# ME3023 Lecture - Chapter 4

# **Probability and Statistics**

Theory and Design for Mechanical Measurements

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#### • 4.1 - Introduction

Who has taken a statistics class before? In college? In high-school?

What does probability and statistics have to do with mechanical engineering?

For a given set of measurements we want to quantify...

- a representative value that characterizes the average of the measured data set
- a representative value that provides a measure of the variation in the data set
- how well the average of the measured data set represents the average of the entire population

- 4.2 Statistical Measurement Theory
  - Where does the measured data set come from?
  - Sampling refers to repeated measurements of the measured variable under fixed operating conditions.
  - We will ignore systematic error for this discussion, is this valid?
  - Instead we will focus on random error, its affects and how to quantify it.
  - Question: If the error is really random error, what is the average error?

- We want to estimate the true mean, x' from repeated measurement of x.
- The true mean, x' is the average of all possible values of x. We never actually get this!
- Through sampling we can find  $\bar{x}$ , the sample mean value of x. We do get this!
- As our sample size increases,  $\bar{x}$  approaches x'.

$$x' = \bar{x} \pm u_{\bar{x}}$$

- Therefore, the sample mean  $\bar{x}$  is the most probable estimate of the true mean x'.
- $\pm u_{\bar{x}}$  is the uncertainty interval in that estimate at some probability level, P%.
- The uncertainty interval is the range about  $\bar{x}$  that you would expect x' to lie.

### • Probability Density Functions

- The frequency with which the measured variable assumes a particular value or interval of values is described by its probability density function.
- If a central tendency exists we should be able to see this in the probability density function.
- As binsize of the histogram of the data set goes to zero this becomes the probability density function.

# • 4.2 - Describing the Behavior of a Population

The true variance is:

$$\sigma^2 = \int_{-\infty}^{\infty} (x - x')^2 p(x) dx$$

For discrete data this becomes:

$$\sigma^2 = \lim_{N \to \infty} \frac{1}{N} \sum_{i=1}^{N} (x_i - x')^2$$

The square root of the variance is the standard deviation.

$$\sigma = \sqrt{\sigma^2}$$

