

Module 13 - Higher Order Systems

ME3050 - Dynamics Modeling and Controls

Mechanical Engineering

Tennessee Technological University

Topic 1 - Deriving the 2DOF Model

Topic 1 - Deriving the 2DOF Model

- Motivation - Physical Models
- Model Description
- Newton's Approach
- Equation of Motion

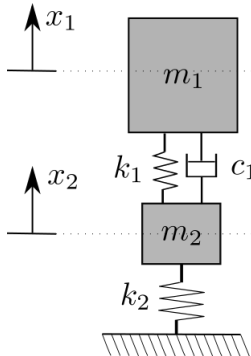
Motivation - Physical Models

Higher Order Models - Mechanical systems involve the interactions between multiple rigid bodies. This can be seen in many examples.

- Automobile Suspension
- Beam Deflection (FEA)
- Tether Based Space Travel
- Virtually Everything!

Motivation - Physical Models

Automobile Suspension - This is a common approximation of a typical automobile suspension known as the *quarter car model*.

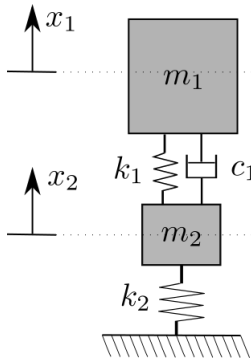


Is this valid?

Why? Why Not?

What does the
response look like?
How can you find
out?

Model Description

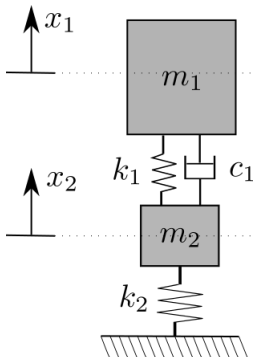


List Assumptions:

-
-
-

Newton's Approach

Draw one free body diagram for each body.



Newton's Approach

Write Newton's Second Law for each body.

Equation of Motion

Equation of Motion

Equation of Motion for Mass 1:

$$m_1 \ddot{x}_1 + c_1(\dot{x}_1 - \dot{x}_2) + k_1(x_1 - x_2) = 0$$

Equation of Motion for Mass 2:

$$m_2 \ddot{x}_2 + k_2 x_2 - c_1(\dot{x}_1 - \dot{x}_2) - k_1(x_1 - x_2) = 0$$

It is common to write the equations of motion as a matrix equation. If you are unsure if you have the correct form just multiply it out and should match.

Equation of Motion

matrix form of the equations of motion:

References

- System Dynamics, Palm III, Third Edition - Chapter 4 - Spring and Damper Elements in Mechanical Systems - pg. 208