 2. Maximal-length sequences**
  1. What are m-sequences?
  2. Generation of  $p$ -ary m-sequences
  3. Correlation local maxima
- 3. Evidence of benefits for non-binary codes**
- 4. Open-source software for non-binary codes**



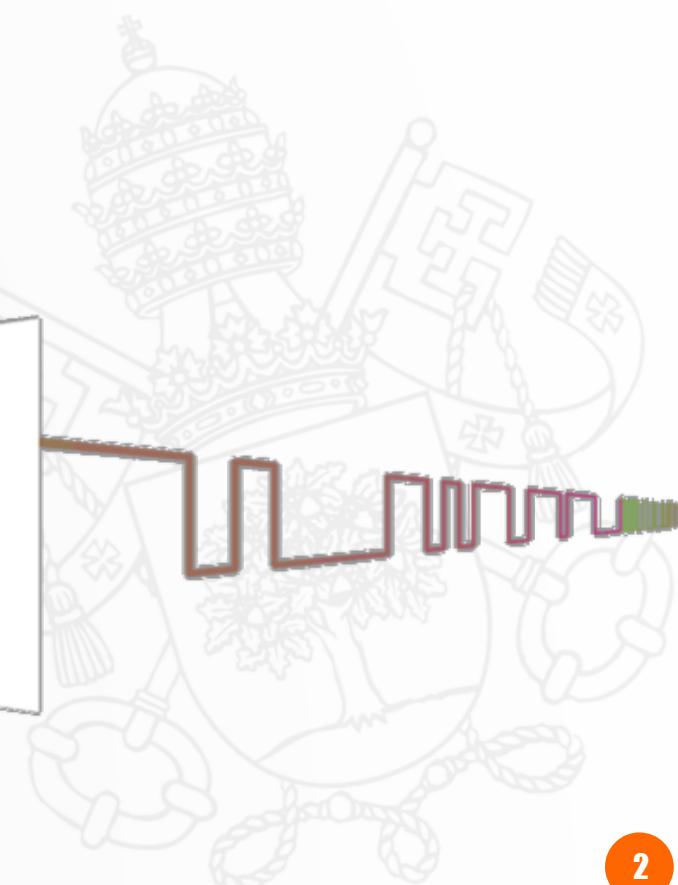
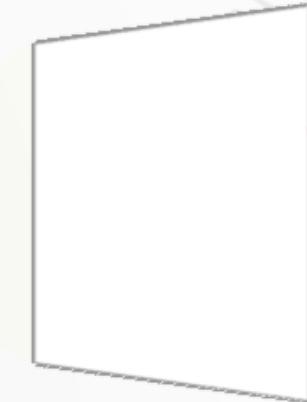
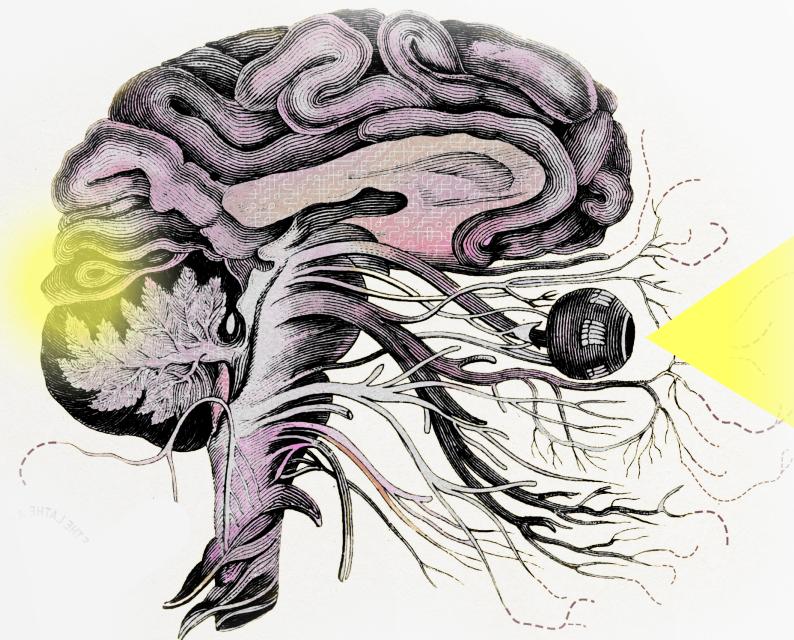
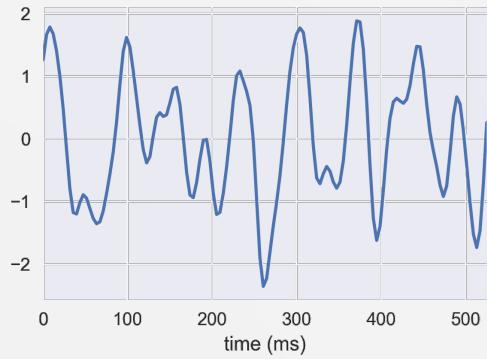


# Introduction



- **Code-modulated visual evoked potentials (c-VEP)**

- Visual evoked potentials in response to pseudorandom codes
- Binary codes are usually encoded with black & white flashes
  - Maximal amplitude depth → stronger response at occipital cortex



# Introduction



Cons

Pros



Eyestrain  
for some  
users

High  
accuracy  
(>90%)

Brief  
calibration  
(~30s)

Visual fatigue may be caused by  
high-contrast stimuli!

0



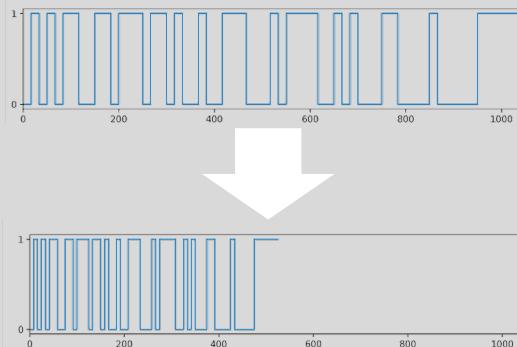
# Introduction



- Addressing user convenience in c-VEP-based BCIs

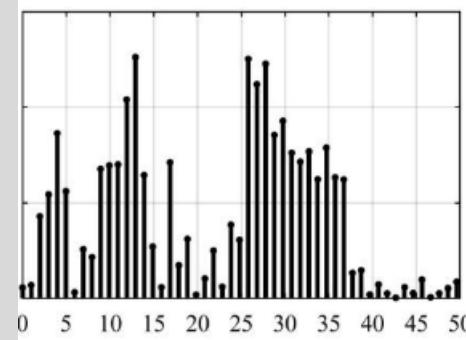
## Higher stimulation rates

1



## High-frequency codes

2



## Non-binary codes

3





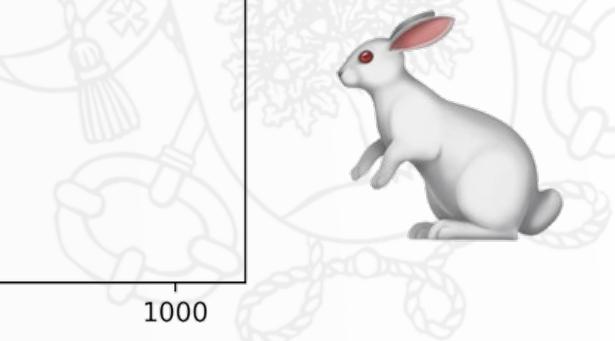
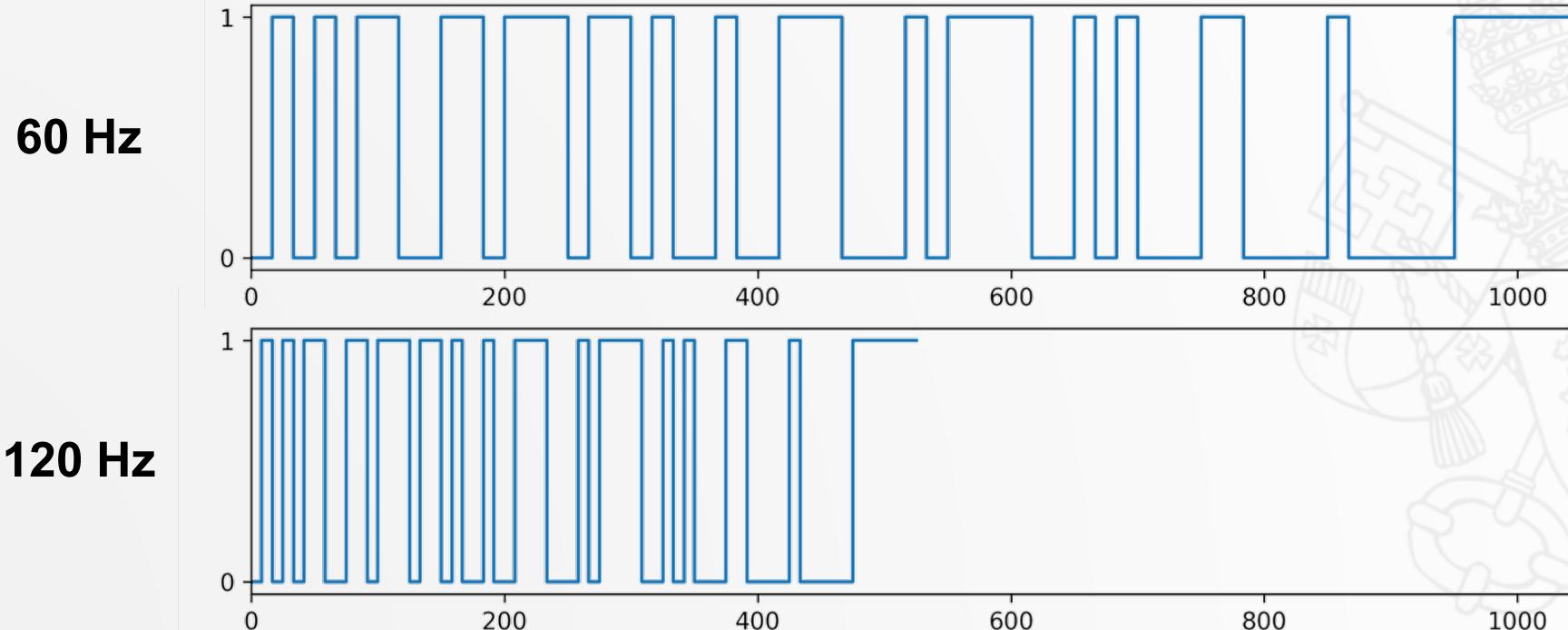
# Introduction



- Addressing user convenience in c-VEP-based BCIs

1. Higher stimulation rates

- Many studies claimed that 120 Hz stimulation is less fatiguing than 60 Hz → [Martínez-Cagigal et al., 2023](#)
- Although decreases in performance reported for >120 Hz rates (e.g. 240 Hz) → [Gembler et al., 2018](#)



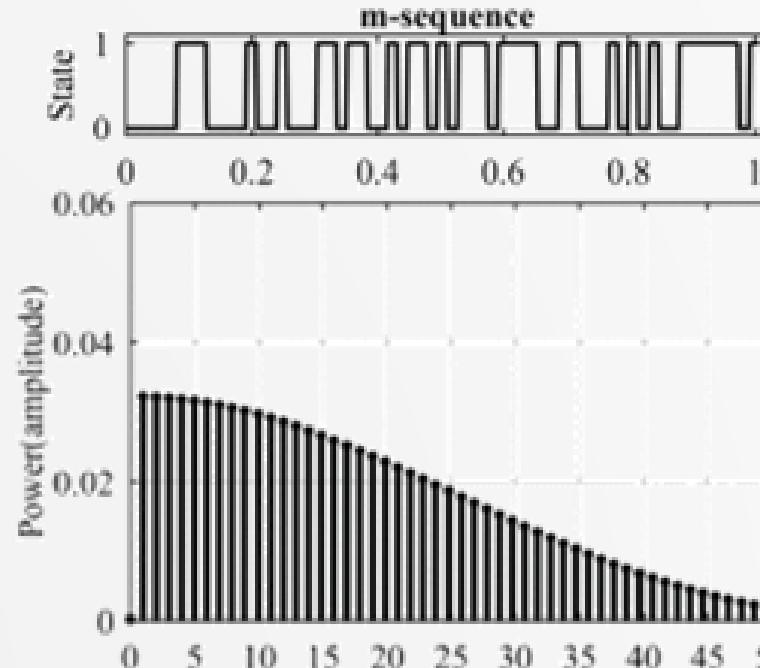


# Introduction

- Addressing user convenience in c-VEP-based BCIs

## 2. High-frequency codes

- Chaotic codes → [Shirzhiyan et al., 2019](#)
- Optimum sequences → [Behboodi et al., 2020](#)
- Superposition optimized pulses → [Yasinzai & Ider, 2020](#)



RESEARCH ARTICLE  
Introducing chaotic codes for the modulation  
of visual evoked potentials in brain-computer interfaces

2762

IEEE TRANSACTIONS ON NEURAL SYSTEMS AND REHABILITATION ENGINEERING, VOL. 28, NO. 12, DECEMBER 2020

EMB



## Optimization of Visual Stimulus Sequence in a Brain

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Mohamm



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## PAPER

New approach for designing cVEP BCI stimuli based on superposition of edge responses

Muhammad Nabi Yasinzai and Yusuf Ziya Ider

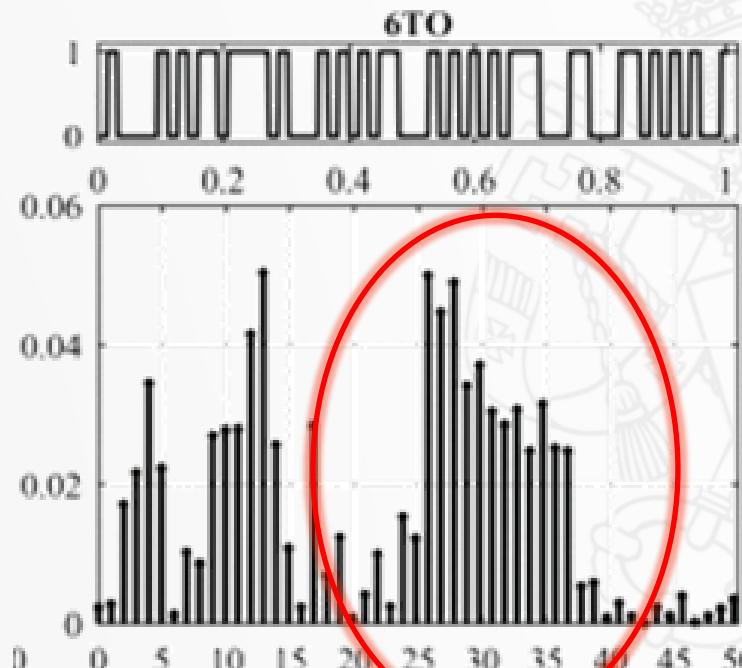
Department of Electrical and Electronics Engineering, Bilkent University, Ankara, Turkey

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Keywords: brain computer interface, coded visually evoked response, EEG, stimulus design, BCI speller

Supplementary material for this article is available online





# Introduction

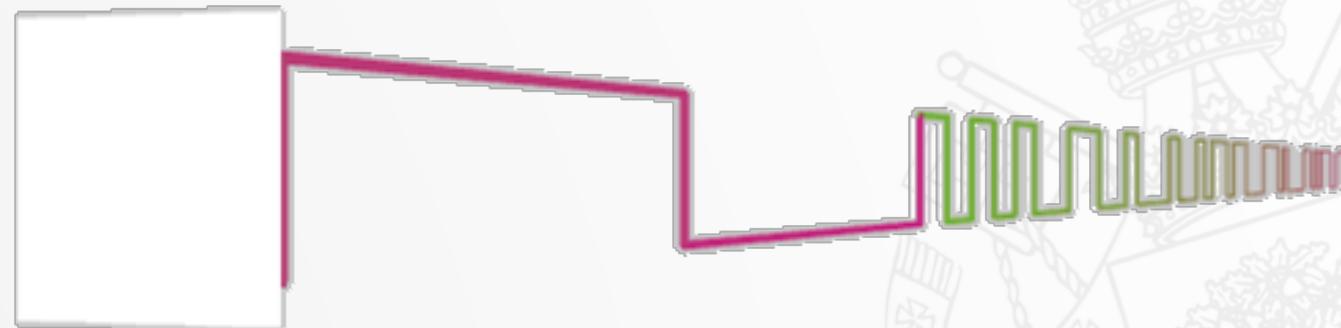


- **Addressing user convenience in c-VEP-based BCIs**

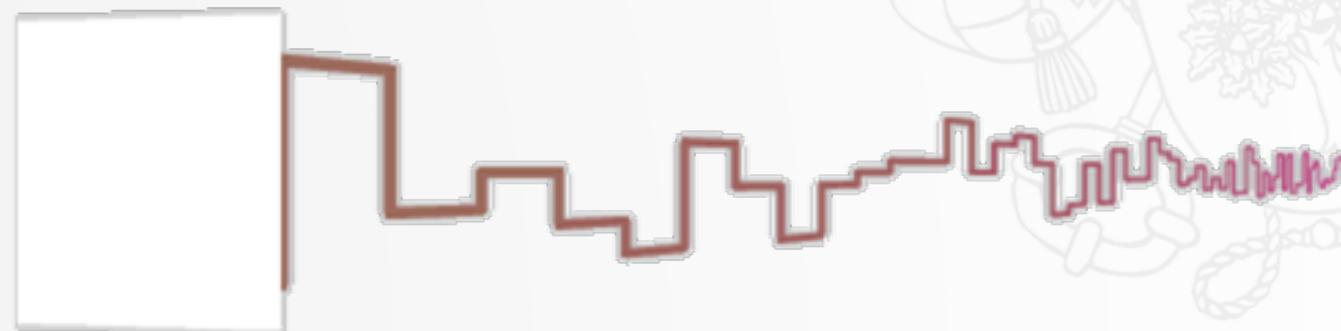
- 3. Non-binary codes

- I.e., codes with more levels than just 0 and 1
    - We can encode them with different shades of gray and colors to reduce amplitude depth
    - Demonstrated to be more comfortable than binary codes → [Martínez-Cagigal et al., 2023](#)

**Binary  
(base 2)**



**11-ary  
(base 11)**



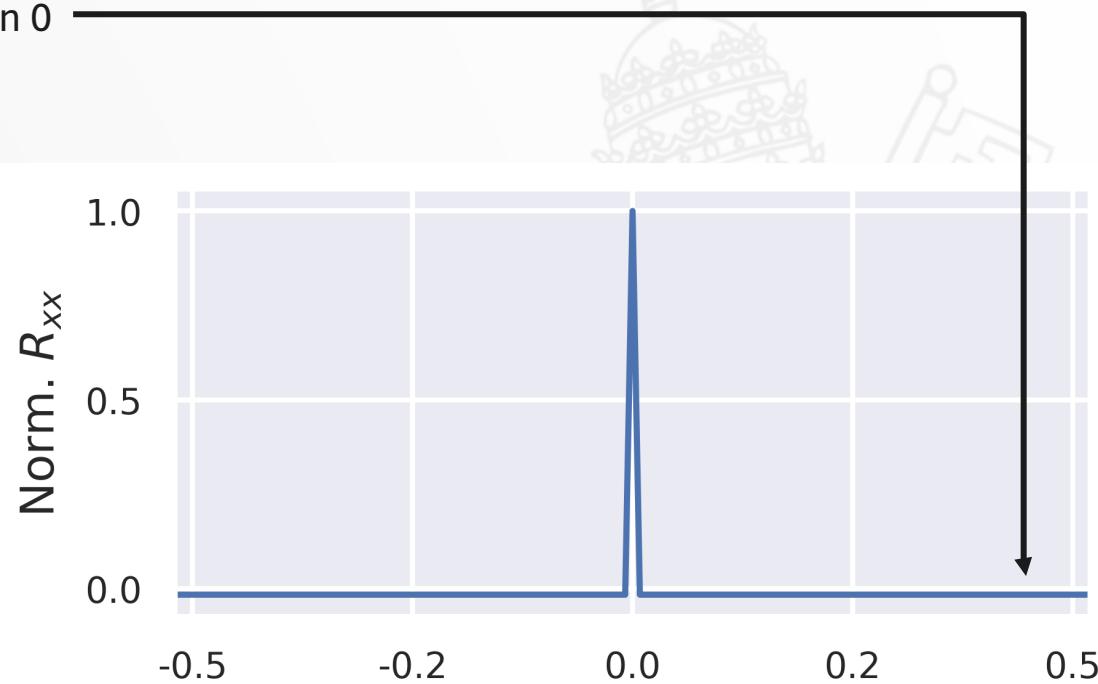
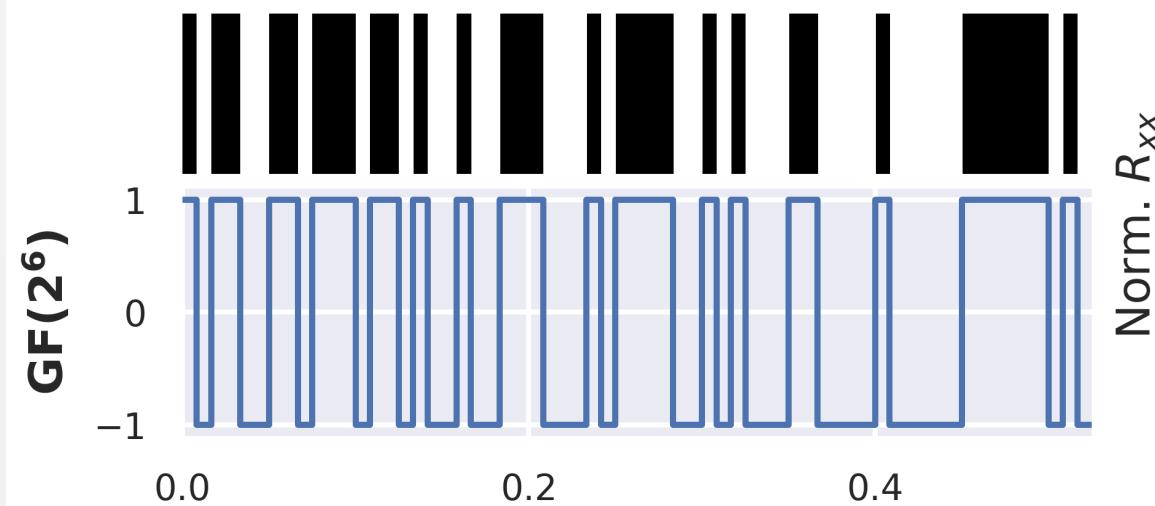


# Maximal-length Sequences



- What are maximal-length sequences (m-sequences)?

- Pseudorandom periodic time series
- With optimal autocorrelation profiles
  - For binary codes,  $-1/N$  for any shift different than 0



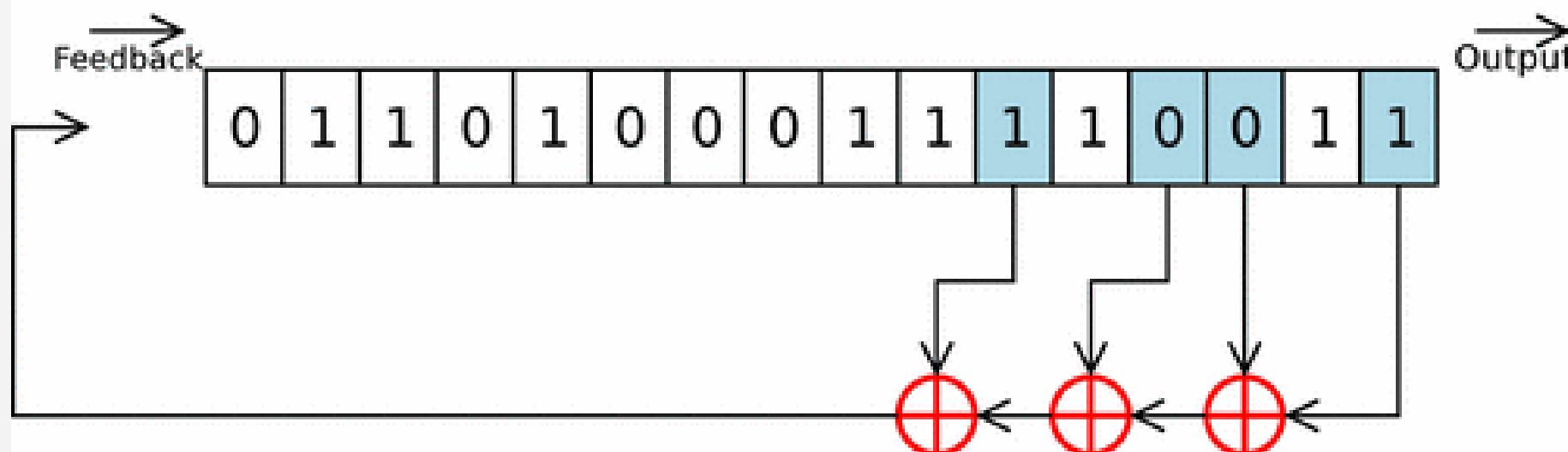


# Maximal-length Sequences



- **Linear Feedback Shift Registers (LFSR)**

- Shift registers that compute new values using a linear function of the immediate previous state
- The code is generated by appending the output to the initial position of the state





# Maximal-Length Sequences



- Generation of  $p$ -ary m-sequences

- The length of the output code depends on:

$$L = p^r - 1$$

Length      Base      Polynomial order

- Notation:

$\text{GF}(p^r)$

For  $\text{GF}(2^6)$ ,  $L = 63$  bits

- Requirement: using primitive polynomials over Galois Field  $\text{GF}(p^r)$ 
    1. Only bases where  $p$  is prime are allowed (e.g., 2, 3, 5, 7, 11...)
    2. The codes are fixed in length (i.e.,  $L = p^r - 1$ )



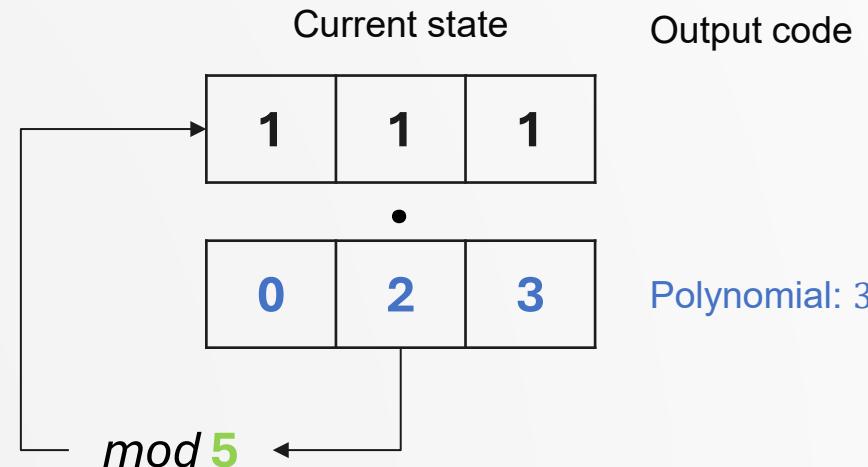
# Maximal-Length Sequences



- Generation of  $p$ -ary m-sequences

- Each bit is calculated by:
  1. Applying matrix product between the current state and the polynomial
  2. Then applying the modulo  $p$  operation
- Example for base 5  $\rightarrow \text{GF}(5^3)$

Base	Order	Length	Polynomial
5	3	124 bits	$3x^3 + 2x^2 + 1$





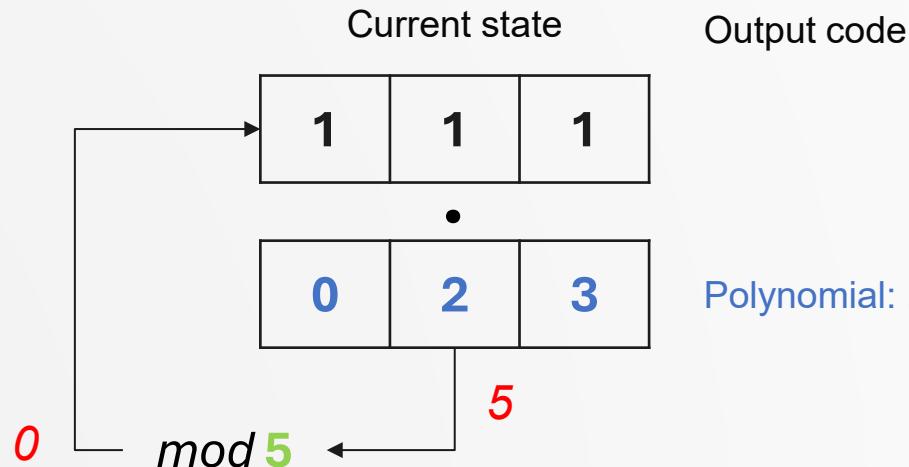
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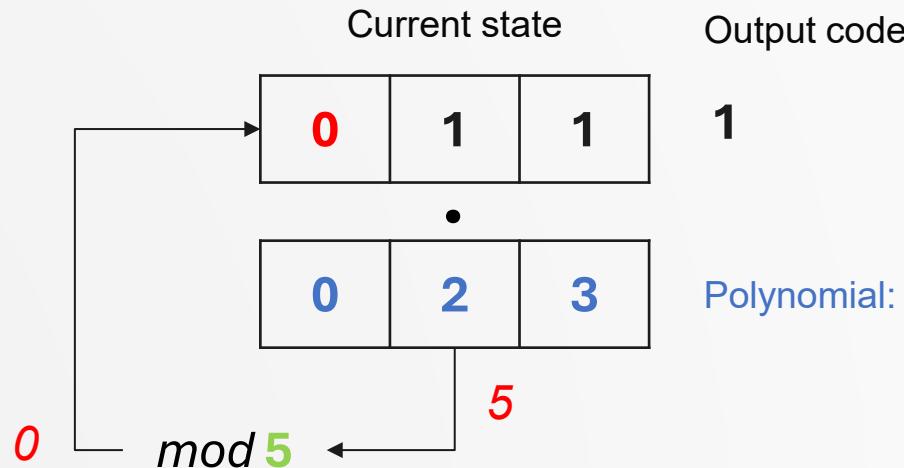
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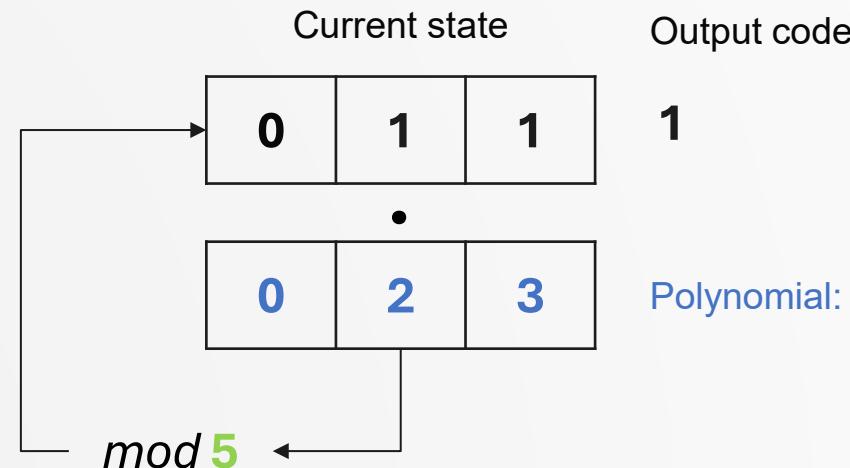
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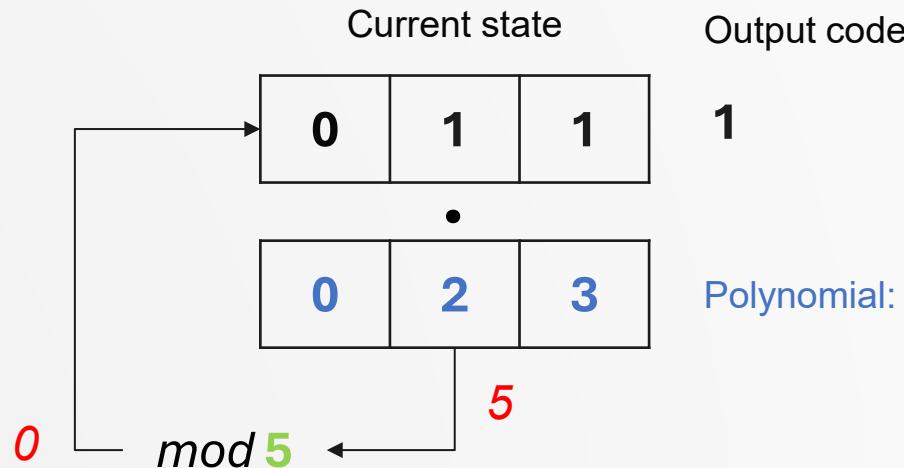
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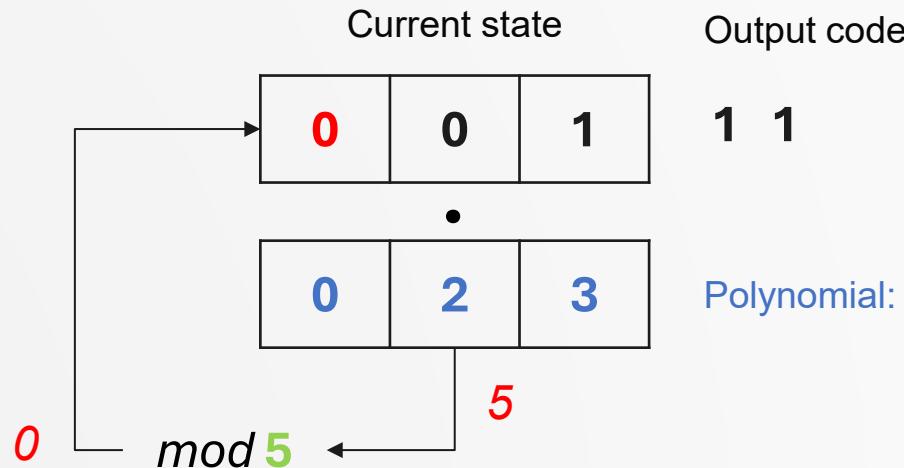
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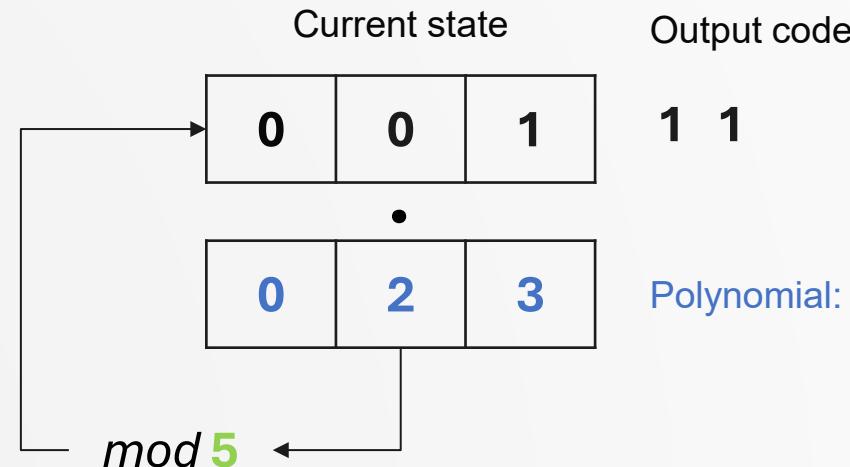
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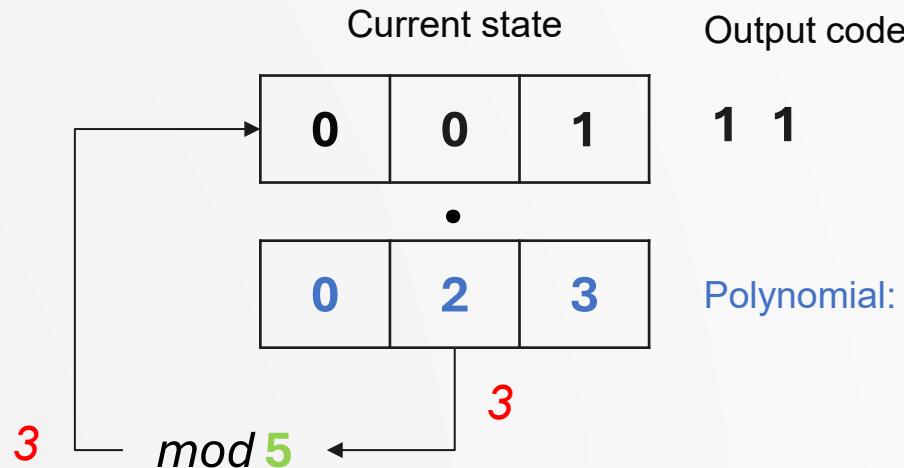
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Output code

1 1

Polynomial:  $3x^3 + 2x^2 + 0x + 1$



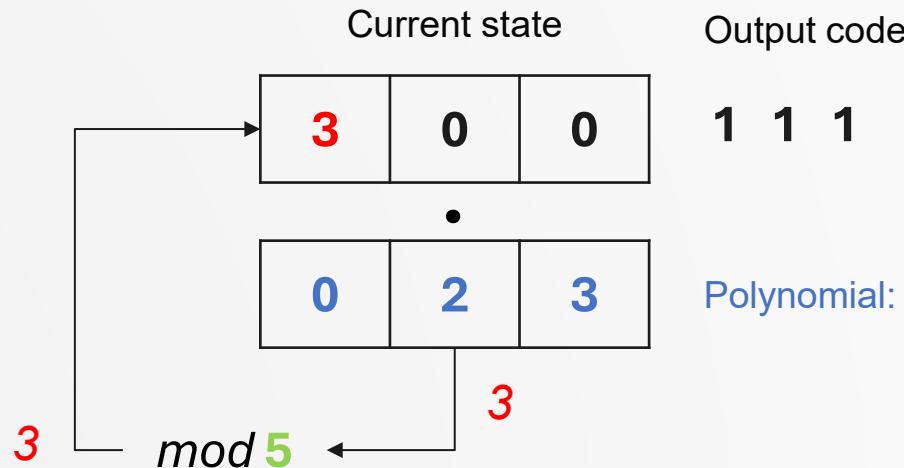
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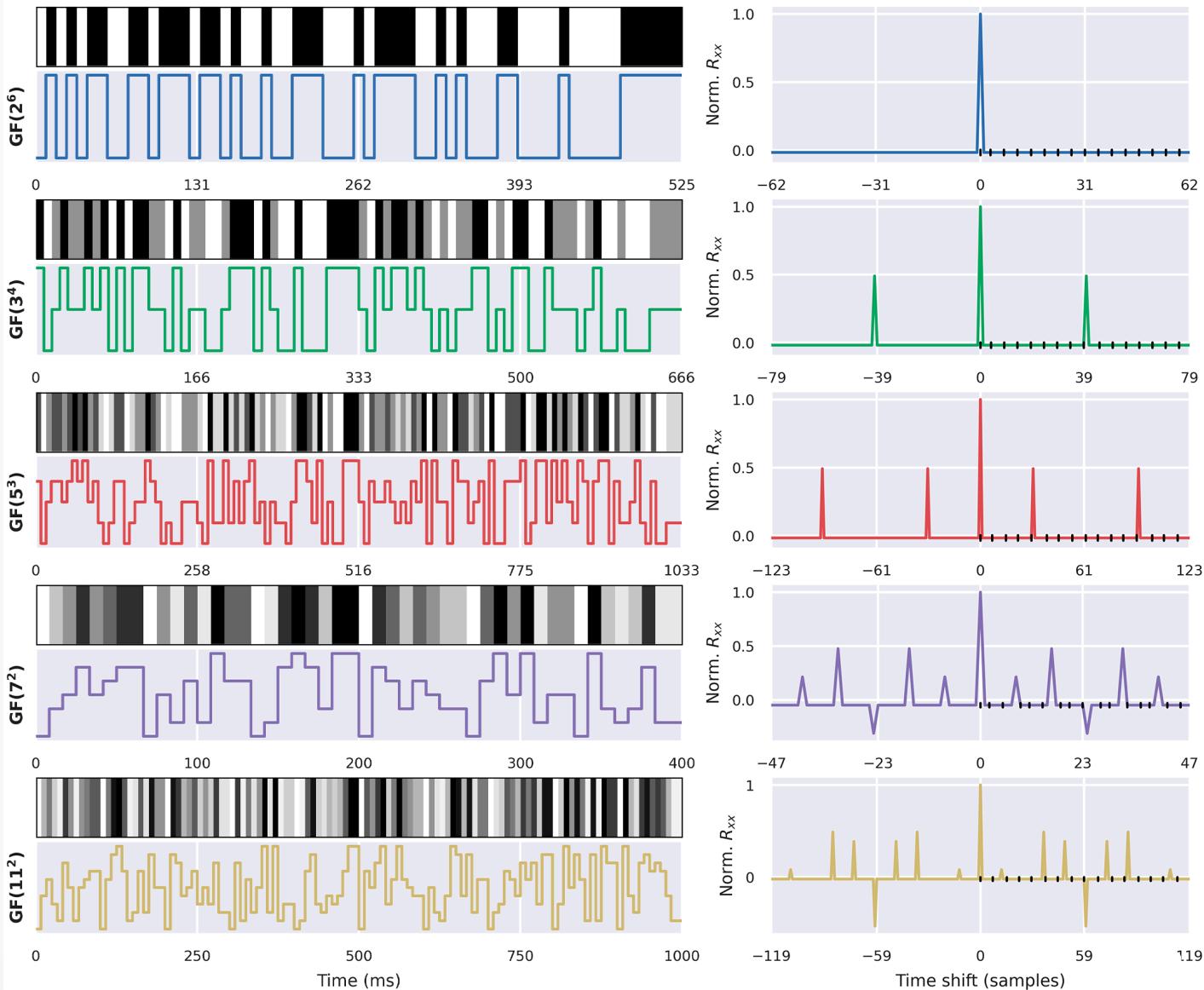


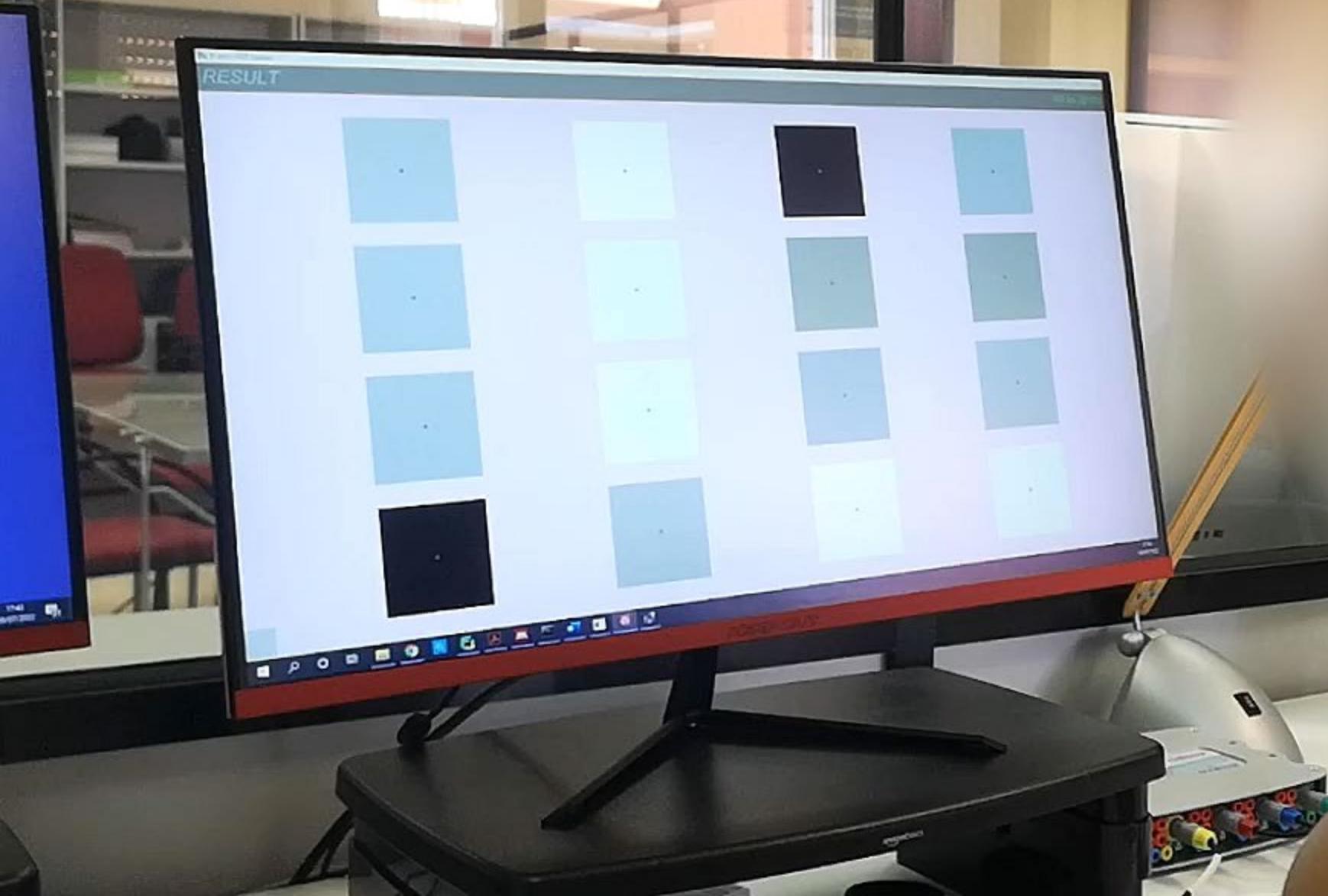
# Correlation local maxima



Generation details of the  $p$ -ary m-sequences.

	Base	Order	Length (bits)	Polynomial	Duration (s/cycle)	
					120 Hz	60 Hz
GF(2 <sup>6</sup> )	2	6	63	$x^6 + x^5 + 1$	0.525	1.050
GF(3 <sup>4</sup> )	3	4	80	$x^4 + 2x^3 + 1$	0.667	1.333
GF(5 <sup>3</sup> )	5	3	124	$3x^3 + 2x^2 + 1$	1.033	2.067
GF(7 <sup>2</sup> )	7	2	48	$4x^2 + 1$	0.408	0.800
GF(11 <sup>2</sup> )	11	2	120	$3x^2 + x + 1$	1.000	2.000







# Evidence of benefits of non-binary codes



Expert Systems With Applications 232 (2023) 120815

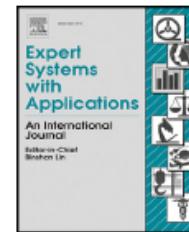


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Non-binary m-sequences for more comfortable brain–computer interfaces based on c-VEPs

Víctor Martínez-Cagigal <sup>a,b,\*</sup>, Eduardo Santamaría-Vázquez <sup>a,b</sup>, Sergio Pérez-Velasco <sup>a,b</sup>,  
Diego Marcos-Martínez <sup>a,b</sup>, Selene Moreno-Calderón <sup>a</sup>, Roberto Hornero <sup>a,b</sup>



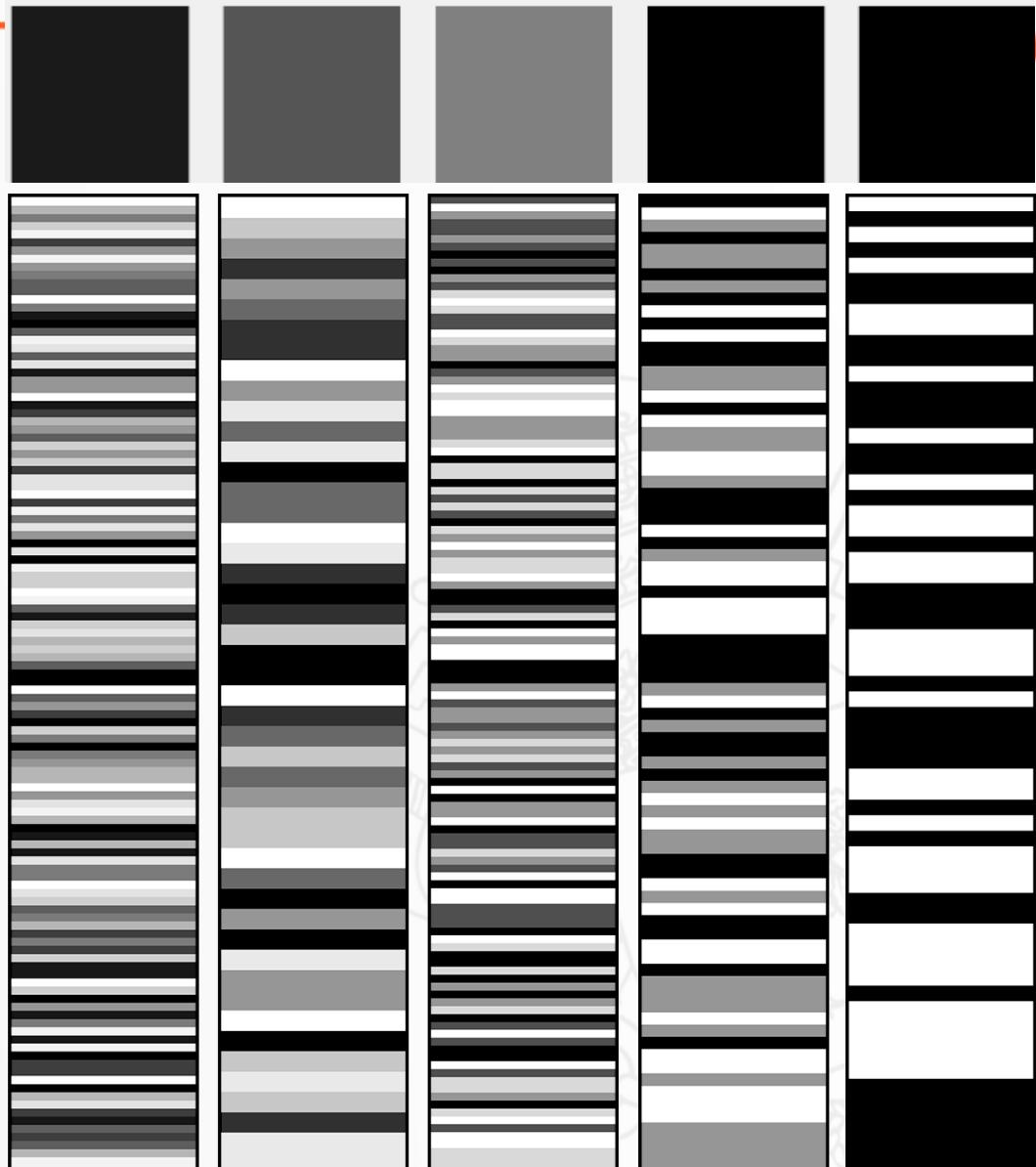


# Evidence of benefits of non-binary codes



- Our study

- Five different  $p$ -ary m-sequences (bases 2, 3, 5, 7 and 11)
- Reference signal processing ( [Martínez-Cagigal et al., 2021](#))
- Equipment
  - g.USBamp with 16 active channels
  - MEDUSA© software ([www.medusabci.com](http://www.medusabci.com))
- Experimental protocol
  - 15 healthy subjects ( $28.80 \pm 5.02$  years)
  - Calibration: 300 cycles for each sequence
  - Online: 32 trials (10 cycles/trial)
  - Command matrix of  $4 \times 4$  dimensions





# Evidence of benefits of non-binary codes



## ▪ Performance analysis

- Users were able to reach more than 98% grand-averaged accuracy with 10 cycles using all the proposed  $p$ -ary m-sequences

Grand-averaged online results across users.

	No. cycles	1	2	3	4	5	6	7	8	9	10	Mean ± STD
GF(2 <sup>6</sup> )	Accuracy (%)	65.43	90.43	96.68	98.05	<b>99.41</b>	<b>99.41</b>	<b>99.61</b>	<b>99.61</b>	<b>99.41</b>	<b>99.61</b>	$94.77 \pm 10.14$
	ITR (bpm)	208.06	188.03	141.04	108.91	90.14	75.11	64.65	56.57	50.08	45.25	$102.78 \pm 55.19$
	Duration (s)	0.53	1.05	1.58	2.10	2.62	3.15	3.68	4.20	4.73	5.25	$2.89 \pm 1.51$
GF(3 <sup>4</sup> )	Accuracy (%)	75.78	92.77	97.27	97.66	98.44	98.83	99.02	99.02	99.02	99.22	$95.70 \pm 6.89$
	ITR (bpm)	216.59	154.70	113.27	85.68	69.67	58.54	50.31	44.02	39.13	35.36	$86.73 \pm 55.97$
	Duration (s)	0.67	1.33	2.00	2.67	3.33	4.00	4.67	5.33	6.00	6.67	$3.67 \pm 1.91$
GF(5 <sup>3</sup> )	Accuracy (%)	83.20	94.14	<b>98.05</b>	<b>98.83</b>	99.02	99.22	99.41	99.41	99.22	99.22	$96.97 \pm 4.83$
	ITR (bpm)	163.72	103.05	74.01	56.54	45.47	38.02	32.76	28.66	25.39	22.85	$59.05 \pm 42.20$
	Duration (s)	1.03	2.07	3.10	4.13	5.17	6.20	7.23	8.27	9.30	10.33	$5.68 \pm 2.97$
GF(7 <sup>2</sup> )	Accuracy (%)	49.80	82.23	93.36	95.90	97.27	97.46	98.05	97.66	98.24	98.05	$90.80 \pm 14.42$
	ITR (bpm)	168.14	205.30	174.38	137.45	113.43	95.18	82.46	71.65	64.31	57.72	$117.00 \pm 49.15$
	Duration (s)	0.40	0.80	1.20	1.60	2.00	2.40	2.80	3.20	3.60	4.00	$2.20 \pm 1.15$
GF(11 <sup>2</sup> )	Accuracy (%)	<b>86.72</b>	<b>97.46</b>	<b>98.05</b>	98.63	98.83	98.63	98.63	98.63	98.63	98.44	<b><math>97.27 \pm 3.54</math></b>
	ITR (bpm)	179.64	113.79	76.79	58.36	46.93	38.99	33.42	29.24	25.99	23.33	$62.65 \pm 47.10$
	Duration (s)	1.00	2.00	3.00	4.00	5.00	6.00	7.00	8.00	9.00	10.00	$5.50 \pm 2.87$

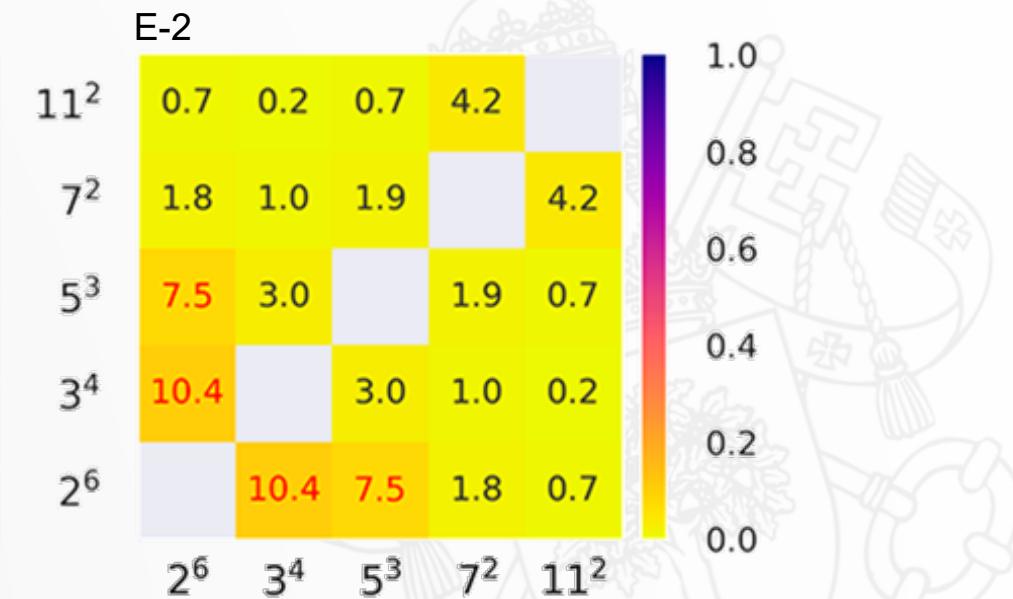
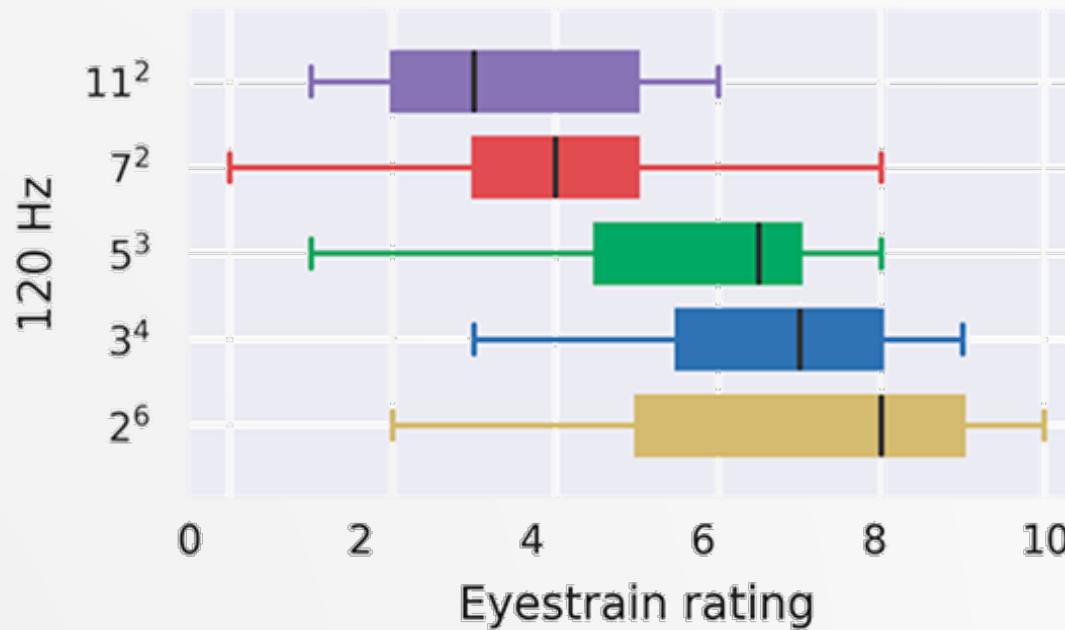


# Evidence of benefits of non-binary codes



## ▪ Eyestrain analysis

- The higher the base (i.e., number of levels), the less eyestrain users perceive
  - E.g., GF( $7^2$ ) and GF( $11^2$ ) are significantly less fatiguing than binary GF( $2^6$ )



Black: significant differences ( $p\text{-value} < 0.05$ )  
Red: no differences ( $p\text{-value} > 0.05$ )



# Open-source software for non-binary codes



[www.medusabci.com](http://www.medusabci.com)



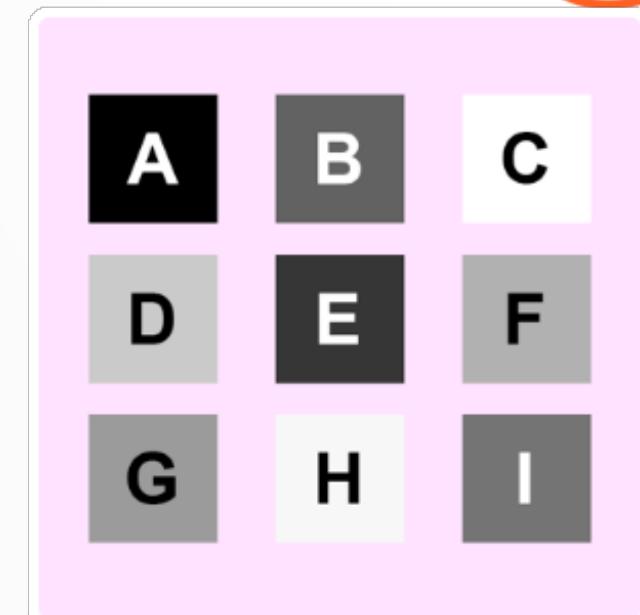
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Eduardo Santamaría-Vázquez, Ph.D.; Víctor Martínez-Cagigal, Ph.D.; Diego Marcos-Martínez, M.Sc.; Víctor Rodríguez-González, M.Sc.; Sergio Pérez-Velasco, M.Sc.; Selene Moreno-Calderón, M.Sc.; Roberto Hornero, Ph.D. Published in Computer Methods and Programs in Biomedicine, vol. 230, pp. 107357, 2023 (10.1016/j.cmpb.2023.107357). Powered by the Biomedical Engineering Group ([www.gib.teUva.es](http://www.gib.teUva.es)) of the University of Valladolid.

Artwork generated with Bing AI.



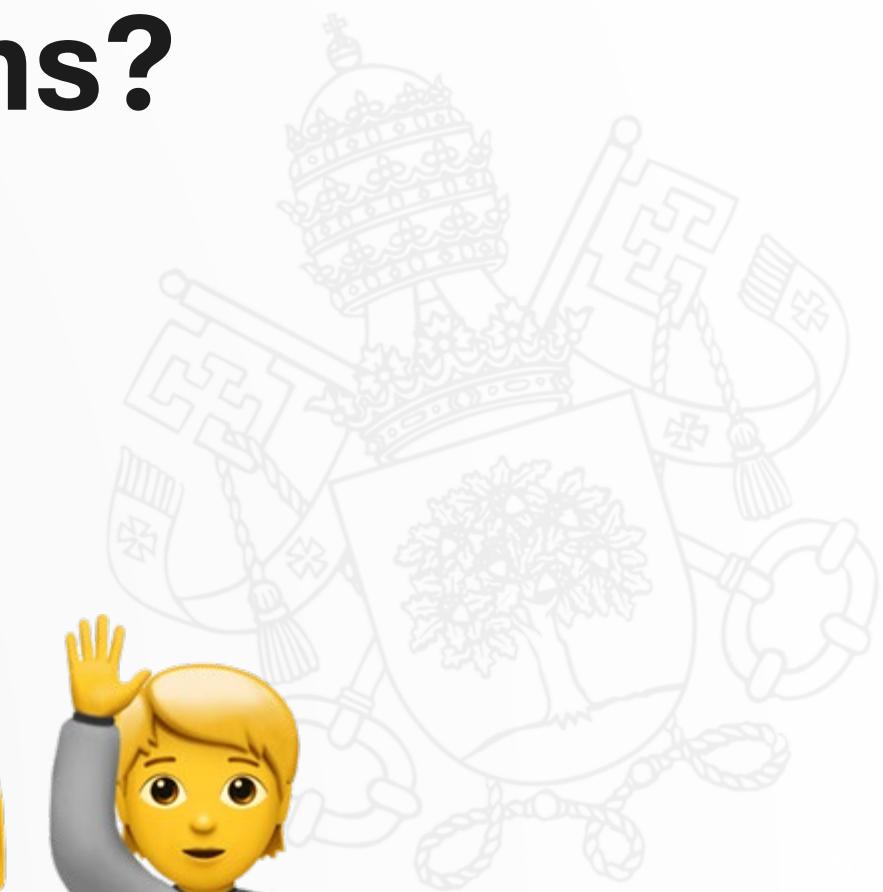
vicmarcag

P-ary c-VEP Speller

A circular-shifting c-VEP speller that supports non-binary m-sequences

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# Any questions?



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