In-Class Activity 8 - Catenary Cable

ME 3001-002- Mechanical Engineering Analysis - Spring 2024

Learning Objectives:

- Demonstrate generating an functional description to fit numnerical data
- Demonstrate using a user tool compared to a built in tool
- Practice using plotting in MATLAB to display graphical results

Peer Collaboration:

This is an individual assignment, but you are encouraged to discuss the problem with your peers. You must write your own program and submit as an individual, but you can share ideas about the algorithm with your peers and the instructor.

Overview:

Consider a flexible steel cable attached to ground at both ends as shown in the image. The physical properties of the cable are known.

The hanging cable (catenary cable) can be represented by and unknown function y(x).

The following displacement measurements we made through visual inspection of a physical system.



Physical Properties:

Total Mass of Cable (not chain shown in image)

$$W = .048(kg)$$

Total Length of Cable

$$L = 147(in)$$

Boundary Conditions:

$$y(x = 0) = 12, \ y'(x = 0) = 0$$

$$y(x = -L/2) = y(x = L/2)$$

Measured Data:

x(in)	0	12	24	36	48	60
y(in)	12	13	16	23	33	48

Activity:

Write a MATLAB program to approximate the displacement function of the catenary cable y(x) using a curve fit model of your choice. Two methods will be used to generate the curve.

- 1. The numerical data should be hardcoded into the program, and the program should run without using user input.
- 2. Generate a curve fit function $y_1(x)$ to fit the data points with a model of your choice using the built-in MATLAB function polyfit() or other MATLAB curve fitting tool. You may need to install the MATLAB Curve fitting Toolbox.
- 3. Generate a second curve fit function $y_2(x)$ to fit the data points with a model of your choice using a custom MATLAB program. Suggested methods are Lagrange polynomials or polynomials as linear systems. Clearly state if the model for is different from the model used in part 2.
- 4. Show the numerical data and both curve fits on the same figure. Use grid lines and label the axes.
- 5. Bonus: Find an analytical solution to the problem using the physical properties and boundary conditions. Show all steps, and include a reference if applicable. Add the analytical curve to the results figure from part 3. Does the solution agree with the measured data?

Submission:

- Submit the MATLAB program as a .m file. The program should run free from errors and produce the results described in the assignment including any figure.
- Include answers to any discussion questions in a seperate document or the assignment submission textbox.