Lecture Module - Time Varying Circuits

Mechanical Engineering
Tennessee Technological University

Topic 2 - First Order Systems

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General System Model

• Mechanical-Electrical Analogies

• Example: RC Circuit

Example: Bulb Thermometer

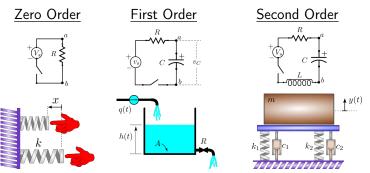
General System Model

The behavior of a circuit is dependent on time, and many common circuits can be represented by a *linear ordinary differential equation* which can be written in the following standard form.

$$a_n \frac{d^n x}{dt^n} + a_{n-1} \frac{d^{n-1} x}{dt^{n-1}} + \dots + a_2 \frac{d^2 x}{dt^2} + a_1 \frac{dx}{dt} + a_0 x = f(t)$$

Mechanical-Electrical Analogies

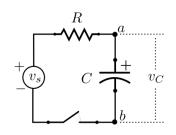
Many mechanical systems are also time dependent, or *dynamic* and a mechanical-electrical analog is often draw between the two.



This concept was used for analysis and simulation.

Example: RC Circuit

The RC circuit is a first order system. The response to a step input v_s is exponential which is described a single parameter the time constant τ .



First Order Model

Response Equation

Example: RC Circuit

time(s)	response(V)



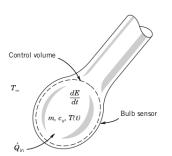
Example: Bulb Thermometer

Consider the bulb thermometer shown which can be modeled as a first order system. Where does the *model* come from?

$$\frac{dE}{dt} = \dot{Q}$$

$$\frac{dE}{dt} = mc_v \frac{T(t)}{dt}$$

$$\dot{Q} = hA_s\Delta T$$

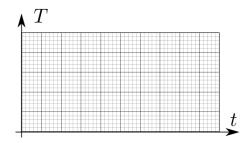


First Order Model

Response Equation

Example: Bulb Thermometer

time(s)	response(°C)



Example: Bulb Thermometer

Think about the general system model.

What is the time constant of the bulb thermometer system?

 $\tau =$

What is the static sensitivity? What are the units?