Module 13 - Higher Order Systems

ME3050 - Dynamics Modeling and Controls

Mechanical Engineering
Tennessee Technological University

Topic 1 - Deriving the 2DOF Model

Topic 1 - Deriving the 2DOF Model

- Motivation Physical Models
- Model Description
- Newton's Approach
- Equation of Motion

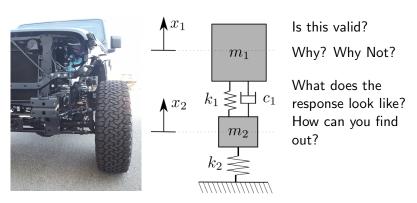
Motivation - Physical Models

Higher Order Models - Mechanical systems involve the interactions between multiple rigid bodies. This can be seen in many examples.

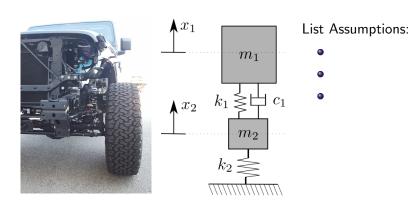
- Automobile Suspension
- Beam Deflection (FEA)
- Tether Based Space Travel
- Virtually Everything!

Motivation - Physical Models

Automobile Suspension - This is a common approximation of a typical automobile suspension known as the *quarter car model*.

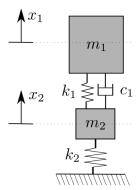


Model Description



Newton's Approach

Draw one free body diagram for each body.



Newton's Approach

Write Newton's Second Law for each body.

Equation of Motion

Equation of Motion

Equation of Motion for Mass 1:

$$m_1\ddot{x}_1 + c_1(\dot{x}_1 - \dot{x}_2) + k_1(x_1 - x_2) = 0$$

Equation of Motion for Mass 2:

$$m_2\ddot{x}_2 + k_2x_2 - c_1(\dot{x}_1 - \dot{x}_2) - k_1(x_1 - x_2) = 0$$

It is common to write the equations of motion as a matrix equation. If you are unsure if you have the correct form just multiply it out and should match.

References

• System Dynamics, Palm III, Third Edition - Chapter 4 - Spring and Damper Elements in Mechanical Systems - pg. 208