General System Model Mechanical-Electrical Analogies Example: RC Circuit Activity: Bulb Thermometer

#### Lecture Module - Time Varying Circuits

Mechanical Engineering
Tennessee Technological University

Topic 2 - First Order Systems

#### Topic 2 - First Order Systems

- General System Model
- Mechanical-Electrical Analogies
- Example: RC Circuit
- Activity: Bulb Thermometer

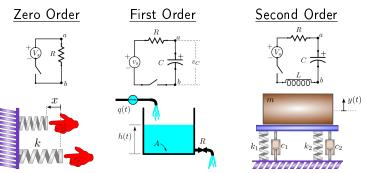
# General System Model

The behavior of a circuit is dependent on time, and many common circuits can be represented by a *linear ordinary differential equation* which can be written in the following standard form.

$$a_n \frac{d^n x}{dt^n} + a_{n-1} \frac{d^{n-1} x}{dt^{n-1}} + \dots + a_2 \frac{d^2 x}{dt^2} + a_1 \frac{dx}{dt} + a_0 x = f(t)$$

#### Mechanical-Electrical Analogies

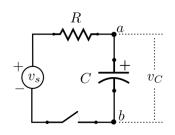
Many mechanical systems are also time dependent, or *dynamic* and a mechanical-electrical analog is often draw between the two.



This concept was used for analysis and simulation.

# Example: RC Circuit

The RC circuit is a first order system. The response to a step input  $v_s$  is exponential which is described a single parameter the time constant  $\tau$ .



First Order Model:

Response Equation:

# Example: RC Circuit

time(s)	response(V)

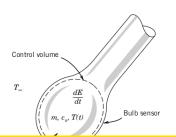


### Activity: Bulb Thermometer

Activity: This should be completed by each student as an individual. You are encouraged to discuss with your peers.

Consider the bulb thermometer shown which can be modeled as a first order system. Write the system model and the expected reponse.

$$\frac{dE}{dt} = \dot{Q} \qquad \qquad \frac{dE}{dt} = mc_v \frac{T(t)}{dt} \qquad \qquad \dot{Q} = hA_s \Delta T$$



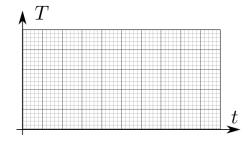
First Order Model:

Response Equation:

## Activity: Bulb Thermometer

Activity: Fill out the table below and sketch a graph to represent the data.

time(s)	response(°C)
0	
1 au	
2 au	
$3\tau$	
$4\tau$	



## Activity: Bulb Thermometer

Activity: Answer the following questions.

(hint: Think about the general system model.)

What is the time constant of the bulb thermometer system?

 $\tau =$ 

What is the static sensitivity? What are the units?