# Regularized Multiple Linear Regression

# September 18, 2019

We have already implemented a simple linear regression model by manually implementing gradient descent. For that implementation of linear regression, refer to the notebook titled "Linear Regression with two variables and manual implementation of gradient descent 22.06.2019".

In this notebook we will solve a case study by using multiple linear regression, and regularised linear regression [Ridge and Lasso]. We will also look at hyperparameter tuning for regularised regression. Also, we will concentrate on feature engineering and data preperation.

This dataset comes from a loan aggregator who collects loan applications from different people and sends it to various financial institutions.

They have collected various information from the loan applicants and have also collected what percentage of interest the bank offered to each of them. Our task now is to predict interest rate for future customers.

The name of our output variable is "Interest.Rate" in the dataset

```
In [82]: # In the class, train_test_split and KFold methods are downloaded from
         #sklearn.cross_validationlibrary but, python packages have been updated,
         #so now the correct package is sklearn.model_selection
         import pandas as pd
         import numpy as np
         import math
         from sklearn.model_selection import train_test_split
         from sklearn.linear_model import LinearRegression, Lasso, Ridge
         from sklearn.model_selection import KFold
         %matplotlib inline
In [83]: data_file=r'C:/Users/HP/Dropbox/Edvancer/CMLEP/Data/Data/loans data.csv'
         loan_data = pd.read_csv(data_file)
In [84]: loan_data.head()
Out [84]:
                 ID Amount.Requested Amount.Funded.By.Investors Interest.Rate
         0 81174.0
                                                                         8.90%
                               20000
                                                           20000
         1 99592.0
                               19200
                                                                        12.12%
                                                           19200
         2 80059.0
                               35000
                                                           35000
                                                                        21.98%
         3 15825.0
                               10000
                                                           9975
                                                                         9.99%
         4 33182.0
                               12000
                                                           12000
                                                                        11.71%
                              Loan.Purpose Debt.To.Income.Ratio State Home.Ownership \
           Loan.Length
```

```
0
             36 months debt_consolidation
                                                           14.90%
                                                                     SC
                                                                              MORTGAGE
                                                           28.36%
                                                                     TX
         1
             36 months debt_consolidation
                                                                              MORTGAGE
         2
             60 months debt_consolidation
                                                           23.81%
                                                                     CA
                                                                              MORTGAGE
             36 months debt_consolidation
                                                           14.30%
                                                                     KS
                                                                              MORTGAGE
         3
             36 months
                                credit_card
                                                           18.78%
                                                                     NJ
                                                                                  RENT
            Monthly.Income FICO.Range Open.CREDIT.Lines Revolving.CREDIT.Balance \
         0
                   6541.67
                               735-739
                                                                             14272
                   4583.33
                               715-719
                                                      12
                                                                             11140
         1
         2
                  11500.00
                               690-694
                                                      14
                                                                             21977
         3
                   3833.33
                                                      10
                                                                              9346
                               695-699
         4
                   3195.00
                               695-699
                                                                             14469
                                                      11
            Inquiries.in.the.Last.6.Months Employment.Length
         0
                                        2.0
                                                      < 1 year
         1
                                        1.0
                                                      2 years
         2
                                        1.0
                                                      2 years
         3
                                        0.0
                                                      5 years
         4
                                        0.0
                                                      9 years
In [85]: loan_data.dtypes
Out[85]: ID
                                            float64
         Amount.Requested
                                             object
         Amount.Funded.By.Investors
                                             object
         Interest.Rate
                                             object
         Loan.Length
                                             object
         Loan.Purpose
                                             object
         Debt.To.Income.Ratio
                                             object
         State
                                             object
         Home.Ownership
                                             object
         Monthly.Income
                                            float64
         FICO.Range
                                             object
         Open.CREDIT.Lines
                                             object
         Revolving.CREDIT.Balance
                                             object
         Inquiries.in.the.Last.6.Months
                                            float64
```

Variables Interest.Rate and Debt.To.Income.Ratio contains "%" sign in their values and because of which they are a "character" column and not a "numeric" column.

In [86]: col\_with\_percentage=['Interest.Rate','Debt.To.Income.Ratio']

Therefore those "%" signs should be removed first.

Employment.Length

dtype: object

```
#first we convert the entire column into string so we can easily remove % sign using
```

#string operation then we replace % with '' in each string using list comprehension

object

```
# and replace the column with this list
         for col in col_with_percentage:
             loan_data[col] = loan_data[col].astype('str')
             loan_data[col] = [x.replace('%','') for x in loan_data[col]]
In [87]: loan_data.dtypes
Out[87]: ID
                                            float64
         Amount.Requested
                                             object
         Amount.Funded.By.Investors
                                             object
         Interest.Rate
                                             object
         Loan.Length
                                             object
         Loan.Purpose
                                             object
         Debt.To.Income.Ratio
                                             object
         State
                                             object
         Home. Ownership
                                             object
         Monthly.Income
                                            float64
         FICO.Range
                                             object
         Open.CREDIT.Lines
                                             object
         Revolving.CREDIT.Balance
                                             object
         Inquiries.in.the.Last.6.Months
                                            float64
         Employment.Length
                                             object
         dtype: object
In [88]: loan data.head()
Out[88]:
                 ID Amount.Requested Amount.Funded.By.Investors Interest.Rate \
         0 81174.0
                                20000
                                                            20000
                                                                            8.90
         1 99592.0
                                19200
                                                            19200
                                                                           12.12
         2 80059.0
                                35000
                                                            35000
                                                                          21.98
         3 15825.0
                                10000
                                                                            9.99
                                                             9975
         4 33182.0
                                12000
                                                            12000
                                                                           11.71
                               Loan.Purpose Debt.To.Income.Ratio State Home.Ownership \
           Loan.Length
             36 months debt consolidation
                                                                     SC
                                                            14.90
                                                                               MORTGAGE
         0
                        {\tt debt\_consolidation}
         1
             36 months
                                                            28.36
                                                                     TX
                                                                               MORTGAGE
             60 months debt_consolidation
                                                            23.81
                                                                     CA
                                                                               MORTGAGE
             36 months debt_consolidation
                                                            14.30
                                                                     KS
                                                                               MORTGAGE
             36 months
                                                            18.78
                                                                                   RENT
                                credit_card
                                                                     NJ
            Monthly.Income FICO.Range Open.CREDIT.Lines Revolving.CREDIT.Balance
         0
                   6541.67
                               735-739
                                                       14
                                                                              14272
         1
                   4583.33
                               715-719
                                                       12
                                                                              11140
         2
                  11500.00
                               690-694
                                                       14
                                                                              21977
         3
                   3833.33
                               695-699
                                                       10
                                                                               9346
                               695-699
                   3195.00
                                                       11
                                                                              14469
```

Inquiries.in.the.Last.6.Months Employment.Length

0	2.0	< 1 year
1	1.0	2 years
2	1.0	2 years
3	0.0	5 years
4	0.0	9 years

Now the '%' symbol from 'Debt.To.Income.Ratio' and 'Interest.Rate' columns are gone. But still, they are not converted to integers, they are still string values.

```
In [89]: loan_data.dtypes
Out[89]: ID
                                            float64
         Amount.Requested
                                             object
         Amount.Funded.By.Investors
                                             object
         Interest.Rate
                                             object
         Loan.Length
                                             object
         Loan.Purpose
                                             object
         Debt.To.Income.Ratio
                                             object
         State
                                             object
         Home. Ownership
                                             object
         Monthly.Income
                                            float64
         FICO.Range
                                             object
         Open.CREDIT.Lines
                                             object
         Revolving.CREDIT.Balance
                                             object
         Inquiries.in.the.Last.6.Months
                                            float64
         Employment.Length
                                             object
```

dtype: object

Now, lets convert all the columns that has only numbers into numeric data types.

```
In [90]: columns_with_numbers_only = ['Amount.Requested', 'Amount.Funded.By.Investors',
                                       'Interest.Rate', 'Debt.To.Income.Ratio',
                                       'Monthly.Income', 'Open.CREDIT.Lines',
                                       'Revolving.CREDIT.Balance',
                                       'Inquiries.in.the.Last.6.Months']
         #Creating a list of column names that should be converted to integers
In [91]: for numeric_column_name in columns_with_numbers_only:
             loan_data[numeric_column_name] = pd.to_numeric(loan_data[numeric_column_name],
                                                           errors='coerce')
         #The 'errors=coerce' argument will replace all non-numeric values in the columns
         # with NaN values If this argument is missing then we will get an error and
         #execution will stop.
In [92]: loan_data.dtypes
Out [92]: ID
                                            float64
         Amount.Requested
                                           float64
```

```
float64
         Interest.Rate
         Loan.Length
                                             object
         Loan.Purpose
                                             object
         Debt.To.Income.Ratio
                                            float64
                                             object
         State
         Home. Ownership
                                             object
         Monthly.Income
                                            float64
         FICO.Range
                                             object
         Open.CREDIT.Lines
                                            float64
         Revolving.CREDIT.Balance
                                            float64
         Inquiries.in.the.Last.6.Months
                                            float64
         Employment.Length
                                             object
         dtype: object
In [93]: loan_data.head()
                                        Amount.Funded.By.Investors
Out [93]:
                     Amount.Requested
                                                                     Interest.Rate \
         0 81174.0
                              20000.0
                                                           20000.0
                                                                              8.90
         1 99592.0
                              19200.0
                                                           19200.0
                                                                             12.12
         2 80059.0
                              35000.0
                                                           35000.0
                                                                             21.98
         3 15825.0
                                                                              9.99
                              10000.0
                                                            9975.0
         4 33182.0
                               12000.0
                                                           12000.0
                                                                             11.71
           Loan.Length
                              Loan.Purpose Debt.To.Income.Ratio State Home.Ownership
             36 months debt_consolidation
                                                                      SC
                                                            14.90
                                                                               MORTGAGE
                                                            28.36
         1
             36 months
                        debt_consolidation
                                                                      TX
                                                                               MORTGAGE
         2
             60 months debt_consolidation
                                                            23.81
                                                                      CA
                                                                               MORTGAGE
         3
             36 months
                        debt_consolidation
                                                            14.30
                                                                      KS
                                                                               MORTGAGE
         4
             36 months
                                                            18.78
                                credit_card
                                                                      NJ
                                                                                   RENT
            Monthly.Income FICO.Range Open.CREDIT.Lines Revolving.CREDIT.Balance
         0
                   6541.67
                              735-739
                                                     14.0
                                                                             14272.0
         1
                   4583.33
                              715-719
                                                     12.0
                                                                             11140.0
         2
                  11500.00
                              690-694
                                                     14.0
                                                                             21977.0
         3
                   3833.33
                              695-699
                                                     10.0
                                                                              9346.0
         4
                   3195.00
                              695-699
                                                     11.0
                                                                             14469.0
            Inquiries.in.the.Last.6.Months Employment.Length
         0
                                        2.0
                                                     < 1 year
         1
                                        1.0
                                                      2 years
         2
                                        1.0
                                                      2 years
         3
                                        0.0
                                                      5 years
         4
                                        0.0
                                                      9 years
In [94]: (loan_data.dtypes=='object').sum(), (loan_data.dtypes=='float64').sum()
```

float64

Amount.Funded.By.Investors

Out[94]: (6, 9)

Now, we can see that we have only 6 columns as strings/object and the remaining 9 are integers. Let's also see what those object columns are

```
In [95]: object_column_names = loan_data.columns[loan_data.dtypes=='object']
         #creating a list of all columns which are of data type 'object'
         loan_data[object_column_names].head()
         #slicing the dataframe using those column names only
Out [95]:
           Loan.Length
                              Loan.Purpose State Home.Ownership FICO.Range \
             36 months debt_consolidation
                                              SC
                                                        MORTGAGE
                                                                    735-739
         0
         1
             36 months debt consolidation
                                              TX
                                                        MORTGAGE
                                                                    715-719
             60 months debt_consolidation
                                              CA
                                                        MORTGAGE
                                                                    690-694
             36 months debt_consolidation
                                              KS
                                                        MORTGAGE
                                                                    695-699
             36 months
                               credit_card
                                              NJ
                                                            RENT
                                                                    695-699
           Employment.Length
                    < 1 year
         0
                     2 years
         1
         2
                     2 years
         3
                     5 years
                     9 years
```

We can see that all the 6 object type columns clearly have strings or some string value in them

Here the variable 'Loan.Lenght' seems to be clearly categorical, so let's convert that into dummy variable

As we can see, there are 3 categories in that variable.

The function 'get\_dummies' from pandas creates dummy variables for all the categorical values we have. This function returns a dataframe. So, we can use that to create dummy variables, then drop the variables that we don't need.

```
In [97]: loan_lenght_dummies = pd.get_dummies(loan_data['Loan.Length'])
In [98]: loan_lenght_dummies.head()
Out [98]:
               36 months 60 months
         0
            0
                       1
                                  0
         1 0
                       1
                                   0
         2 0
                       0
                                  1
         3 0
                       1
                                  0
         4 0
                       1
                                  0
```

since '60\_months' and the other value '.' has very less number of values compared to the value '36\_months' we can drop them both altogether and add the dummy variable '36 months' to our original dataframe.

```
In [99]: loan_data['Loan_lenght_36'] = loan_lenght_dummies['36 months']
```

Now that we don't need the variable 'loan\_length\_dummies' we can drop it altogether. Note:dropping variables from notebook environment is a permenant operation.

To know what all variables we have in our environment at present we can use the function 'who'

```
In [101]: who
```

KFold	Lasso	LinearRegression	Ridge	e a	alphas	bes
col_with_p	ercentage	columns_with_numbe	ers_only	data_file	err	eri
linreg	loan_data	loan_data_dum	mies	lower_limit	math	np
pd	predictionErrorO	nTestData p	redictionErr	corOnTestData_las	380	prediction
rmse_lasso	rmse_list	t rmse_ridg	ge te	est_loan_data	train_	index
x test	x train	${\tt xval\_err}$	y test	y train		

Now that we have created dummy variables for the variable Loan.Lenght we can drop that variable from our original dataset

```
In [102]: loan_data.drop(labels='Loan.Length', axis=1, inplace=True)
In [103]: loan_data.head()
Out[103]:
                                         Amount.Funded.By.Investors Interest.Rate \
                      Amount.Requested
                  ID
                                20000.0
                                                                                8.90
          0
             81174.0
                                                             20000.0
          1
             99592.0
                                19200.0
                                                             19200.0
                                                                               12.12
             80059.0
                                35000.0
                                                             35000.0
                                                                               21.98
          3
             15825.0
                                10000.0
                                                              9975.0
                                                                                9.99
             33182.0
                                12000.0
                                                             12000.0
                                                                               11.71
                   Loan.Purpose Debt.To.Income.Ratio State Home.Ownership
                                                  14.90
             debt_consolidation
                                                           SC
                                                                    MORTGAGE
          0
             debt_consolidation
                                                  28.36
                                                           ΤX
                                                                    MORTGAGE
             debt_consolidation
                                                  23.81
                                                           CA
                                                                    MORTGAGE
          3
             {\tt debt\_consolidation}
                                                  14.30
                                                           KS
                                                                    MORTGAGE
                    credit_card
                                                  18.78
                                                           NJ
                                                                        RENT
```

Monthly.Income FICO.Range Open.CREDIT.Lines Revolving.CREDIT.Balance \

```
0
          6541.67
                      735-739
                                             14.0
                                                                     14272.0
          4583.33
                      715-719
                                             12.0
                                                                     11140.0
1
2
         11500.00
                      690-694
                                             14.0
                                                                     21977.0
3
          3833.33
                      695-699
                                             10.0
                                                                      9346.0
4
          3195.00
                      695-699
                                             11.0
                                                                     14469.0
   Inquiries.in.the.Last.6.Months Employment.Length Loan_lenght_36
0
                                             < 1 year
1
                               1.0
                                              2 years
                                                                     1
2
                                              2 years
                               1.0
                                                                     0
```

5 years

9 years

1

1

Let's see how many string datatype columns we have now

3

4

0.0

0.0

loan\_data[object\_column\_names].head()
#slicing the dataframe using those column names only

```
Out[104]:
                   Loan. Purpose State Home. Ownership FICO. Range Employment. Length
                                                         735-739
          0 debt_consolidation
                                    SC
                                             MORTGAGE
                                                                           < 1 year
             debt_consolidation
                                    TX
                                             MORTGAGE
                                                          715-719
                                                                            2 years
          2 debt_consolidation
                                    CA
                                             MORTGAGE
                                                          690-694
                                                                            2 years
          3 debt_consolidation
                                    KS
                                             MORTGAGE
                                                          695-699
                                                                            5 years
          4
                    credit_card
                                    NJ
                                                 RENT
                                                         695-699
                                                                            9 years
```

Now, we have only 4. Let's start to examine the next variable 'Loan.Purpose'

```
In [105]: loan_data['Loan.Purpose'].value_counts()
```

```
Out[105]: debt_consolidation
                                 1307
          credit_card
                                  444
          other
                                   200
                                  152
          home_improvement
          major_purchase
                                  101
          small business
                                   87
                                   50
          car
          wedding
                                   39
          medical
                                   30
          moving
                                   29
          vacation
                                   21
          house
                                   20
          educational
                                   15
          renewable_energy
                                    4
          Name: Loan.Purpose, dtype: int64
```

In [106]: print(len(loan\_data['Loan.Purpose'].value\_counts()))

We have 14 categories in the variable 'Loan.Purpose'.

We can either make 13 dummy variables or we can group some categories together to reduce the number of effective dummy variables needed.

One method we can use to find possibilities to group categories together is by performing group\_by operation between this variable and the response variable 'Interest.Rate'.

```
In [107]: loan_data.groupby('Loan.Purpose')['Interest.Rate'].mean().round()
Out[107]: Loan.Purpose
                                 11.0
          car
          credit_card
                                 13.0
          debt_consolidation
                                 14.0
          educational
                                 11.0
          home_improvement
                                 12.0
                                 13.0
          house
          major_purchase
                                 11.0
                                 12.0
          medical
          moving
                                 14.0
          other
                                 13.0
          renewable_energy
                                 10.0
          small_business
                                 13.0
          vacation
                                 12.0
                                 12.0
          wedding
          Name: Interest.Rate, dtype: float64
```

Let's see how many effective categories this grouping provides us

We can see there are 4 effective categories

```
# grouping all categories with mean value 13(received in line 25) together
              if loan_data.loc[i]['Loan.Purpose'] in ['credit_card', 'house', 'other',
                                                       'small_business']:
                  loan_data.loc[i,'Loan.Purpose'] = 'chos'
              # grouping all categories with mean value 14 (received in line 25) together
              if loan_data.loc[i]['Loan.Purpose'] in ['debt_consolidation','moving']:
                  loan data.loc[i, 'Loan.Purpose']='dm'
In [110]: loan_data['Loan.Purpose'].head()
Out[110]: 0
                 dm
                 dm
                 dm
          3
                 dm
          4
               chos
          Name: Loan.Purpose, dtype: object
```

As we can see, we have effectively combined the 13 out of 14 categories into 4 categories.

We have not included the category 'renewable\_energy' in this grouping because it had only 4 occurences in the entire data frame.

Now, let's create dummies for the variable Loan.Purpose

```
In [111]: loan_data_dummies = pd.get_dummies(loan_data['Loan.Purpose'], prefix='lp')
In [112]: loan_data_dummies.head()
Out[112]:
             lp_cem lp_chos lp_dm lp_hmvw lp_renewable_energy
                                   1
          1
                  0
                            0
                                                                   0
                                             0
          2
                  0
                            0
                                   1
                                             0
                                                                   0
          3
                  0
                            0
                                   1
                                             0
                                                                   0
          4
                  0
                            1
                                   0
                                             0
                                                                   0
```

As we can see we have a dummy variable for 'renewable\_energy'. Since we don't need it we can drop this variable and also the original variable 'Loan.Purpose'. But before that let's just concatanate the dummy variables to the original dataframe.

```
FL
       169
IL
       101
GA
        97
PA
        96
NJ
        94
VA
        78
        73
MA
OH
        71
MD
        68
        64
NC
CO
        61
WA
        58
CT
        50
AZ
        46
ΜI
        45
MN
        38
AL
        38
MO
        33
NV
        32
OR
        30
SC
        28
WI
        26
ΚY
        23
LA
        22
OK
        21
KS
        21
UT
        16
NH
        15
        15
RΙ
WV
        14
NM
        13
        13
AR
ΗI
        12
AK
        11
DC
        11
DΕ
         8
MT
         7
         5
VT
WY
         4
SD
         4
IN
         3
         1
MS
         1
         1
ΙA
Name: State, dtype: int64
```

There are too many states. Let's check how many unique values this variable has.

```
In [116]: loan_data['State'].nunique()
```

#### Out[116]: 47

There are 47 unique values in this variable, so for now, let's decide to drop this variable altogether. Although we don't have a reason to drop this variable, we will just to do that to reduce the amount of data preperation needed for now. We can add this variable later if needed.

```
In [117]: loan_data.drop(labels='State',axis=1,inplace=True)
In [118]: loan_data.columns[loan_data.dtypes=='object']
Out[118]: Index(['Home.Ownership', 'FICO.Range', 'Employment.Length'], dtype='object')
```

We have effectively reduced 6 'object' variables to 3. Let's go further and work with the other 3 variables.

Let's process the variable 'Home.Ownership'

Here we can simply ignore the categories 'OTHER' and 'NONE' and create dummy variables for the remaing 3 categories

```
In [120]: loan_data['ho_mortgage'] = np.where(loan_data['Home.Ownership']=='MORTGAGE',1,0)
          loan_data['ho_rent'] = np.where(loan_data['Home.Ownership'] == 'RENT',1,0)
In [121]: loan data.head()
Out[121]:
                                         Amount.Funded.By.Investors
                  ID
                      Amount.Requested
                                                                      Interest.Rate \
          0
             81174.0
                                20000.0
                                                             20000.0
                                                                               8.90
          1 99592.0
                                19200.0
                                                             19200.0
                                                                              12.12
          2 80059.0
                                                                              21.98
                                35000.0
                                                             35000.0
          3 15825.0
                                10000.0
                                                              9975.0
                                                                               9.99
             33182.0
                                12000.0
                                                             12000.0
                                                                              11.71
             Debt.To.Income.Ratio Home.Ownership
                                                   Monthly.Income FICO.Range
          0
                             14.90
                                         MORTGAGE
                                                                      735-739
                                                          6541.67
          1
                             28.36
                                         MORTGAGE
                                                          4583.33
                                                                      715-719
          2
                             23.81
                                         MORTGAGE
                                                          11500.00
                                                                      690-694
          3
                             14.30
                                                          3833.33
                                                                      695-699
                                         MORTGAGE
          4
                             18.78
                                             RENT
                                                          3195.00
                                                                      695-699
             Open.CREDIT.Lines Revolving.CREDIT.Balance \
          0
                          14.0
                                                  14272.0
```

11140.0

12.0

1

```
2
                  14.0
                                            21977.0
3
                  10.0
                                            9346.0
4
                  11.0
                                            14469.0
   Inquiries.in.the.Last.6.Months Employment.Length Loan length 36
0
                                 2.0
                                                < 1 year
                                                                                   0
                                                                          1
                                                 2 years
1
                                 1.0
                                                                          1
                                                                                   0
2
                                 1.0
                                                 2 years
                                                                          0
                                                                                   0
3
                                 0.0
                                                 5 years
                                                                                   0
                                                                          1
4
                                 0.0
                                                 9 years
                                                                          1
                                                                                   0
   lp_chos
            lp_dm lp_hmvw
                               ho_mortgage
0
          0
                                           1
                  1
                            0
                                           1
1
          0
                  1
                            0
                                                     0
2
                                                     0
          0
                  1
                            0
                                           1
3
          0
                  1
                            0
                                           1
                                                     0
4
          1
                            0
                                                     1
```

Now that we have created dummy variables for 'Home.Ownership' we can go ahead and drop that variable.

Since this variable has a range, one easy way is to replace each value with the average of the range.

In order to do that, 1. first let's split each value in the variable 'FICO.Range' on the hyphen('-') in the middle of the value. 2. Then let's put the first part of the split result (which will be the lower limit) in a list called 'lower\_limit' and the second part of the split result (which will be the upper limit) in a list called 'upper\_limit'. 3. Finally let's slice the lower and upper limit values from each list then find the average of these and insert them in a new variable called 'fico' in the original dataframe 'loan\_data'

```
In [125]: lower_limit=[]
     upper_limit=[]
```

```
lower_limit.append(int(loan_data['FICO.Range'][i].split('-')[0]))
              upper_limit.append(int(loan_data['FICO.Range'][i].split('-')[1]))
          #splitting the column on '-' and appending the results to two columns
          # called lower_limit and upper_limit
          for i in range(len(loan_data)):
              loan_data.loc[i,'fico'] = ((lower_limit[i]+upper_limit[i])/2)
          # on a for loop we slice the values from the two lists, find their average and inser
          # them in a new column called 'fico' in the original dataframe 'loan data'
   Now that we have created a new variable for the original variable 'FICO.Range' containing
the average value of the range, we can drop the original variable 'FICO.Range' and the temproary
lists 'lower_limit' and 'upper_limit'.
In [126]: loan_data.drop(labels='FICO.Range', axis=1, inplace=True)
          %reset_selective lower_limit, upper_limit
Once deleted, variables cannot be recovered. Proceed (y/[n])? y
In [127]: loan_data.head()
Out [127]:
                                          Amount.Funded.By.Investors
                  ID
                       Amount.Requested
                                                                       Interest.Rate \
          0
             81174.0
                                20000.0
                                                              20000.0
                                                                                 8.90
          1
             99592.0
                                19200.0
                                                              19200.0
                                                                                12.12
          2 80059.0
                                                                                21.98
                                35000.0
                                                              35000.0
          3 15825.0
                                10000.0
                                                               9975.0
                                                                                 9.99
             33182.0
                                12000.0
                                                              12000.0
                                                                                11.71
             Debt.To.Income.Ratio
                                    Monthly.Income
                                                     Open.CREDIT.Lines
          0
                             14.90
                                            6541.67
                                                                   14.0
          1
                             28.36
                                            4583.33
                                                                   12.0
          2
                             23.81
                                           11500.00
                                                                   14.0
          3
                             14.30
                                            3833.33
                                                                   10.0
          4
                             18.78
                                            3195.00
                                                                   11.0
             Revolving.CREDIT.Balance
                                        Inquiries.in.the.Last.6.Months Employment.Length
          0
                               14272.0
                                                                     2.0
                                                                                   < 1 year
          1
                               11140.0
                                                                                    2 years
                                                                     1.0
          2
                               21977.0
                                                                     1.0
                                                                                    2 years
          3
                                                                                    5 years
                                9346.0
                                                                     0.0
          4
                               14469.0
                                                                     0.0
                                                                                    9 years
             Loan_lenght_36 lp_cem lp_chos lp_dm lp_hmvw
                                                                ho_mortgage
          0
                           1
                                   0
                                             0
                                                    1
                                                              0
                                                                           1
                                                                                     0
```

for i in range(len(loan\_data)):

0

0

1

1

0

0

1

1

0

0

1

0

0

0

1

2

```
3
                           1
                                   0
                                                             0
                                                                                    0
                                                    1
                                                                           1
          4
                                             1
                                                    0
                                                                                    1
              fico
          0 737.0
          1 717.0
          2 692.0
          3 697.0
          4 697.0
In [128]: loan_data.columns[loan_data.dtypes=='object']
Out[128]: Index(['Employment.Length'], dtype='object')
   The only remaining 'object' column is 'Employment.Length'. Let's deal with that now.
In [129]: loan_data['Employment.Length'].value_counts()
Out[129]: 10+ years
                        653
          < 1 year
                        249
          2 years
                        243
          3 years
                        235
          5 years
                        202
          4 years
                        191
          1 year
                        177
          6 years
                        163
          7 years
                        127
          8 years
                        108
          9 years
                         72
          Name: Employment.Length, dtype: int64
   Let's first fix remove the words 'years' and 'year' from the variable.
In [130]: loan_data['Employment.Length'] = loan_data['Employment.Length'].astype('str')
              # first let's convert the variable to string datatype so that removing words and
              # be easy
          loan_data['Employment.Length'] = [x.replace('years','') for x in
                                              loan_data['Employment.Length']]
          loan_data['Employment.Length'] = [x.replace('year', '') for x in
                                              loan_data['Employment.Length']]
In [131]: loan_data['Employment.Length'].value_counts()
Out[131]: 10+
                  653
          < 1
                  249
                  243
                  235
          3
```

```
5
        202
4
        191
1
        177
6
        163
7
        127
8
         108
nan
         78
9
          72
           2
Name: Employment.Length, dtype: int64
```

Now let's group this variable with the response variable 'Interest.Rate' so we can combine categories togther

```
In [132]: loan_data.groupby('Employment.Length')['Interest.Rate'].mean().round(2)
Out[132]: Employment.Length
                   11.34
          1
                   12.49
          10+
                   13.34
          2
                   12.87
          3
                   12.77
          4
                   13.14
          5
                   13.40
          6
                   13.29
          7
                   13.10
          8
                   13.01
          9
                   13.15
          < 1
                   12.86
          nan
                   12.78
          Name: Interest.Rate, dtype: float64
```

- 1. As we can see, 'nan' and '<1' are similar to each other in mean. so we can compare them together.
- 2. '<1' means 0, so we can replace that with 0.
- 3. '10+' can be replaced by 10.

2 2.0 3 5.0 4 9.0 Name: Employment.Length, dtype: float64 In [135]: loan\_data.dtypes Out[135]: ID float64 Amount.Requested float64 Amount.Funded.By.Investors float64 Interest.Rate float64 Debt.To.Income.Ratio float64 Monthly.Income float64 Open.CREDIT.Lines float64 Revolving.CREDIT.Balance float64 Inquiries.in.the.Last.6.Months float64 Employment.Length float64 Loan\_lenght\_36 uint8 lp\_cem uint8 lp\_chos uint8 lp\_dm uint8 lp\_hmvw uint8 ho\_mortgage int32 int32 ho\_rent fico float64 dtype: object

Now, all our variables are numeric. We can also drop the variable 'ID' because it's the identity number for every person and doesn't solve any real purpose.

```
In [136]: loan_data.drop(labels='ID',axis=1,inplace=True)
In [137]: loan_data.head()
Out [137]:
             Amount.Requested Amount.Funded.By.Investors
                                                            Interest.Rate \
                      20000.0
                                                                      8.90
          0
                                                    20000.0
          1
                       19200.0
                                                    19200.0
                                                                     12.12
          2
                       35000.0
                                                    35000.0
                                                                     21.98
          3
                       10000.0
                                                     9975.0
                                                                      9.99
          4
                       12000.0
                                                    12000.0
                                                                     11.71
             Debt.To.Income.Ratio Monthly.Income Open.CREDIT.Lines
          0
                             14.90
                                                                   14.0
                                           6541.67
          1
                             28.36
                                           4583.33
                                                                  12.0
          2
                             23.81
                                          11500.00
                                                                  14.0
          3
                             14.30
                                           3833.33
                                                                  10.0
                             18.78
                                           3195.00
                                                                  11.0
```

Revolving.CREDIT.Balance Inquiries.in.the.Last.6.Months \

```
2.0
          0
                                14272.0
          1
                                11140.0
                                                                       1.0
          2
                                21977.0
                                                                       1.0
          3
                                 9346.0
                                                                      0.0
          4
                                                                      0.0
                                14469.0
             Employment.Length Loan lenght 36
                                                  lp_cem
                                                           lp_chos
                                                                      lp dm
                                                                             lp hmvw
                             0.0
          0
                                                1
                                                                  0
                                                                          1
          1
                             2.0
                                                1
                                                         0
                                                                  0
                                                                          1
                                                                                   0
          2
                             2.0
                                                0
                                                         0
                                                                  0
                                                                          1
                                                                                   0
          3
                             5.0
                                                1
                                                         0
                                                                  0
                                                                                   0
                                                                          1
          4
                             9.0
                                                1
                                                         0
                                                                  1
                                                                          0
                                                                                    0
             ho_mortgage
                           ho_rent
                                      fico
                                     737.0
          0
                        1
          1
                        1
                                  0 717.0
          2
                        1
                                  0 692.0
          3
                                  0 697.0
                        1
          4
                        0
                                     697.0
In [138]: loan_data.isna().sum().sum()
Out[138]: 33
In [139]: loan_data.shape
Out[139]: (2500, 17)
In [140]: loan_data.dropna(axis=0,inplace=True)
In [141]: loan_data.shape
Out[141]: (2473, 17)
   Now, let's split the data into train and test data to proceed with modelling.
In [142]: train_loan_data, test_loan_data = train_test_split(loan_data, test_size=0.2,
                                                                 random_state=2)
In [143]: train_loan_data.shape, test_loan_data.shape
Out[143]: ((1978, 17), (495, 17))
```

'Interest.Rate' variable is the one we are going to predict, so let's make that the 'Y' variable in both training and test data and drop it from the X variable in both training and test data.

Also the variable 'Amount.Funded.By.Investors' won't be available to us at this point in real life. So, let's drop this also from the training and test data.

```
In [144]: x_train=train_loan_data.drop(labels=['Interest.Rate', 'Amount.Funded.By.Investors'],
                                         axis=1)
          y_train=train_loan_data['Interest.Rate']
          x_test=test_loan_data.drop(labels=['Interest.Rate', 'Amount.Funded.By.Investors'],
                                       axis=1)
          y_test=test_loan_data['Interest.Rate']
In [145]: linreg=LinearRegression()
          #Initializing a linear regression object
In [146]: linreg.fit(X=x_train, y=y_train)
          #fitting the linear model on train data
Out[146]: LinearRegression(copy_X=True, fit_intercept=True, n_jobs=None,
                    normalize=False)
In [147]: predictions=linreg.predict(X=x_test)
          #Making predictions on test data
In [148]: error=predictions-y_test
          #calculating the errors in prediction by fiding the difference in actual 'y' and
          # predicted 'y'
In [149]: %%latex
          m = 1/m \times \sum_{i=0}^{m-1} \operatorname{predictions}(i) - ytest(i))^2
  rmse = 1/m * \sum_{i=0}^{m-1} \sqrt{(predictions(i) - ytest(i))^2}
In [150]: rmse=np.sqrt((np.sum(error**2))/len(x_test))
In [151]: rmse
Out[151]: 2.0225656998568877
   RMSE can be used to compare our linear regression model with other techniques and eventu-
ally pick the model with the least error.
   Next, let's see how to extract coefficients from the model.
In [152]: coefs=linreg.coef_
          #these are the beta or theta values(beta_1 to beta_n) that our model is predicting
In [153]: linreg.intercept_
          # this is the intercept value
Out[153]: 75.24596218863286
In [154]: features = x_train.columns
In [155]: list(zip(features,coefs))
```

# 0.1 Regularization

As we can see, linear regression gives the coefficient value for each feature. Ideally, the feature which does not contribute much in predicting our output variable should have a coefficient value of 0. But it is not the case. So, we use regularization to penalize and minimize the coefficients of variables that don't contribute much to our model.

# 0.2 Ridge Regression

alpha or regularisation parameter is a hyperparameter and we'd look at multiple values of it and choose the best one through 10 fold cross validation. Note: In class notes, regularisation parameter is called lambda

We have initiated 10 fold cross validation object so cross validation loop will run for 10 iterations and each time our training data X\_train will be split into 10 buckets. Likewise if we use 20 fold cross validation our cross validation loop will run for 20 times and the training data will be split into 20 buckets.

- 1.2. We initiate an object called xval\_err as 0.
- 1.3. For each alpha and first iteration of the KFold validation:
  - 1.3.1. The k-fold will split our training data [x\_train] into 9 buckets of training data and 1 bucket of validation data. It will use 9 buckets of the training data [X\_train] to train the Ridge model and 1 bucket of the training data [X\_train] to preside the output [Y\_cap].
  - 1.3.2. This predicted 'y\_cap' is subtracted from the actual y values from the training data  $[X_train]$  corresponding to the 10th set (validation set) to calculate the validation error.
  - 1.3.3. The validation error for this iteration is squared and added to the variable xval\_err for the next 10 iterations.
- 1.4. The total validation error for the past 10 iterations are squared, divided by the length of the training dataset  $(x_train)$  and a squared root is taken on the quotient.

This is the RMSE for this value of alpha using 10 fold CV.

- 1.5. This RMSE value is stored in the rmse\_list object.

  Once we have completed iterating through all the alpha values, the rmse\_list object will have a length of 100, since we use 100 different alpha values.
- 1.6. Finally the alpha value which corresponds to the minimum rmse value is returned as the optimal alpha value.

"""
rmse\_list=[]

for a in alphas:
 ridge=Ridge(fit\_intercept=True, alpha=a)

# ridge is a linear regression model with L2 regularization.

kf = KFold(n\_splits=10)
xval\_err=0

```
i = 0
              for train_index, validation_index in kf.split(x_train):
                  #print(len(train_index), len(validation_index))
                  ridge.fit(x_train.iloc[train_index,:], y_train[train_index])
                  p=ridge.predict(x train.iloc[validation index,:])
                  err = p-y_train[validation_index] #iloc doesn't work here for some reason
                  xval err = xval err+np.dot(err, err)
              rmse_10cv = np.sqrt(xval_err/len(x_train))
              rmse_list.append(rmse_10cv)
              print('{:.3f}\t {:.6f}\t'.format(a, rmse_10cv))
          best_alpha= alphas[rmse_list==min(rmse_list)]
          print('Alpha with minimum 10CV error is {} and the corresponding RMSE is {}: '.
                format(best_alpha[0], min(rmse_list)))
0.000
              2.070131
0.101
              2.070081
0.202
              2.070040
0.303
              2.070008
0.404
              2.069980
0.505
              2.069957
0.606
              2.069938
0.707
              2.069921
0.808
              2.069906
0.909
              2.069892
1.010
              2.069881
1.111
              2.069870
1.212
              2.069861
1.313
              2.069853
1.414
              2.069845
1.515
              2.069838
1.616
              2.069832
1.717
              2.069827
1.818
              2.069821
1.919
              2.069817
2.020
              2.069813
2.121
              2.069809
2.222
              2.069806
2.323
              2.069803
2.424
              2.069800
2.525
              2.069797
2.626
              2.069795
2.727
              2.069793
2.828
              2.069792
2.929
              2.069790
3.030
              2.069789
3.131
              2.069788
3.232
              2.069788
3.333
              2.069787
```

3.434	2.069787
3.535	2.069787
3.636	2.069787
3.737	2.069787
3.838	2.069787
3.939	2.069788
4.040	2.069789
4.141	2.069790
4.242	2.069791
4.343	2.069792
4.444	2.069793
4.546	
	2.069795
4.647	2.069796
4.748	2.069798
4.849	2.069800
4.950	2.069802
5.051	2.069804
5.152	2.069807
5.253	2.069809
5.354	2.069812
5.455	2.069815
5.556	2.069817
5.657	2.069820
5.758	2.069824
5.859	2.069827
5.960	2.069830
6.061	2.069834
6.162	2.069837
6.263	2.069841
6.364	2.069845
6.465	2.069849
6.566	2.069853
6.667	2.069857
6.768	2.069861
6.869	2.069866
6.970	2.069870
7.071	2.069875
7.172	2.069880
7.273	2.069884
7.374	2.069889
7.475	2.069894
7.576	2.069900
7.677	2.069905
7.778	2.069910
7.879	2.069916
7.980	2.069910
8.081	2.069927
8.182	2.069933

```
8.283
               2.069939
8.384
               2.069945
8.485
              2.069951
8.586
              2.069957
8.687
              2.069964
8.788
               2.069970
8.889
              2.069977
8.990
              2.069983
9.091
              2.069990
9.192
              2.069997
9.293
              2.070004
9.394
              2.070011
9.495
               2.070018
9.596
              2.070025
9.697
               2.070032
9.798
              2.070040
9.899
               2.070047
10.000
                2.070055
```

Alpha with minimum 10CV error is 3.5354181818181822 and the corresponding RMSE is 2.0697866245

Now we will use the best alpha value that we just determined to fit a ridge regression object on the entire dataset and predict the rmse value for the entire dataset.

```
In [158]: ridge=Ridge(fit_intercept=True, alpha=best_alpha)
          ridge.fit(x_train, y_train)
          predictionsOnTestData = ridge.predict(x_test)
          predictionErrorOnTestData = predictionsOnTestData - y_test
          rmse_ridge = np.sqrt(np.dot(predictionErrorOnTestData,
                                      predictionErrorOnTestData)/len(predictionsOnTestData))
          rmse_ridge
Out[158]: 2.0236668696412723
In [159]: list(zip(x_train.columns,ridge.coef_))
Out[159]: [('Amount.Requested', 0.0001641799190080323),
           ('Debt.To.Income.Ratio', 0.0006487949921075561),
           ('Monthly.Income', -4.169344863753166e-05),
           ('Open.CREDIT.Lines', -0.039616383599302744),
           ('Revolving.CREDIT.Balance', -2.5209565104184987e-06),
           ('Inquiries.in.the.Last.6.Months', 0.3870049295626152),
           ('Employment.Length', 0.004888838204666946),
           ('Loan_lenght_36', -3.041894854788477),
           ('lp_cem', 0.011310143101232472),
           ('lp_chos', -0.0321514576874333),
           ('lp_dm', -0.1690620008874746),
           ('lp_hmvw', -0.2882910897632634),
           ('ho_mortgage', -0.3626507937625516),
```

```
('ho_rent', -0.11681552700277421), ('fico', -0.08593974410496531)]
```

### 0.2.1 Results of Ridge Regression:

We can see that ridge even though regression shrinks the coefficient value for each variable, it never really makes them 0. Which means it never shrinks the size of our model.

# 0.3 Lasso Regression

In [160]: """

We have 100 values of alpha between 0.001 and 1. We use these 100 values and 10 fold CV for each value to see which value has the least rmse, that value will be the best alpha.

In the for-loop below:

- 1. For each value of alpha:
  - 1.1 We initiate a KFold object for 10 fold cross-validation.

We have initiated 10 fold cross validation object so cross validation loop will run for 10 iterations and each time our training data X\_train will be split into 10 buckets. Likewise if we use 20 fold cross validation our cross validation loop will run for 20 times and the training data will be split into 20 buckets.

- 1.2. We initiate an object called xval\_err which is equal to 0.
- 1.3. For each alpha and first iteration of the KFold validation:
  - 1.3.1. The k-fold will split our training data [x\_train] into 9 buckets of training data and 1 bucket of validation data. It will use 9 buckets of the training data [X\_train] to train the Lasso model and 1 bucket of the training data [X\_train] to predect the output [Y\_cap].
  - 1.3.2. This predicted 'y\_cap' is subtracted from the actual y values from the training data  $[X_train]$  corresponding to the 10th set (validation set) to calculate the validation error.
  - 1.3.3. The validation error for this iteration is squared and added to the variable xval\_err for the next 10 iterations.

```
training dataset(x_train) and a squared root is taken on the
                  quotient.
                  This is the RMSE for this value of alpha using 10 fold CV.
                  1.5. This RMSE value is stored in the rmse list object.
                  Once we have completed iterating through all the alpha values,
                  the rmse_list object will have a length of 100, since we
                  use 100 different alpha values.
                  1.6. Finally the alpha value which corresponds to the minimum
                  rmse value is returned as the optimal alpha value."""
          alphas=np.linspace(0.0001,1,100)
          rmse_list=[]
          for a in alphas:
              lasso=Lasso(fit_intercept=True, alpha=a, max_iter=10000)
              # Lasso is a linear regression model with L1 regularization.
              kf = KFold(n splits=10)
              xval_err=0
              for train_index, validation_index in kf.split(x_train):
                  lasso.fit(x_train.iloc[train_index,:], y_train[train_index])
                  p=lasso.predict(x_train.iloc[validation_index,:])
                  err = p-y_train[validation index] #iloc doesn't work here for some reason
                  xval_err = xval_err+np.dot(err, err)
              rmse_10cv = np.sqrt(xval_err/len(x_train))
              rmse_list.append(rmse_10cv)
              print('{:.3f}\t {:.6f}\t'.format(a, rmse_10cv))
          best_alpha= alphas[rmse_list==min(rmse_list)]
          print('Alpha with minimum 10CV error is {} and the corresponding RMSE is {}: '.
                format(best_alpha[0], min(rmse_list)))
0.000
              2.070110
0.010
              2.069490
0.020
              2.069924
0.030
              2.071233
0.041
              2.073187
0.051
              2.075622
0.061
              2.077515
0.071
              2.079609
0.081
              2.082291
0.091
              2.085403
0.101
              2.088892
0.111
              2.092756
0.121
              2.096993
```

1.4. The total validation error for the past 10 iterations

are squared, divided by the length of the

0.131	2.101651
0.141	2.106692
0.152	2.112098
0.162	2.117865
0.172	2.123991
0.182	2.130519
0.192	2.137403
0.202	2.144636
0.212	2.152212
0.222	2.160129
0.232	2.168383
0.242	2.176970
0.253	2.185886
0.263	2.195126
0.273	2.204688
0.283	2.214567
0.293	2.224758
0.303	2.235257
0.313	2.246061
0.323	2.257168
0.333	2.268569
0.343	2.280261
0.354	2.292239
0.364	2.304500
0.374	2.317037
0.384	2.329848
0.394	2.342926
0.404	2.356269
0.414	2.369871
0.424	2.382382
0.434	2.391821
0.444	2.397942
0.455	2.399453
0.465	2.400998
0.475	2.402576
0.485	2.404186
0.495	2.405833
0.505	2.407512
0.515	2.409228
0.525	2.410977
0.535	2.412759
0.545	2.414465
0.556	2.415905
0.566	2.417304
0.576	2.418402
0.586	2.419524
0.596	2.420670
0.606	2.421792
0.000	2.421192

```
0.616
              2.422704
0.626
              2.423412
0.636
              2.423918
0.646
              2.424262
0.657
               2.424449
0.667
              2.424487
0.677
              2.424484
0.687
              2.424482
0.697
              2.424464
0.707
              2.424446
0.717
              2.424429
0.727
              2.424410
0.737
               2.424384
0.747
              2.424358
0.758
              2.424331
0.768
              2.424302
0.778
              2.424273
0.788
              2.424244
0.798
              2.424217
0.808
              2.424189
0.818
              2.424163
0.828
              2.424136
0.838
              2.424113
0.848
              2.424115
0.859
              2.424118
0.869
              2.424120
0.879
              2.424123
0.889
              2.424125
0.899
              2.424128
0.909
              2.424130
0.919
              2.424133
0.929
              2.424136
0.939
              2.424138
0.949
              2.424141
0.960
              2.424144
0.970
              2.424147
0.980
              2.424149
0.990
              2.424152
1.000
              2.424155
```

Alpha with minimum 10CV error is 0.01019999999999999999999999999999 and the corresponding RMSE is 2.069490409

The best alpha value we got throuh lasso regression is 0.010199. We will use this value to train our final Lasso model and calculate the rmse.

```
predictionErrorOnTestData_lasso = predictionsOnTestData_lasso - y_test
          rmse_lasso = np.sqrt(np.dot(predictionErrorOnTestData_lasso,
                                       predictionErrorOnTestData_lasso)/len(predictionsOnTestDa
          rmse_lasso
Out[161]: 2.023276788895483
In [162]: list(zip(x_train.columns,lasso.coef_))
Out[162]: [('Amount.Requested', 0.00016395821531931226),
           ('Debt.To.Income.Ratio', 0.00032219108556223947),
           ('Monthly.Income', -4.2720916538871394e-05),
           \hbox{('Open.CREDIT.Lines', $-0.03907551699159986),}\\
           ('Revolving.CREDIT.Balance', -2.5527196166969956e-06),
           ('Inquiries.in.the.Last.6.Months', 0.37860640070117296),
           ('Employment.Length', 0.002810166741741678),
           ('Loan_lenght_36', -3.0073811789972993),
           ('lp_cem', 0.0),
           ('lp_chos', 0.057359802778081066),
           ('lp_dm', -0.027293745553160276),
           ('lp_hmvw', -0.0562011482052836),
           ('ho_mortgage', -0.22708727621821279),
           ('ho_rent', -0.0),
           ('fico', -0.08593321837314784)]
```

#### 0.3.1 Results of Lasso Regression

As, we can see Lasso regression not only reduces our RMSE value a little, it also reduces the size of our model by making the coefficients of some variables as zero.