2023-03-17

10.1: Recursion

<u>Wikipedia:</u> Recursion is the process a procedure goes through when <u>one of the</u> <u>steps of the procedure involves invoking the procedure itself</u>. A procedure that goes through recursion is said to be 'recursive'.

<u>GeeksforGeeks</u>: A recursive function solves a particular problem by <u>calling a copy of itself and solving smaller subproblems of the original problems</u>. ... It is essential to know that we should provide a certain case in order to terminate this recursion process. So we can say that <u>every time the function calls itself with a simpler version of the original problem.</u>

Chris: Recursion is what happens when a method calls itself

<u>Wikipedia:</u> Recursion is the process a procedure goes through when <u>one of the</u> <u>steps of the procedure involves invoking the procedure itself</u>. A procedure that goes through recursion is said to be 'recursive'.

<u>GeeksforGeeks</u>: A recursive function solves a particular problem by <u>calling a copy of itself and solving smaller subproblems of the original problems</u>. ... It is essential to know that we should provide a certain case in order to terminate this recursion process. So we can say that <u>every time the function calls itself with a simpler version of the original problem.</u>

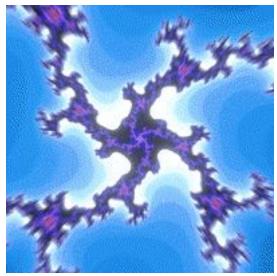
Chris: Recursion is what happens when a method calls itself

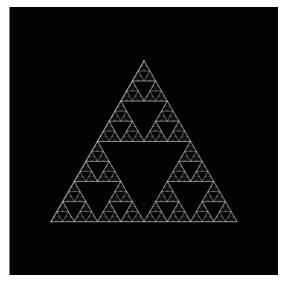
Or described another way...



- Many recursive methods can be written in a non-recursive (iterative) way, however depending on the problem you are trying to solve - recursion can greatly improve the readability of your code (although it may be more challenging to conceptually understand)
- Some common examples where recursion works well
 - Calculating the Fibonacci Sequence up to a certain number
 - Traversing a list, map, tree, or filesystem
 - Generating fractals...







Common pitfalls that generate incorrect results or cause infinite recursion

- Not properly sub-dividing the problem on each invocation
- Not properly identifying the end state (or Base Case) when the recursion should stop



Common pitfalls that generate incorrect results or cause **infinite recursion**



- pro
- When you program runs it reserves a section of memory called the stack
- The stack is used by the program to understand where it is and what it is doing
- No sta rec
- Usually this means that whatever is on the top of the stack (or on the bottom for some architectures) is the current execution context - which has things like the current local variables
- Every time you invoke a method another execution context is pushed onto the stack
- During infinite recursion methods keep calling themselves each time adding another execution context to the stack - until eventually the stack runs out of space and your program crashes with a stack overflow error

Common pitfalls that generate incorrect results or cause infinite recursion

- Not properly sub-dividing the problem on each invocation
- Not properly identifying the end state (or Base Case) when the recursion should stop



```
void printMessage(String message) {
  printMessage(message);
}
printMessage("Hello!");
```

Common pitfalls that generate incorrect results or cause infinite recursion

- Not properly sub-dividing the problem on each invocation
- Not properly identifying the end state (or Base Case) when the recursion should stop

```
void printMessage(String message)
  printMessage(message);
}
printMessage("Hello!");
```

```
//b35c90/reanat.java/jat_ws/recursion_b/8abaai/bin lest
Exception in thread "main" java.lang.StackOverflowError
        at Test.printMessage(Test.java:8)
        at Test.printMessage(Test.java:8)
```

Infinite Recursion due to no Base Case

```
void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse(nums, 0);

    Print the array of integers in reverse order

• For each invocation we pass in the array and
an ever-increasing index into the array
• While the index is less that the length of
the array - we keep calling ourselves

    Until the index has reached the end - and

then we stop the process and begin to unwind
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```

```
void printReverse(int[] nums, int idx) {
                                                 printReverse(nums, 0)
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse(nums, 0);

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```

```
printReverse(nums, 0)
  printReverse(nums, 1)
```

```
void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
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```

```
printReverse(nums, 0)
  printReverse(nums, 1)
  printReverse(nums, 2)
```

```
void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
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printReverse(nums, 0)
  printReverse(nums, 1)
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    printReverse(nums, 3)
```

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void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
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int[] nums = new int[] { 1, 2, 3, 4, 5 };
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printReverse(nums, 0)
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    printReverse(nums, 3)
    printReverse(nums, 4)
```

```
void printReverse(int[] nums, int idx) {
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printReverse(nums, 0)
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void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
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printReverse(nums, 0)
  printReverse(nums, 1)
    printReverse(nums, 2)
    printReverse(nums, 3)
       printReverse(nums, 4)
       printReverse(nums, 5)
       // stop
```

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void printReverse(int[] nums, int idx) {
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    printReverse(nums, idx + 1);
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```
printReverse(nums, 0)
  printReverse(nums, 1)
    printReverse(nums, 2)
      printReverse(nums, 3)
        printReverse(nums, 4)
          printReverse(nums, 5)
            // stop
          System.out.println(nums[4])
> 5
```

```
void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse(nums, 0);
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printReverse(nums, 0)
  printReverse(nums, 1)
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      printReverse(nums, 3)
        printReverse(nums, 4)
          printReverse(nums, 5)
            // stop
          System.out.println(nums[4])
        System.out.println(nums[3])
> 5
```

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void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse(nums, 0);

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          printReverse(nums, 5)
            // stop
          System.out.println(nums[4])
        System.out.println(nums[3])
      System.out.println(nums[2])
> 5
```

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void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
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  printReverse(nums, 1)
    printReverse(nums, 2)
      printReverse(nums, 3)
        printReverse(nums, 4)
          printReverse(nums, 5)
            // stop
          System.out.println(nums[4])
        System.out.println(nums[3])
      System.out.println(nums[2])
    System.out.println(nums[1])
> 5
> 2
```

```
void printReverse(int[] nums, int idx) {
  if (idx < nums.length) {</pre>
    printReverse(nums, idx + 1);
    System.out.println(nums[idx]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse(nums, 0);
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      printReverse(nums, 3)
        printReverse(nums, 4)
          printReverse(nums, 5)
            // stop
          System.out.println(nums[4])
        System.out.println(nums[3])
      System.out.println(nums[2])
    System.out.println(nums[1])
  System.out.println(nums[0])
> 5
> 2
> 1
```

```
import java.util.Arrays;
void printReverse2(int[] nums) {
  if (0 != nums.length) {
    printReverse2 (Arrays.copyOfRange (
      nums, 1, nums.length));
    System.out.println(nums[0]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse2(nums);
• For each invocation we create a new copy of
the array that removes the first element
• While the array passed is not empty - we
keep calling ourselves
• When an empty array is passed - we stop the
process and begin to unwind
```

```
import java.util.Arrays;
void printReverse2(int[] nums) {
  if (0 != nums.length) {
    printReverse2 (Arrays.copyOfRange (
      nums, 1, nums.length));
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int[] nums = new int[] { 1, 2, 3, 4, 5 };
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    System.out.println(nums[0]);
int[] nums = new int[] { 1, 2, 3, 4, 5 };
printReverse2(nums);
• For each invocation we create a new copy of
the array that removes the first element
• While the array passed is not empty - we
keep calling ourselves

    When an empty array is passed - we stop the

process and begin to unwind
```

```
printReverse([1,2,3,4,5])
  printReverse([2,3,4,5])
   printReverse([3,4,5])
    printReverse([4,5])
    printReverse([5])
    printReverse([5])
    // stop
```

```
import java.util.Arrays;
                                                printReverse([1,2,3,4,5])
                                                  printReverse([2,3,4,5])
void printReverse2(int[] nums) {
                                                    printReverse([3,4,5])
  if (0 != nums.length) {
                                                      printReverse([4,5])
    printReverse2 (Arrays.copyOfRange (
                                                        printReverse([5])
      nums, 1, nums.length));
                                                          printReverse([])
                                                            // stop
    System.out.println(nums[0]);
                                                           System.out.println(nums[0])
                                                         System.out.println(nums[0])
                                                      System.out.println(nums[0])
int[] nums = new int[] { 1, 2, 3, 4, 5 };
                                                    System.out.println(nums[0])
printReverse2(nums);
                                                  System.out.println(nums[0])
• For each invocation we create a new copy of
                                                > 5
the array that removes the first element
• While the array passed is not empty - we
keep calling ourselves
                                                > 2

    When an empty array is passed - we stop the

process and begin to unwind
```

Recursion Done Correctly

Recursion Done Correctly

Includes termination criteria ("Base Case")
"Will it ever end?"

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Includes termination criteria ("Base Case")
"Will it ever end?"

Each invocation sub-divides the problem "Will it process all the data"



```
Recursion - Example 1 (increase offset)

void printReverse(int[] nums, int idx) {
   if (idx < nums.length) {
        printReverse(nums, idx + 1);
        System.out.printIn(nums[idx]);
   }
}</pre>
recursion - Example 2 (trim data)

void printReverse2 (int[] nums) {
   if (0 != nums.length) {
        printReverse2 (Arrays.copyOfRange (
            nums, 1, nums.length));
        System.out.printIn(nums[0]);
}

System.out.printIn(nums[0]);
}
```

Includes termination criteria ("Base Case")
"Will it ever end?"

Each invocation sub-divides the problem "Will it process all the data"





```
int getWordCount(String text, String word) {
  int count = 0;
  if (text.length() >= word.length()) {
    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;
• For each invocation we determine if the word
appears at the beginning of text
• While the text is at least as long as word - we
keep calling ourselves
• Each recursive call returns a count that is added
to the count of the caller as we unwind
```

```
int getWordCount(String text, String word) {
  int count = 0;
  if (text.length() >= word.length()) {
    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;

    For each invocation we determine if the word

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int getWordCount(String text, String word) {
  int count = 0;
  if (text.length() >= word.length()) {
    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;

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    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;

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int getWordCount(String text, String word) {
  int count = 0;
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    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;

    For each invocation we determine if the word

appears at the beginning of text
• While the text is at least as long as word - we
keep calling ourselves

    Each recursive call returns a count that is added

to the count of the caller as we unwind
```

```
getWordCount("hello","l")
  getWordCount("ello","l")
    getWordCount("llo","l")
    getWordCount("lo","l")
    getWordCount("o","l")
    getWordCount("","l")
    // stop
```

```
int getWordCount(String text, String word) {
  int count = 0;
  if (text.length() >= word.length()) {
    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
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    For each invocation we determine if the word

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```

Recursion - Example 3 (data a

Includes termination criteria ("Base Case")
"Will it ever end?"

```
int getWordCount(String text, String word) {
  int count = 0;
  if (text.length() >= word.length()) {
    String s = text.substring(0, word.length());
    if (s.equals(word)) {
      count += 1;
    count += getWordCount(text.substring(1), word);
  return count;

    For each invocation we determine if the word

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    Each recursive call returns a count that is added

to the count of the caller as we unwind
```

Each invocation sub-divides the problem "Will it process all the data"

Practice on your own

- CSAwesome 10.1 Recursion
- Replit Recursion