

Module 3 - Systems of Linear Equations

ME3001 - Mechanical Engineering Analysis

Mechanical Engineering

Tennessee Technological University

Topic 1 - Linear Algebra Review

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- What is a Linear Equation ?
- General Form of A Linear System
- The Geometrical Explanation
- Examples in MATLAB

What is a Linear Equation ?

What is a Linear Equation

- “A linear equation is an algebraic equation in which each term is either a constant or the product of a constant and a single variable” - Wikipedia
- slope intercept form
- does not contain

What is a System of Linear Equations?

- multiple linear equations with...
- also known as...

General Form of A Linear System

The general system of linear equations is shown with variables $x_{1,2,...,n}$, coefficients $a_{11,12,...,nm}$, and knowns $b_{1,2,...,m}$

$$a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n = b_1$$

$$a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n = b_2$$

.

$$a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mn}x_n = b_m$$

The equations are cast into matrix form of the system.

$$\begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ & . & & \\ & . & & \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} \times \begin{bmatrix} x_1 \\ x_2 \\ . \\ . \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ . \\ . \\ b_m \end{bmatrix}$$

The Geometrical Explanation

Consider the intersection of 2 Lines. Begin with the XY plane (2D).
 $ax+by=c$

- 1 Write the individual equations.