Module 7 - Damping Elements

ME3050 - Dynamics Modeling and Controls

Mechanical Engineering
Tennessee Technological University

Topic 3 - Mass Spring Damper Model



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- Standard Model Form
- Engineering Applications
- Example: Automobile Suspension

Standard Model Form

The EOMs we have derived can be represented in the following standard form.

$$a_n \frac{d^n}{dt^n} x(t) + a_{n-1} \frac{d^{n-1}}{dt^{n-1}} x(t) + \dots + a_2 \frac{d^2}{dt^2} x(t) + a_1 \frac{d}{dt} x(t) + a_0 x(t) = f(t)$$

- ullet The dependent variable x and its derivatives depend on t.
- The coefficients a_n through a_0 are functions of the physical parameters in the system.
- The function f(t) is called the _____
- The system is linear if ...



Standard Model Form

In solid mechanics and dynamics the standard form of the model becomes the generalized mass spring damper model.

$$a_n x^{(n)} + a_{n-1} x^{(n-1)} + \dots + a_2 x'' + a_1 x' + a_0 x = f(t)$$

$$\rightarrow$$
 $m\ddot{x} + c\dot{x} + k\dot{x} = f(t) \rightarrow M\ddot{x} + C\dot{x} + K\dot{x} = f(t)$

This is a fundamental equation that we will investigate throughout the rest of the semester.



Engineering Applications

The mass spring damper model can be applied to most mechanics problems.

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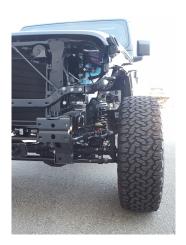
Example: Automobile Suspension



Newton's Second Law Approach

- Draw a Free Body Diagram
- Make an assumption of motion
- Determine all forces acting on the system and their directions.
- Write Newton's second law for the appropriate DOF.
- Re-write the ODE in the standard form of a system equation.

Example: Automobile Suspension - Steps 1,2 and 3



Example: Automobile Suspension - Steps 4,5

Standard Model Form Engineering Applications Example: Automobile Suspension Standard Model Form Engineering Applications Example: Automobile Suspension