Trial Solution Method Complementary Solution Particular Solution Apply Initial Conditions

Ordinary Differential Equations - Lecture 3

ME3001 - Mechanical Engineering Analysis

Mechanical Engineering

Tennessee Technological University

Trial Solution for Second Order ODEs



Lecture 3 - Trial Solution for Second Order ODEs:

- Trial Solution Method
- Complementary Solution
- Particular Solution
- Apply Initial Conditions

Trial Solution Method

Use the trial solution method to solve the ODE.

This is an **analytical** method that you learned in calculus but it may have been called something different. In the Zill book it is called *Homogenous Linear ... Constant Coefficients* (4.3-4.4).

$$a_2y'' + a_1y' + a_0y = f(x)$$

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Trial Solution Method

Complementary Solution

<u>Step 1</u> - Find the **complementary part** of the solution from the left hand side of the ODE alone (LHS=0).

$$a_2y'' + a_1y' + a_0y = f$$
 \rightarrow $a_2y'' + a_1y' + a_0y = 0$

Assume an exponential solution for the complementary part.

$$y_{complementary} = y_c(t) =$$

Substitute this solution into the ODE (LHS=0).

Complementary Solution

Particular Solution

Step 2 - Find the **particular part** of the solution from the entire equation $\overline{(LHS=RHS)}$.

$$a_2y'' + a_1y' + a_0y = f$$

The form of the particular part follows the RHS of the ODE.

$$y_{particular} = y_p(t) =$$

Substitute this solution into the ODE above and solve for any unknown constants in $y_p(t)$.



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Particular Solution

Apply Initial Conditions

Step 3 - Now combine the **complementary** and **particular** solutions through *superposition*.

$$y(x) = y_c(x) + y_p(x) =$$

The ODE is first order and we have _____ unknown. Coincidence?

$$y(x) =$$

This **initial value problem** requires _____ intial condition.

Apply Initial Conditions

$$v(x = 0) =$$

$$y(x = 0) =$$
$$y'(x = 0) =$$

Apply Initial Conditions

What does the solution look like this time?

