

# **ME2021 – Mechanics of Machines I**

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## **Lecture 01: INTRODUCTION TO MECHANISMS AND KINEMATICS**

**Thilina H. Weerakkody**

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SLIIT.*

# Introduction

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This module develops the

- knowledge to **motion of a particle or multibody system**,
- knowledge to **analyse kinematics, kinetics and dynamic of planer mechanisms, gear transmission systems** and
- knowledge to **analyse power transmission devices**.

# Outline

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1. **Introduction:** Kinematic analysis of 2D Link mechanisms, Kinematic pairs, degree of freedom of a kinematic chain, mechanism mobility analysis using Grubler's criterion, Commonly employed mechanisms: four-bar mechanism and Grashof's Criterion, Slider crank mechanism and inversions.
2. **Kinematic Analysis of planer mechanisms** (Analytical approach using vector loop method)
3. **Gears and Gear Trains:** Friction gearing, common types of toothed gears, involute gear teeth, speed-ratio, simple gear train, compound gear trains, planetary gear trains, kinematic analysis of multiple stage planetary gear trains, differentials.
4. **Static force analysis for planer mechanisms.** Two force and Three force members, static force analysis using force polygon method.
5. **Kinetic analysis of planer mechanisms**, free body diagram, D'Alembert's principle, dynamic equilibrium

# Recommended Text

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- *Waldron, K.J., and Kinzel, G.L., “Kinematics, Dynamics, and Design of Machinery”, 3rd edition, Wiley.*
- *W.L. Cleghorn, “Mechanisms and Machines” 2<sup>nd</sup> edition, Oxford University Press, 2015.*
- *John J. Uicker, Gordon R. Pennock and Joseph E. Shigley, “Theory of Machines and Mechanisms”, Oxford University Press*

# Learning Outcomes

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- LO1:** Explain the significance, effect and control of mechanical vibrations in the design and operation of mechanical plant.
- LO2:** Identify kinematic loops in a mechanism; apply closed-form position analysis methods.
- LO3:** Differentiate loop closure equations to perform velocity and acceleration analysis.
- LO4:** Simulate mechanism motion using computer software.
- LO5:** Understand, motion limits, instantaneous center of rotation and singularities.
- LO6:** Understand tooth gear transmission, compound, planetary gear trains and differentials.
- LO7:** Construct free body diagrams of mechanism links, and derive statics or inverse dynamics equations in matrix-vector form.
- LO8:** Determine mechanism forces and torques using graphical methods.
- LO9:** Simulate mechanism static and/or dynamic forces and torques using computer software.
- LO10:** Use D'Alembert's principle and perform dynamic analysis for planer mechanisms.

# Course Description

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## Assessment Criteria

- Continuous assessment will carry 35% of the total marks.
  - ✓ Labs, Assignments, Quizzes      **20%**
    - ✓ Test 1 – March 1, 2019
    - ✓ Test 2 – April 3, 2019
  - ✓ Midterm Examination      **15%**
- Final Examination      **65%**

<b>Lectures</b>	Wednesday: 8.30 – 10.30	<i>EA2</i>
	Wednesday: 10.30 – 12.30	<i>E106</i>
	Friday: 13.30 – 14.30	<i>E101</i>
<b>Tutorials</b>	Friday: 14.30 – 15.30	<i>E101</i>
<b>Laboratory</b>	<b>Mechanical:</b> Monday 8.30 – 10.30, Friday 10.30 – 12.30 <b>Mechatronics:</b> Monday 15.30 – 17.30, Friday 15.30 – 17.30	<i>Mechanics Laboratory (3<sup>rd</sup> Floor)</i>

# Unit Study Calendar - 2019

Week	Dates	Description	Lecture (hrs.)	Tutorials (hrs.)
1	5-8 Feb	Introduction to Mechanics, commonly employed mechanisms, planer mechanisms, Kinematic Chains and Kinematic Pairs, mechanism mobility using Grubler's criterion	3	1
2	11-15 Feb	Mechanism inversion, types of four bar and slider crank mechanisms, Grahsof's criterion, Introduction to Kinematic analysis. Instantaneous center of rotation, Kennedy's theorem, analysis of velocities, brief introduction to polygon method	3	1
3	18-22 Feb	Mechanics of rigid bodies and planer mechanisms, displacement analysis, relative velocity between two points undergoing planer motion,	3	1
4	25 -1 Mar	Planer Mechanism, special cases of relative velocity expressions, relative acceleration between two points undergoing planer motion	3	Test 1 (Mar 1)
5	4-8 Mar	Analytical Kinematic Analysis of planer mechanisms (Loop closure equation), position, velocity and acceleration representation.	3	1
6	11-15 Mar	Analysis of Four Bar chain, Slider crank mechanism	3	1
7	18-22 Mar	Solution under different input conditions, analytical solution for slider crank inversion,	3	1

# Unit Study Calendar - 2019

Week	Dates	Description	Lecture (hrs.)	Tutorials (hrs.)
8	25-29 Mar	<b>Mid-semester exam</b>		Mid Exam
9	1-5 Apr	Kinematics for Gears	3	1
10	8-12 Apr	Gears, friction gearing, common types of toothed gears, gear geometry, Simple and compound gear trains, planetary gear trains, tabular analysis of planetary gear trains, differentials.	3	1
11	15-19 Apr	<b>New Year Holidays</b>	3	1
12	22-26 Apr	Static force analysis of planer mechanisms, graphical method, Static force analysis, vector approach	3	1
13	29-3 May	Dynamic Analysis of Planer Mechanisms and Virtual work	3	Test 2 (Apr 3)
14	6-10 May	Dynamic Analysis of Planer mechanisms,	3	1
15	13-17 May	Unbalance forces and couples, balancing of rotors.	3	1

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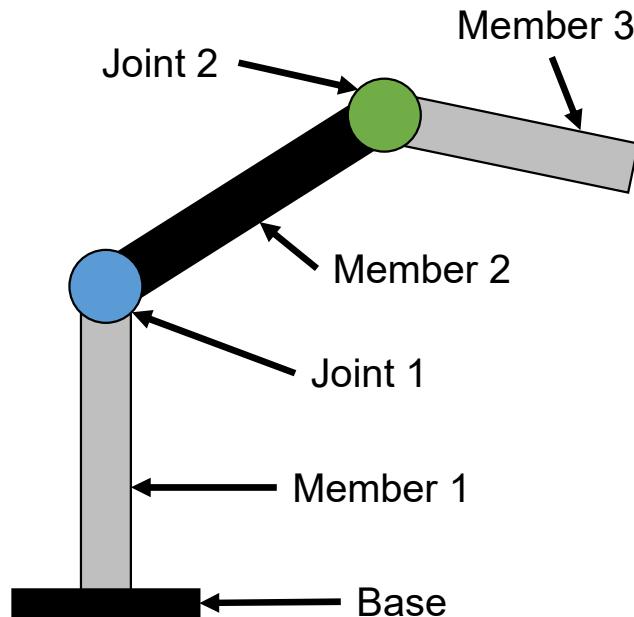
# **Lecture 01:**

# **INTRODUCTION TO MECHANISMS AND KINEMATICS**

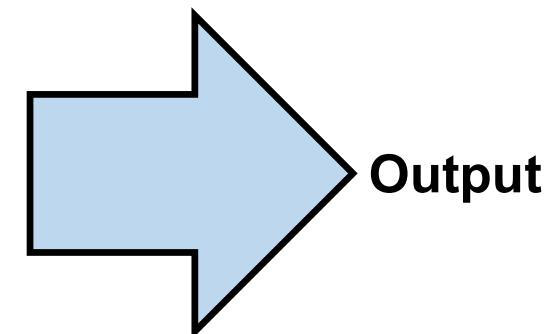
# Introduction

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- Mechanism is a machine composed of several **Members** and **Joints**.

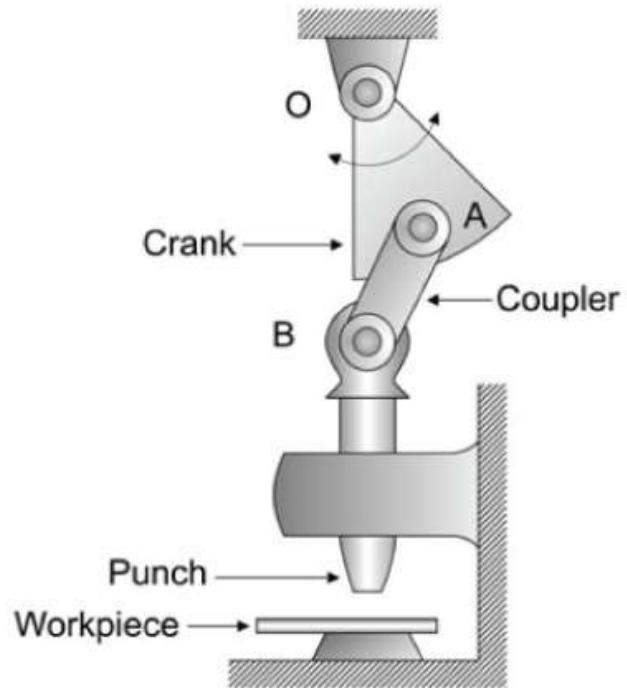


**Power Source**  
1. Motion  
2. Force



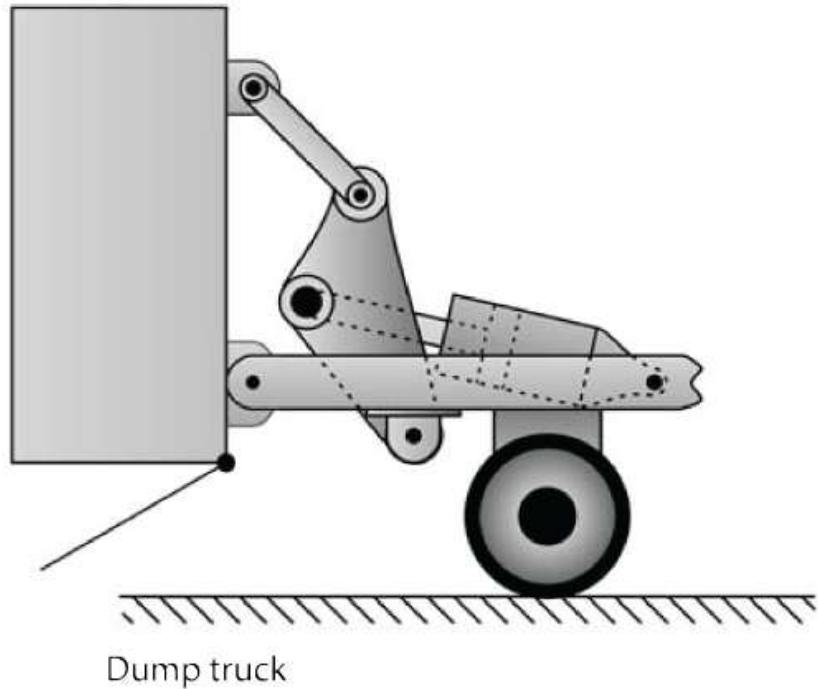
# Example – Punch Mechanism

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# Example – Dump Truck

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# **ME2021 – Mechanics of Machines I**

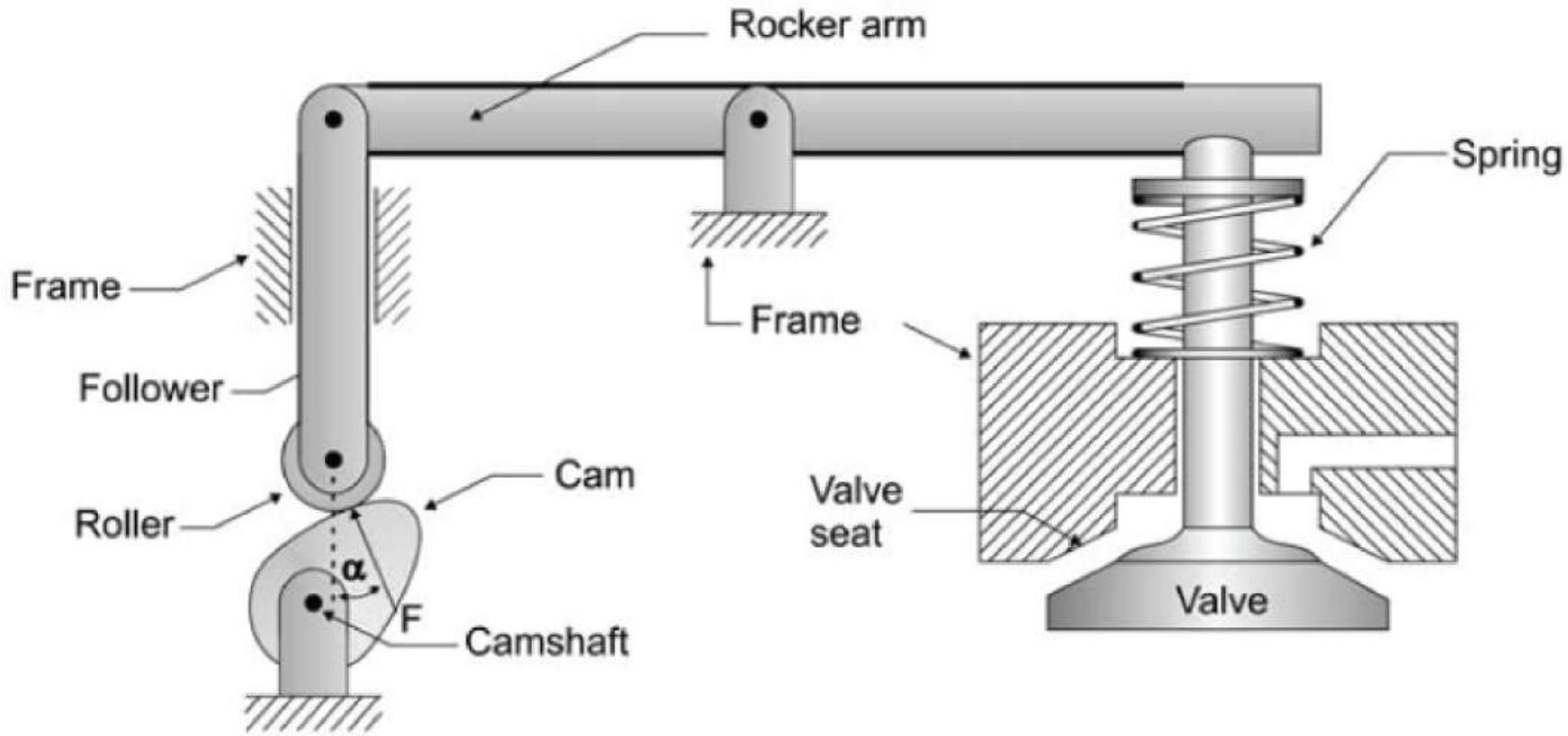
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## **Lecture 02: INTRODUCTION TO MECHANISMS AND KINEMATICS**

**Thilina H. Weerakkody**

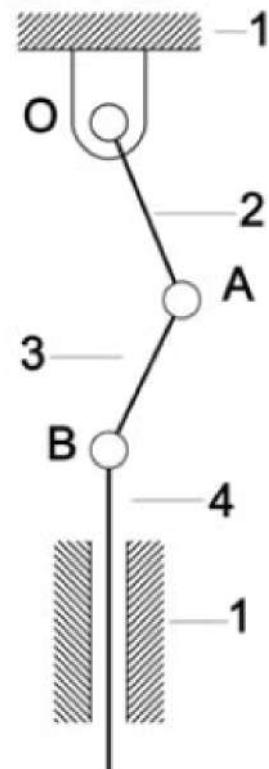
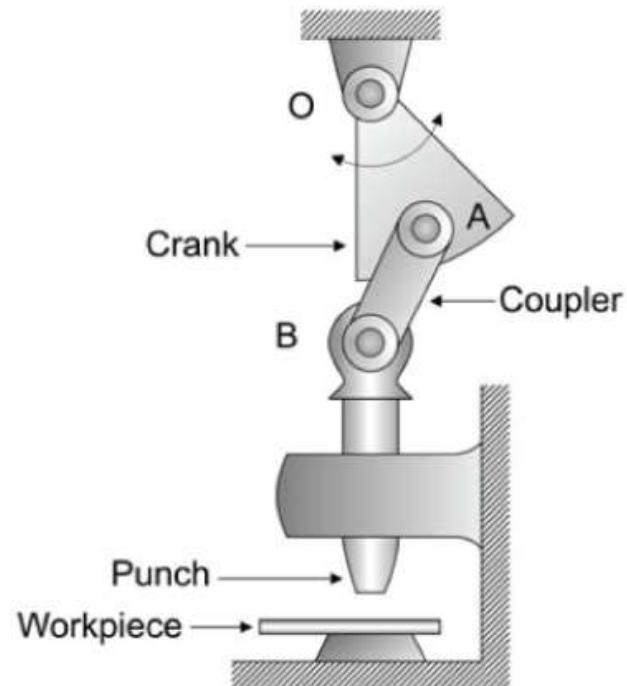
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Department of Mechanical Engineering,  
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# Example – Cam Operating Valve



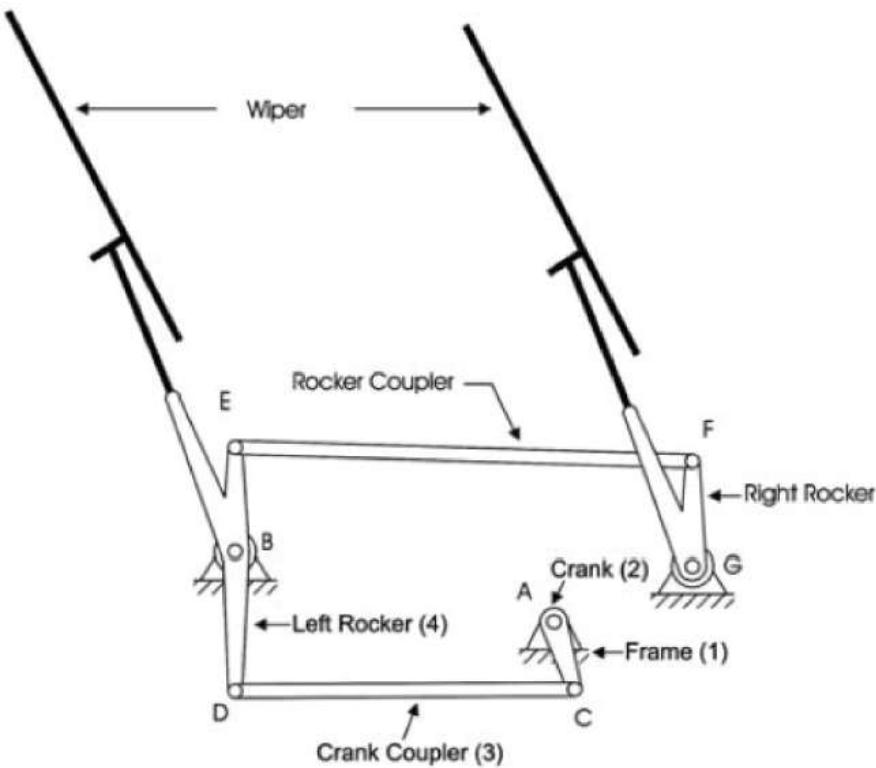
# Example – Punch Mechanism

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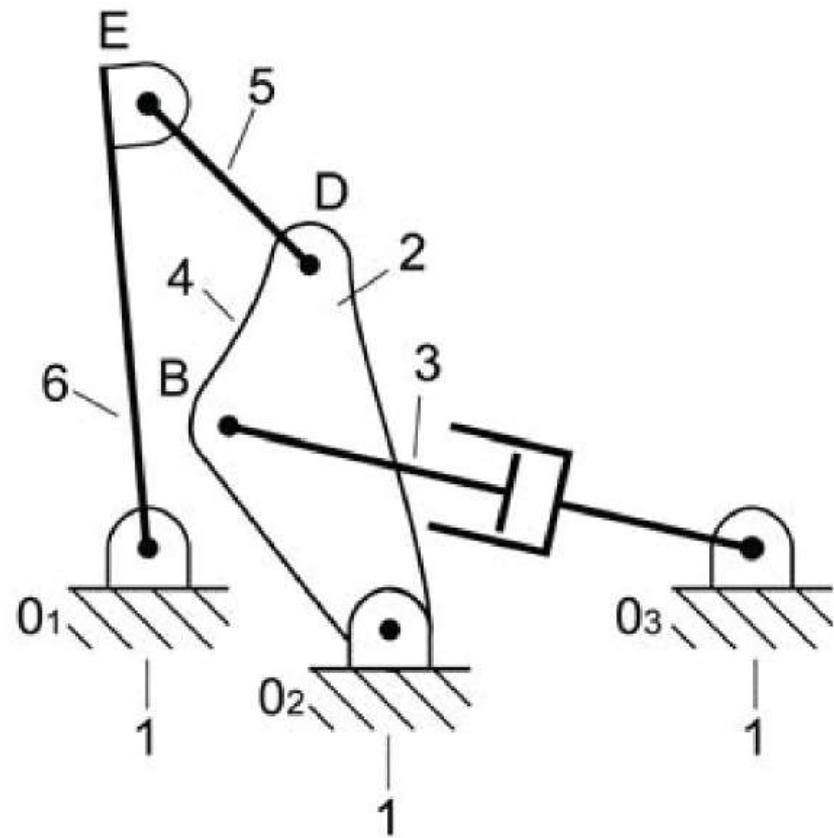
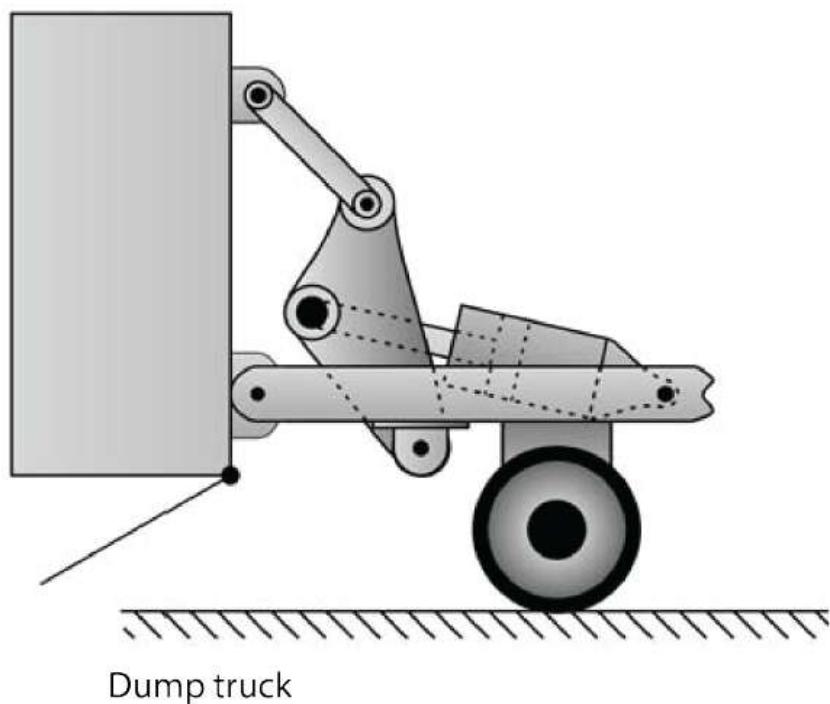
# Example – Windshield wiper mechanism

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# Example – Dump Truck

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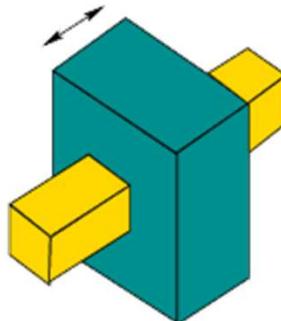


# Lower Pair Joint Types

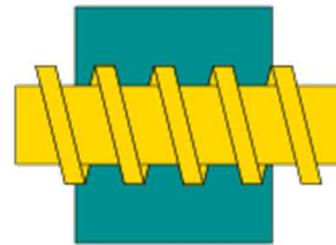
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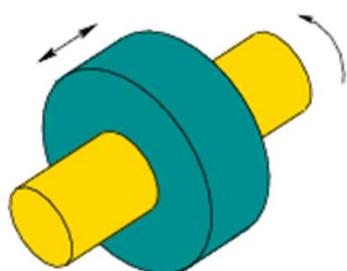
**Revolute**  
1 Degree of Freedom



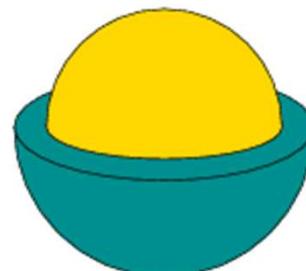
**Prismatic**  
1 Degree of Freedom



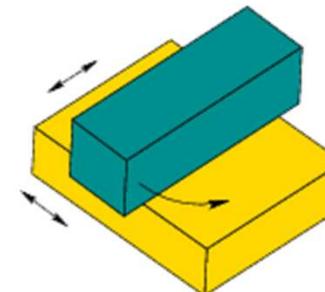
**Screw**  
1 Degree of Freedom



**Cylindrical**  
2 Degrees of Freedom



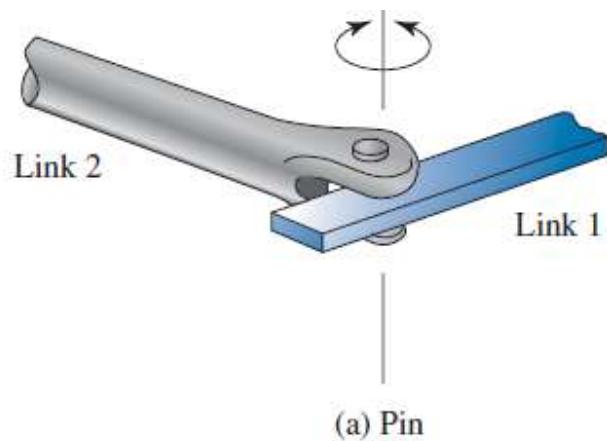
**Spherical**  
3 Degrees of Freedom



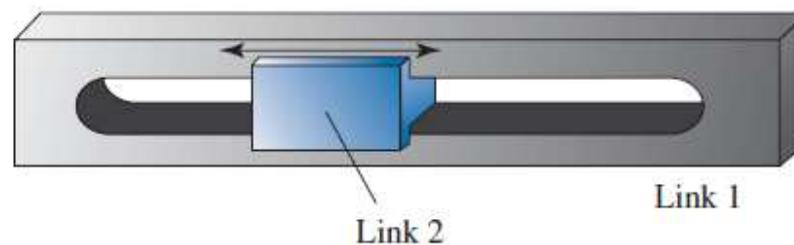
**Planar**  
3 Degrees of Freedom

# Lower Pair Joint Types

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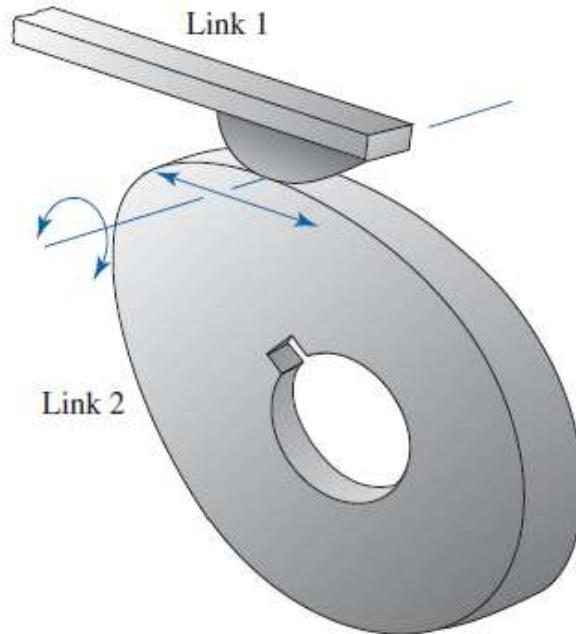
(a) Pin



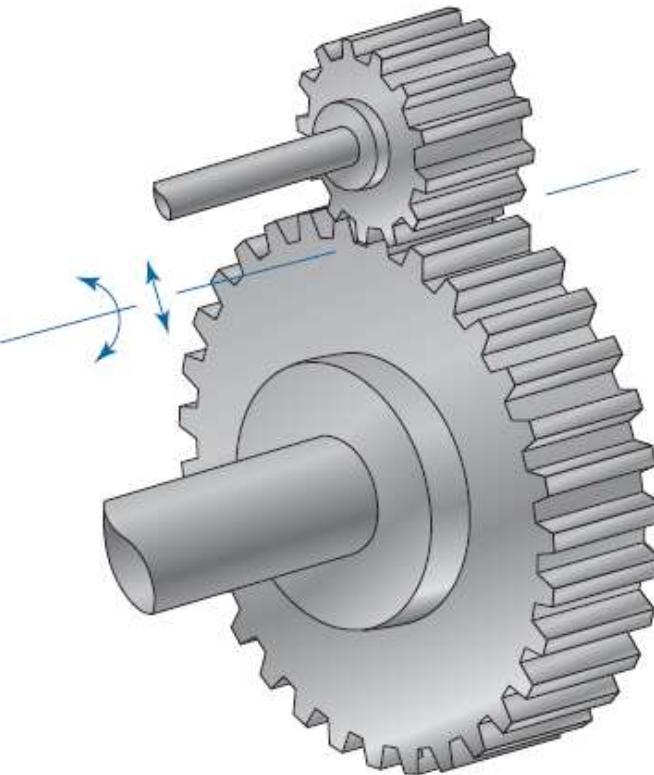
(b) Sliding

# Higher Pair Joint Types

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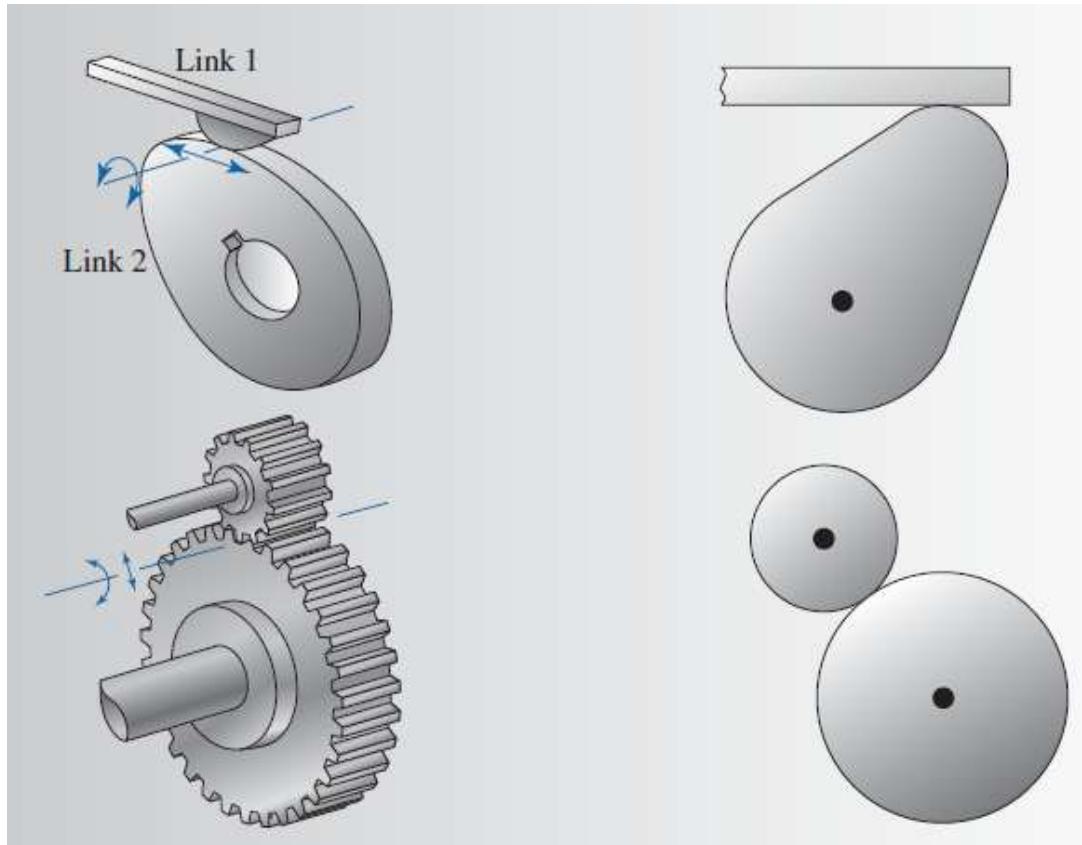
(a) Cam joint



(b) Gear joint

# Higher Pair Joint Types

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# Compound Joint Types

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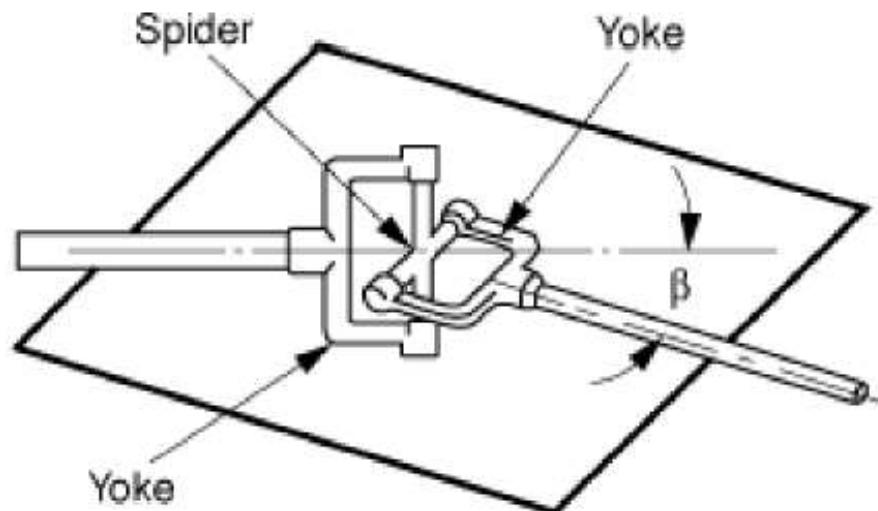
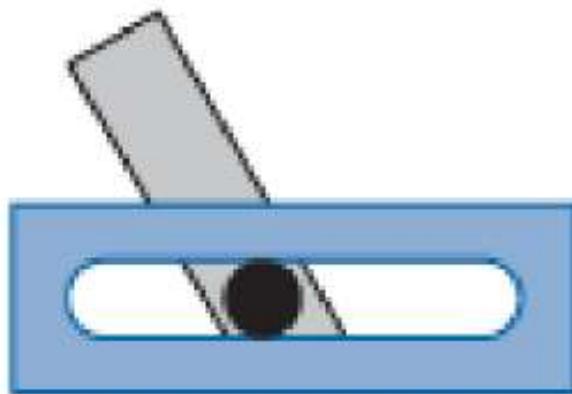


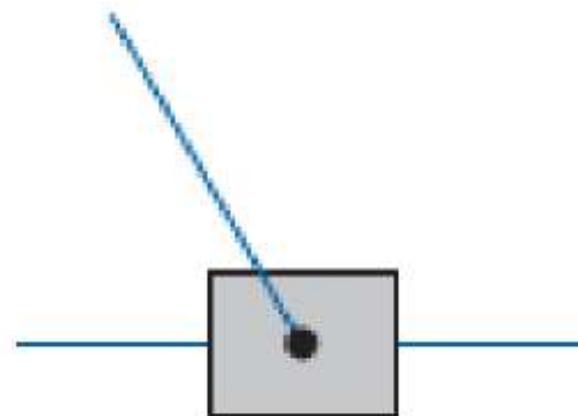
Figure 8: (a) Ball bearing (b) Universal joint

# Compound Joint Types – Pin in a slot

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(a) actual pin in a slot



(a) Compound model

# Compound Joint Types – Screw Joint

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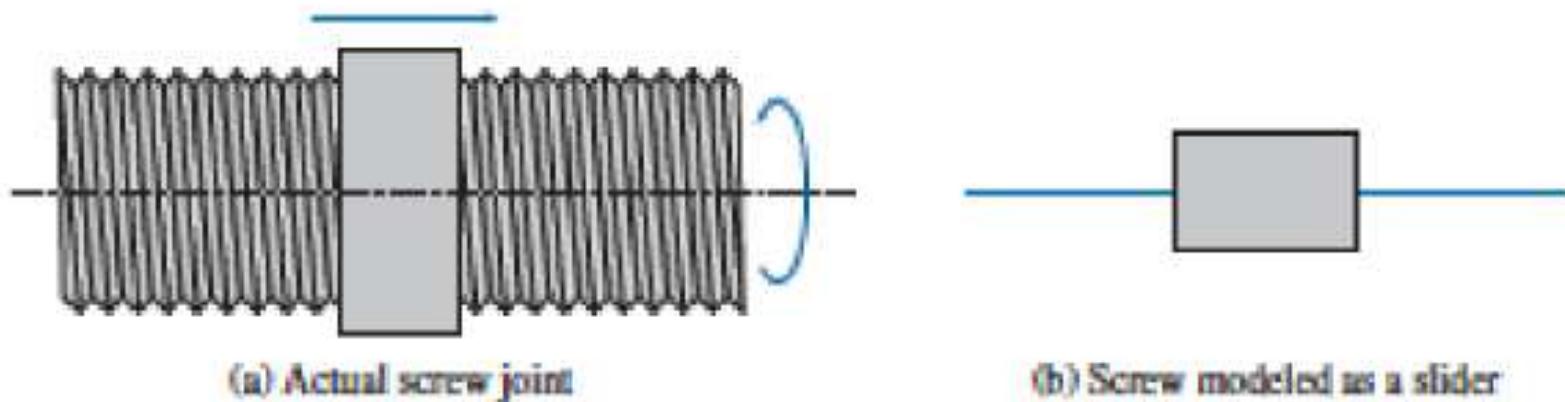
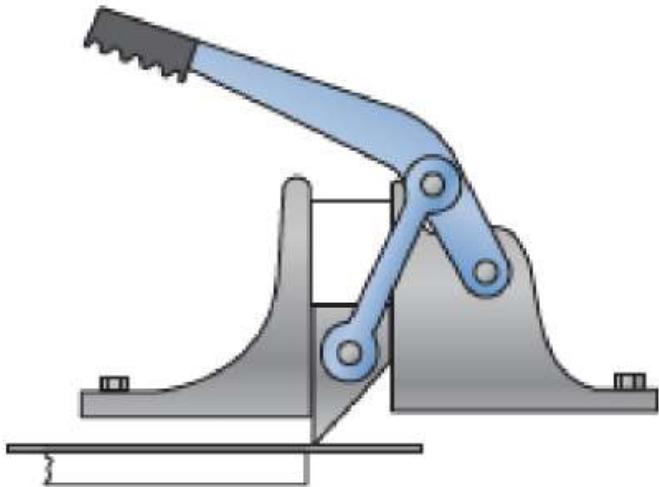


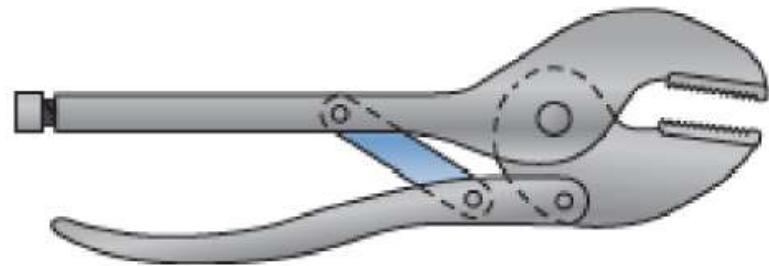
Figure 10: Screw Joint modelled as a sliding joint

# Examples

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(a) Sheer Press



(b) Vice Grip

# Gruebler's Equation

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$$M = 3(n - 1) - 2j_p - j_h$$

*M – Mobility of a planar mechanism*

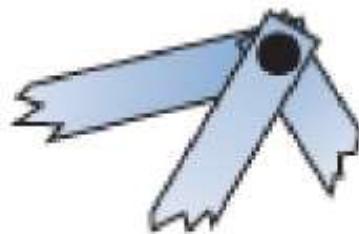
*n – Total No. of links in the mechanism*

*j<sub>p</sub> – Total No. of primary joints (Pivot or sliding)*

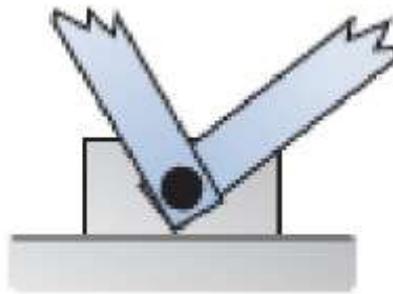
*j<sub>h</sub> – Total No. of higher – order joint (cams or gears)*

# Coincide joints

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(a) Three rotating links

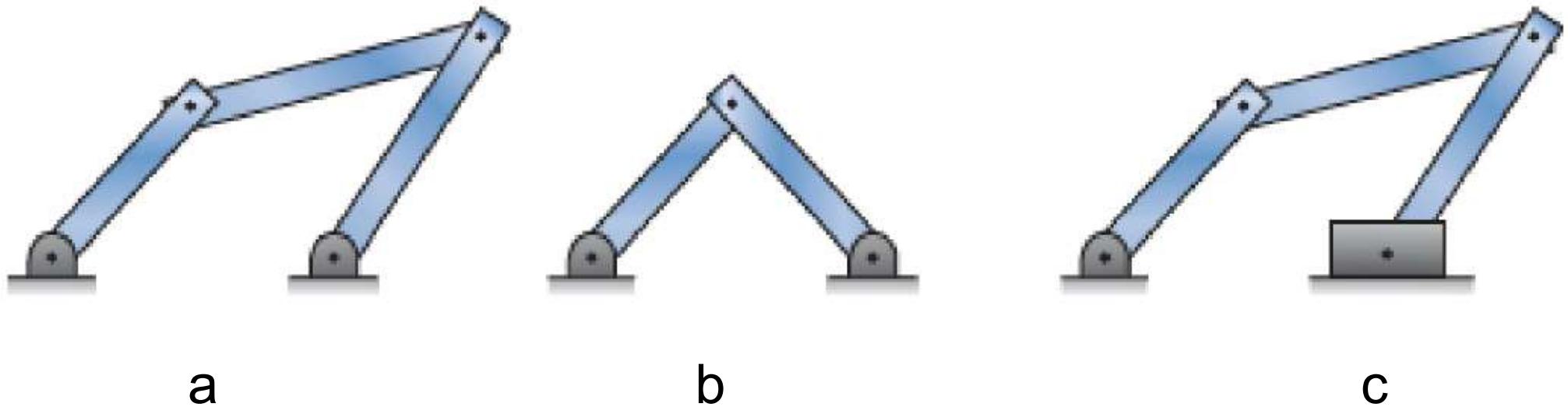


(b) Two rotating and one sliding link

$p$  members      =>       $(p - 1)$  identical joints

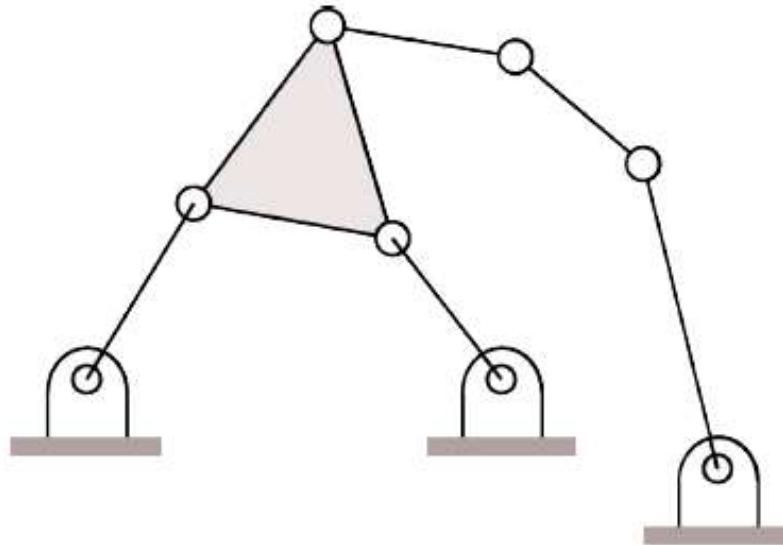
# Examples

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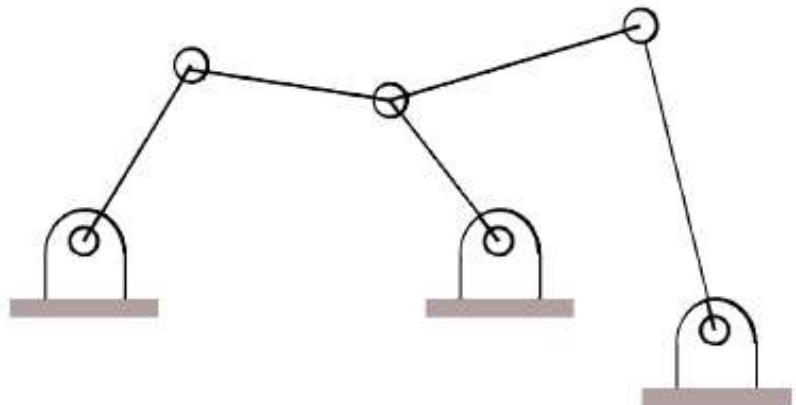


# Examples

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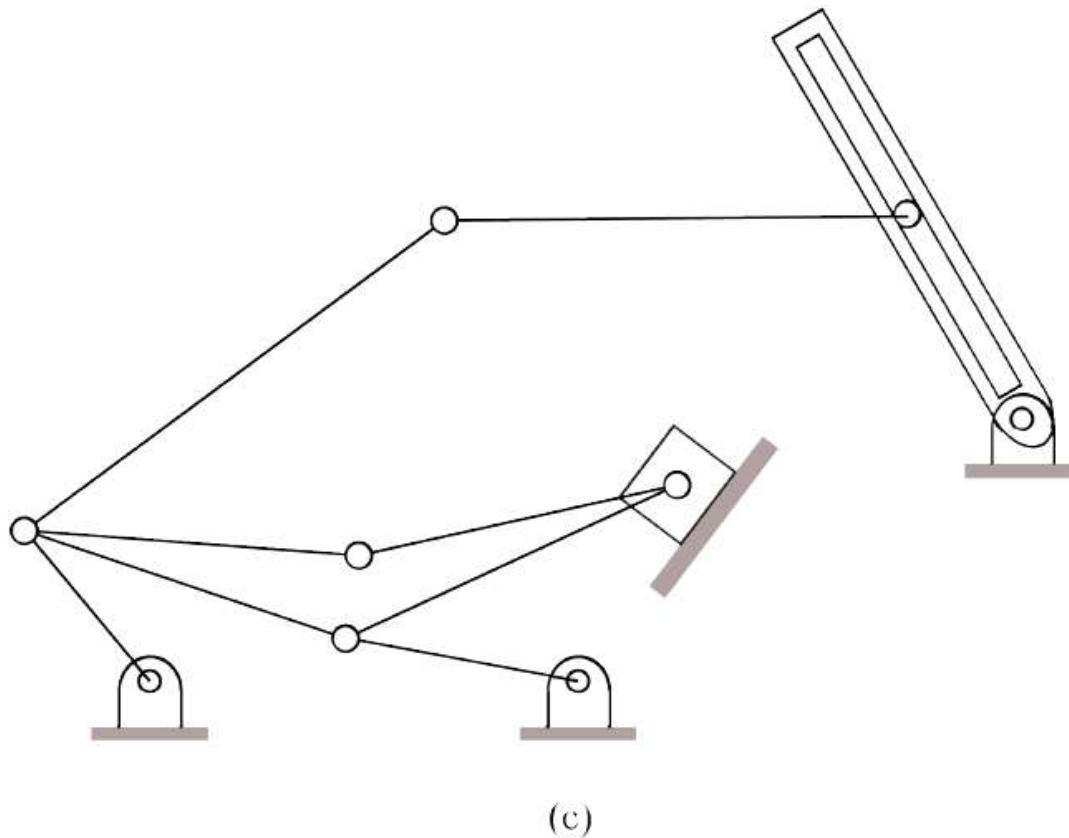
(a)



(b)

# Examples

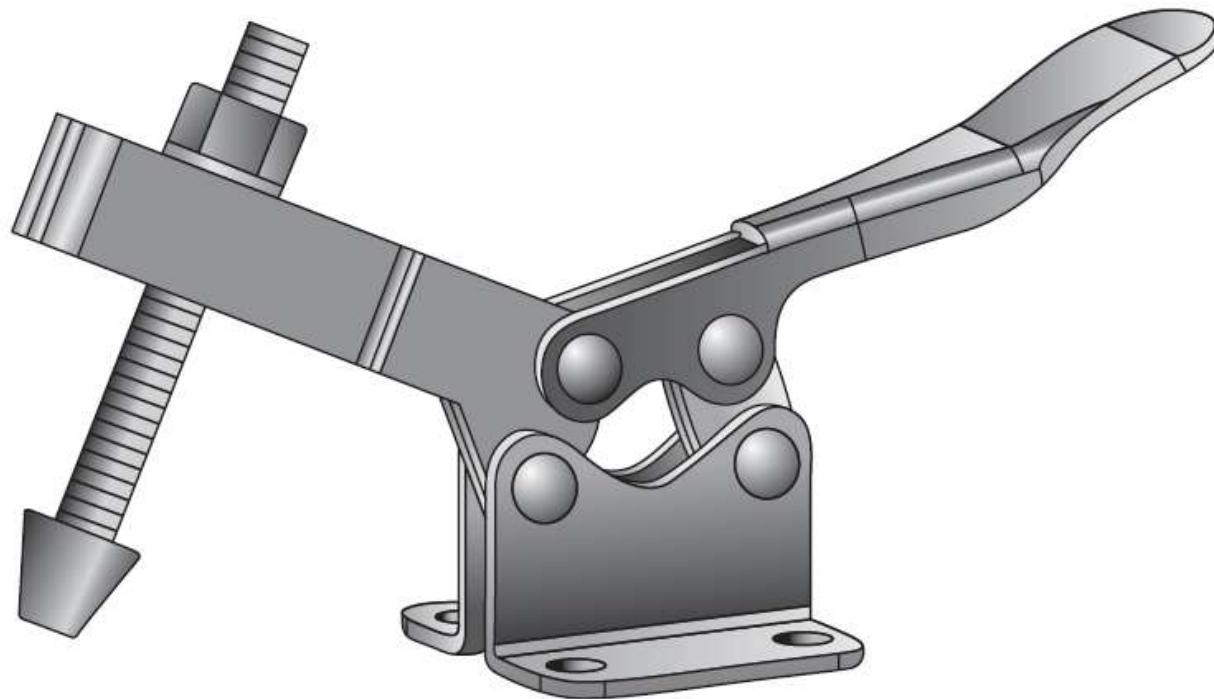
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(c)

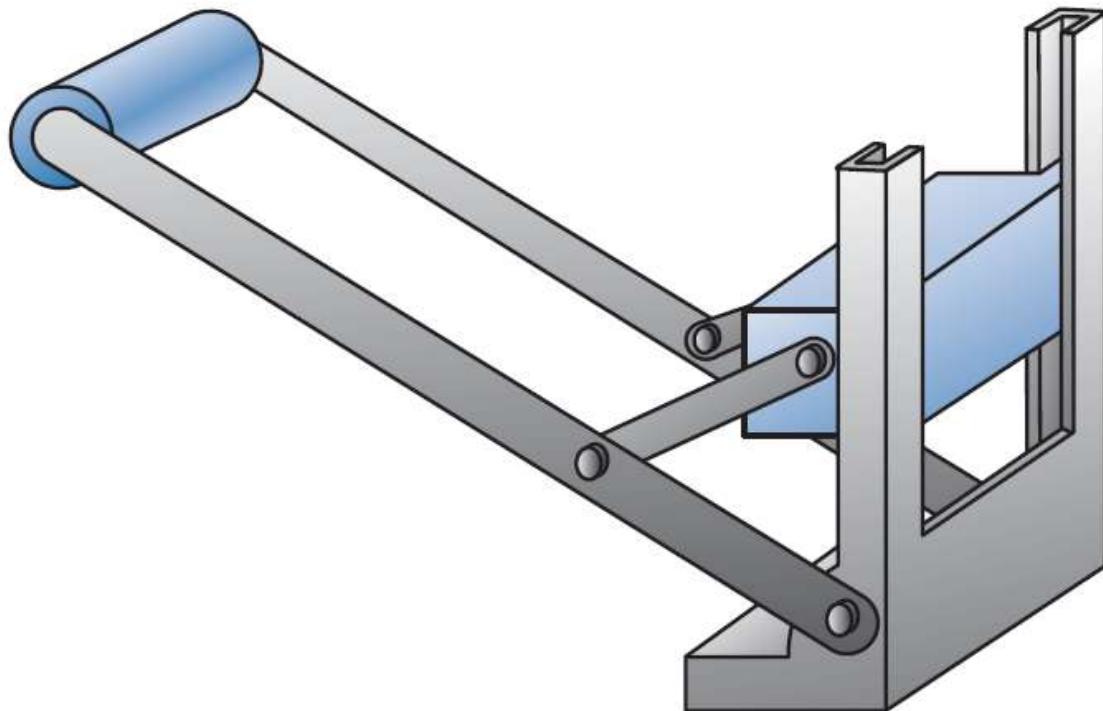
# Examples – Toggle clamp

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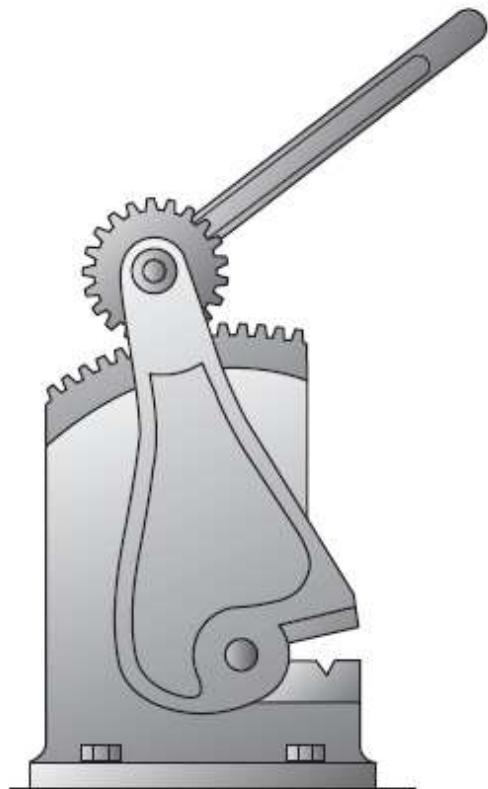
# Examples – Beverage can crusher

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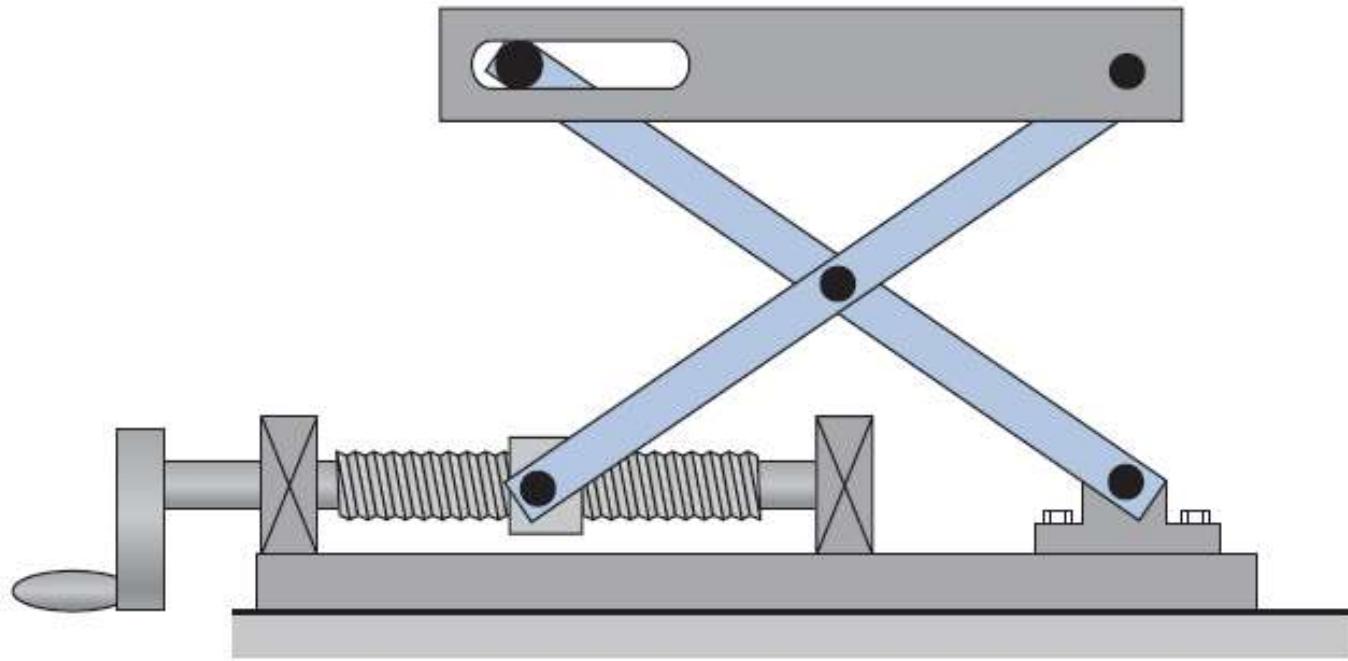
# Examples – Shear Press

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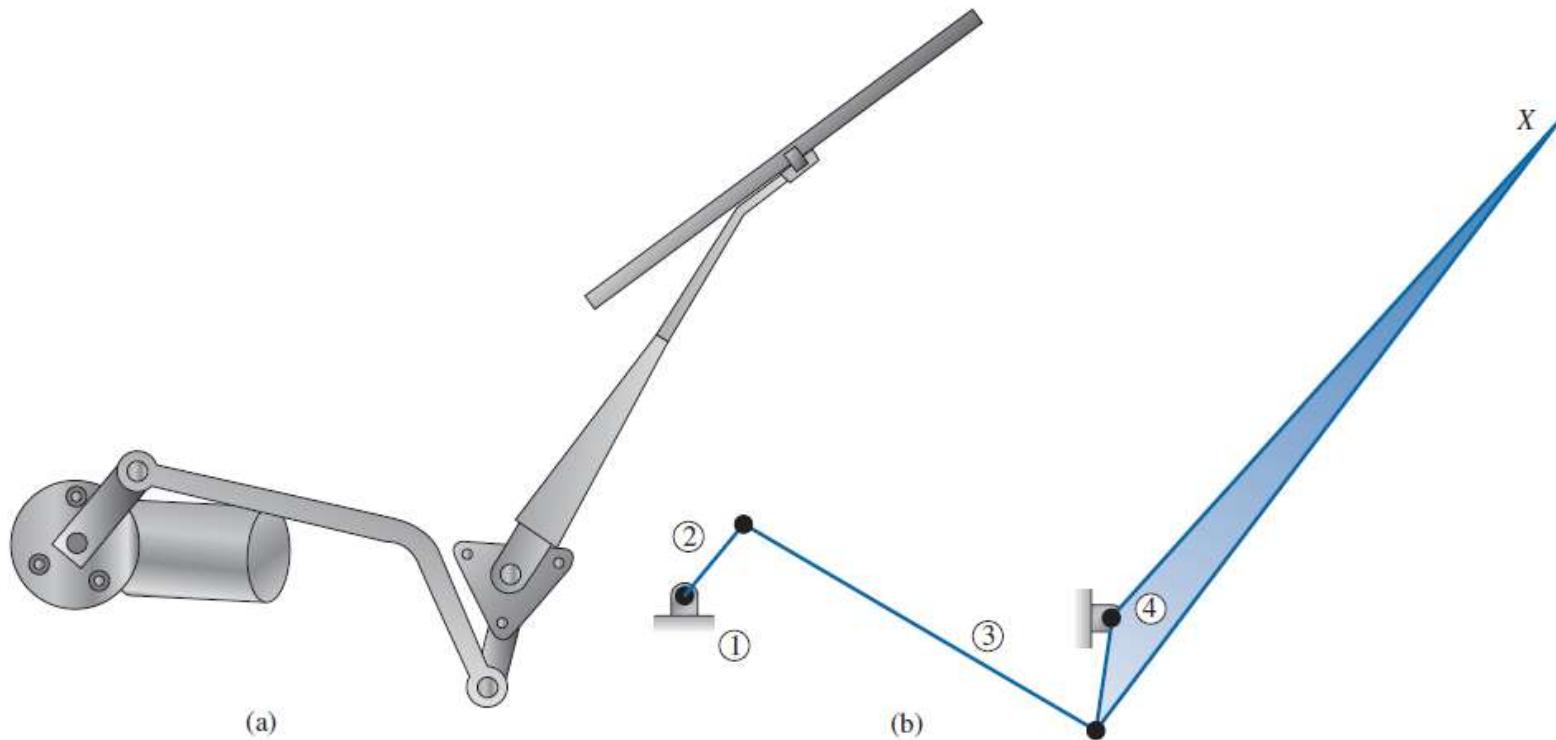
# Examples – Lift Table

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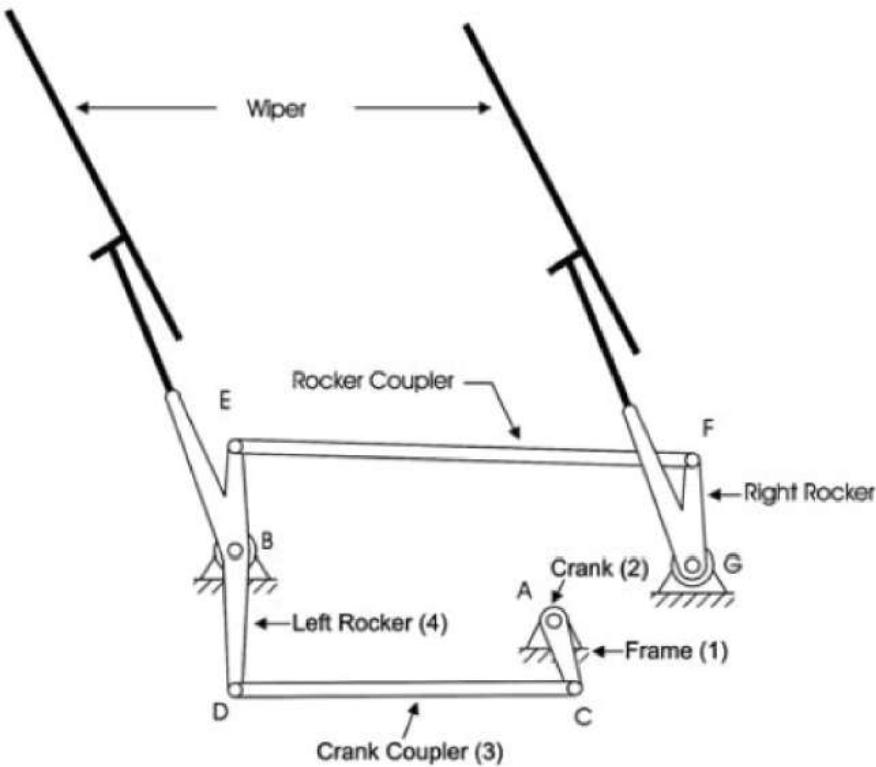
# Examples – Rear Window wiper mechanism

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# Example – Windshield wiper mechanism

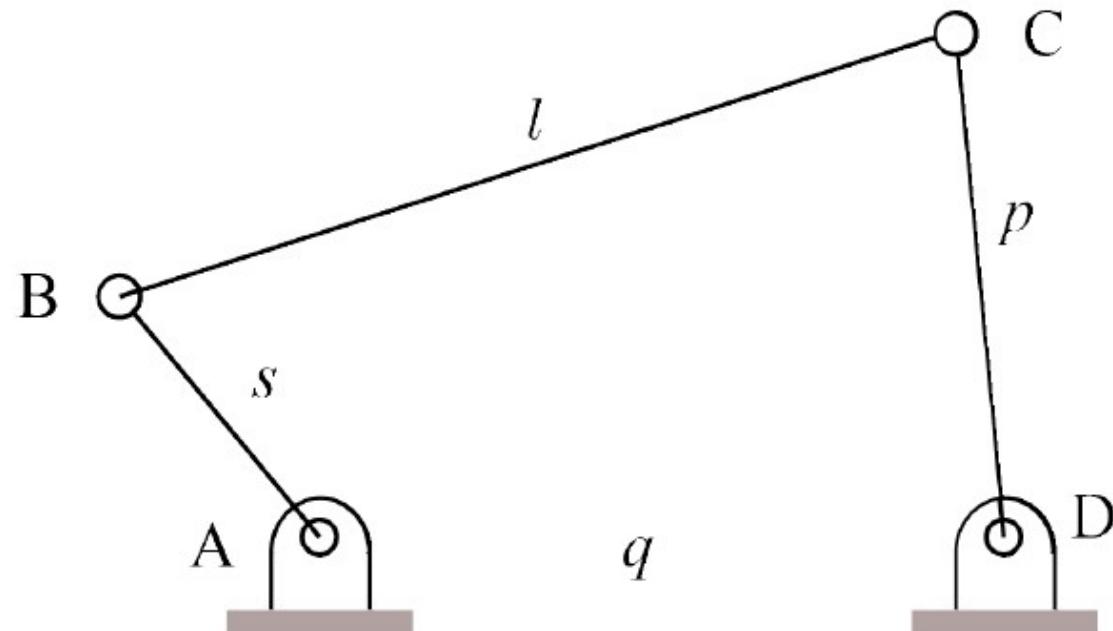
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# Grashof's Criteria

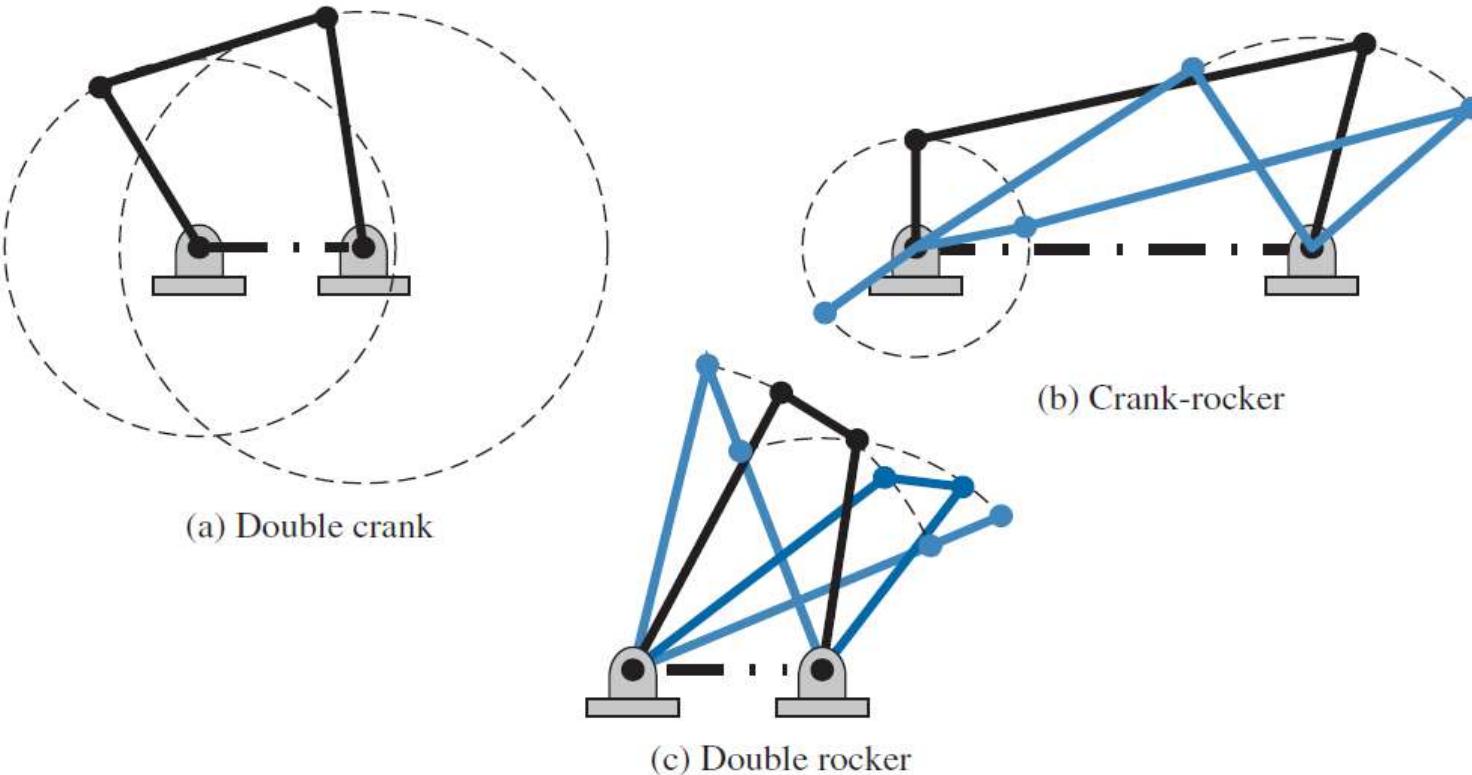
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$$s + l \leq p + q$$



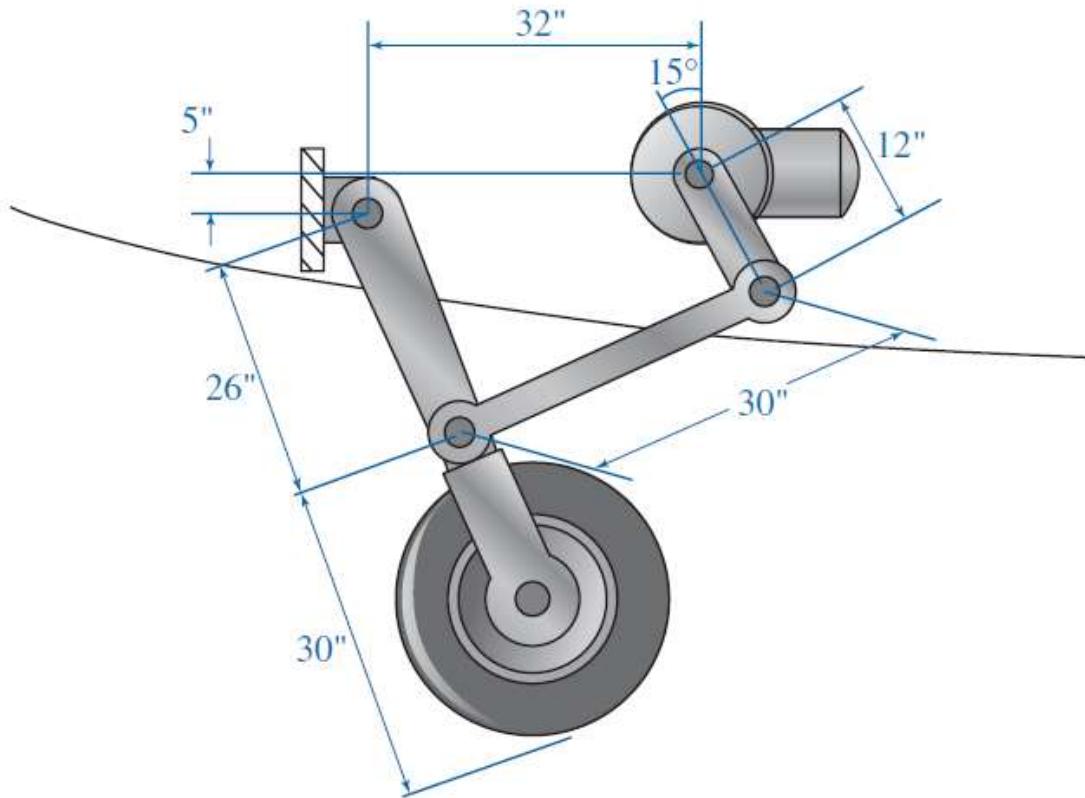
# Grashof Type 1 Linkages

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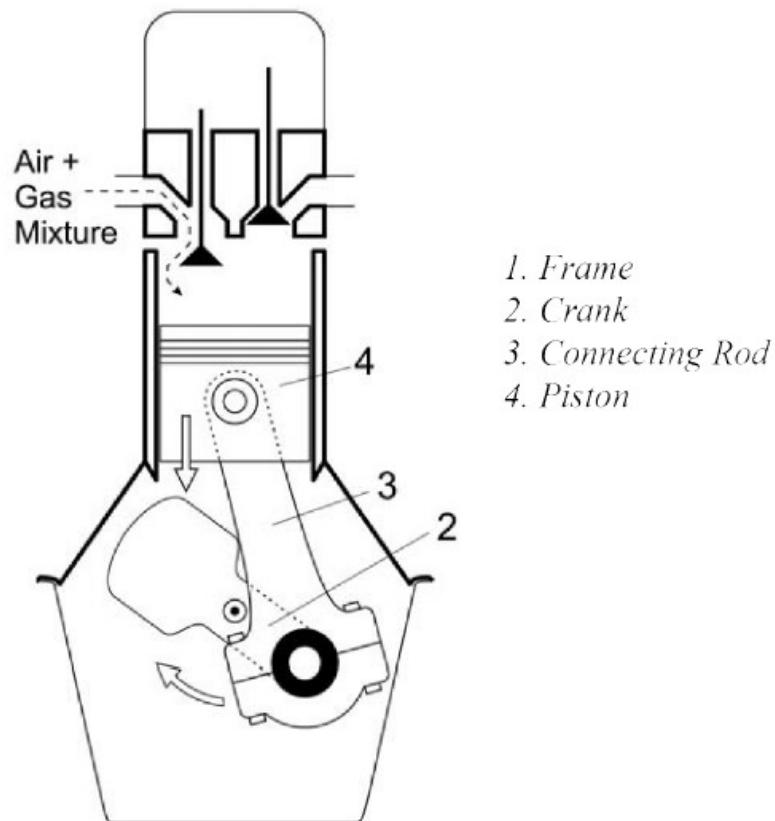
# Nose Wheel Mechanism

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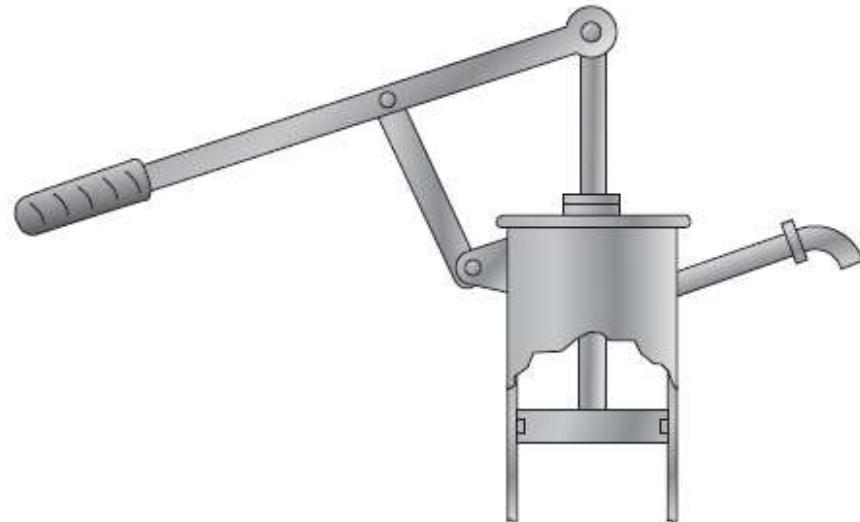
# Slider Crank Mechanism

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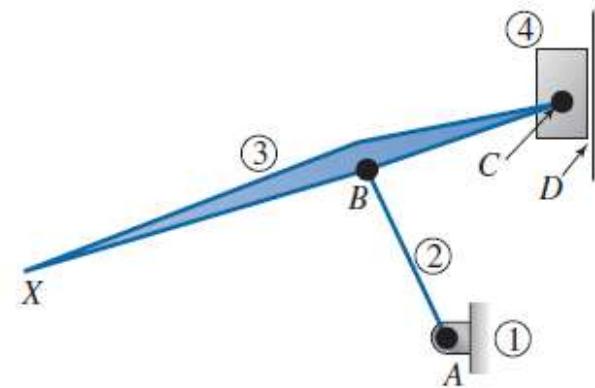


# Manual water pump

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(a)



(b)

# Recommended Text

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- *Waldron, K.J., and Kinzel, G.L., “Kinematics, Dynamics, and Design of Machinery”, 3rd edition, Wiley.*
- *W.L. Cleghorn, “Mechanisms and Machines” 2<sup>nd</sup> edition, Oxford University Press, 2015.*
- *John J. Uicker, Gordon R. Pennock and Joseph E. Shigley, “Theory of Machines and Mechanisms”, Oxford University Press*