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TASK 7.1P - Data analysis and interpretation

SIT225: Data Capture Technologies

Activity 7.1: Data analysis and interpretation

Data analysis is a broad term that covers a wide range of techniques that enable you to reveal any insights and relationships that may exist within raw data. As you might expect, Python lends itself readily to data analysis. Once Python has analyzed your data, you can then use your findings to make good business decisions, improve procedures, and even make informed predictions based on what you've discovered.

You have done data wrangling using Python Pandas module already in activity 5.2. In this activity, you will learn Data science statistics and linear regression models.

Hardware Required

No hardware is required.

Software Required

Python 3

Python packages including Pandas, Numpy, Scikit-learn, seaborn, plotly

Steps:

Step	Action
1	A Jupyter Notebook is provided for Data Science exploration here
	(https://github.com/deakin-deep-dreamer/sit225/tree/main/week_7). You will
	need to fill in your student ID and name and run all the cells to observe the
	output. Convert the Notebook into PDF and merge with this activity sheet
	which needs to be combined with this week's task for OnTrack submission.

Question: There are sections in the Notebook. After running the cells and observing the outputs, provide your reflection in brief on the topic items for each section of the Notebook.

Answer: <Your answer>

Basically, the file Jupyter outlines some important concepts related to Descriptive Statistics. More specifically, we have looked some concepts such as **Percentile** -relative position of a data point in a dataset, the measurements in terms of the dispersion of the data points in a dataset, namely **Standard Deviation**, **Coefficient of variation** and **Variance**. Then we examined the relationship between 2 numerical variables by studying **Correlation Coefficient** then from that we expanded the concept of the **Correlation Matrix** represented in a heatmap. Finally, using all those concepts that we have learnt we studied the use of **Linear Regression** and understood how it can applied to the real world.

Question: In the 1.1 Percentile subsection of **Descriptive statistics** section in the Notebook, you have calculated 10%, 25%, 50% and 75% percentiles for *Max_Pulse*. Compare these percentiles with *Average_Pulse* percentiles for any trend, if exists.

Answer: <Your answer>

Avg_Pulse:

```
avg_pulse = full_health_data["Average_Pulse"]
print("parcentile_10", np.percentile(avg_pulse, 10))
print("parcentile_25", np.percentile(avg_pulse, 25))
print("parcentile_50", np.percentile(avg_pulse, 50))
print("parcentile_75", np.percentile(avg_pulse, 75))
```

parcentile_10 92.2
parcentile_25 100.0
parcentile_50 105.0
parcentile_75 111.0

Max Pulse:

```
: # Get the data from the Max Pulse column

max_pulse = full_health_data["Max_Pulse"]

print("parcentile_10", np.percentile(max_pulse, 10))

print("parcentile_25", np.percentile(max_pulse, 25))

print("parcentile_50", np.percentile(max_pulse, 50))

print("parcentile_75", np.percentile(max_pulse, 75))

parcentile_10 120.0

parcentile_25 124.0

parcentile_50 131.0

parcentile_75 141.0
```

As we can see from our results it can be clearly seen that all the corresponding values of the **Max_Pulse** are much higher than the ones in **Avg_Pulse**. This is obviously natural since the **Max_Pulse** column contains just only the high peak value.

Furthermore, not only the higher values the Max_Pulse has compared to the Avg_Pulse but it also has the difference between corresponding percentiles much higher. For the percentile 10th, its difference is 27.8 which is indicatively large => slightly spread out than the Avg_Pulse

Question: In the "Correlation Does not imply Causality" section answer the question regarding the increase of ice cream sale in your own understanding.

Answer: <Your answer>

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The increase of ice cream sold **does not** imply that it will be a direct cause of increased drowning accidents. A high correlation coefficient means that two variables increase one increases and the other one will increase as well but it does not tell us why this relationship exists.

Additionally, Ince cream sold increases because more people buy ice cream to cool down due to hot weather. Besides that, drowning accidents since more people go the beach and swim so it does not imply that buying ice cream is the factor leads to drowning accidents.

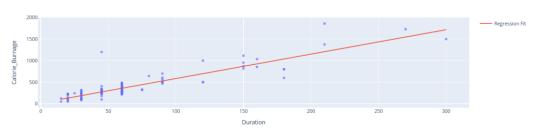
Question: In the **1.7 Linear Regression** section in the Notebook, a linear regression model was used to predict Calorie_Burnage from attributes such as Average_Pulse. The Duration value was predicted from the model for all the value range of Average_Pulse and a regression line was drawn. You will need to answer the follow up question next to 1.7 section where it is required to generate a linear regression model for Duration instead of Average_Pulse to predict the Calorie_Burnage. Take a screenshot of the regression line and paste it here. Also, comment on both the regression lines.

Answer: <Your answer>

Average_Pulse: Average_Pulse

Duration:

```
3]: # Build a regression line between the feature Duration and the predicted value Calorie_Burnage
    model = LinearRegression()
    # Get the predictor
    X = df[["Duration"]].values.reshape(-1, 1)
    # Fit the model
    model.fit(X, df["Calorie_Burnage"])
    x_range = np.linspace(X.min(), X.max(), 100)
    y_range = model.predict(x_range.reshape(-1, 1))
    fig = px.scatter(df, x='Duration', y='Calorie_Burnage', opacity=0.65)
    fig.add_traces(go.Scatter(x=x_range, y=y_range, name='Regression Fit'))
    fig.show()
```



As we can see from our generated regression lines. In terms of the Average_Pulse there is no relationship between the Average_Pulse and the Calorie_Burnage (there was a horizontal line) and we can conclude that Average_Pulse shouln't be considered as a good predictor to predict unseen output Calorie_Burnage.

On the other hand, with respect to **Duration** the regression line increased diagonally indicates a strong positive correlation between it and the output Calorie_Burnage so it is considered one of the predictors in a regression model to predict the Calorie_Burnage.

data-analysis-interpret

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1 SIT225: Data Analysis & interpretation

Run each cell to generate output and finally convert this notebook to PDF.

```
[1]: # Fill in student ID and name
#
student_id = "Truong Khang Thinh Nguyen"
student_first_last_name = "223446545"
print(student_id, student_first_last_name)
```

Truong Khang Thinh Nguyen 223446545

2 1. Descriptive Statistics

Descriptive statistics summarizes important features of a data set such as: * Count * Sum * Standard deviation * Percentile * Average

```
[2]: # Make sure necessary packages are already installed.
#!pip install pandas numpy seaborn

import pandas as pd
import numpy as np
import seaborn as sns

full_health_data = pd.read_csv("full_health_data.csv", header=0, sep=",")
print (full_health_data.describe())
```

	Duration	Average_Pulse	Max_Pulse	Calorie_Burnage	Hours_Work	\
count	163.000000	163.000000	163.000000	163.000000	163.000000	
mean	64.263804	107.723926	134.226994	382.368098	4.386503	
std	42.994520	14.625062	16.403967	274.227106	3.923772	
min	15.000000	80.000000	100.000000	50.000000	0.000000	
25%	45.000000	100.000000	124.000000	256.500000	0.000000	
50%	60.000000	105.000000	131.000000	320.000000	5.000000	
75%	60.000000	111.000000	141.000000	388.500000	8.000000	
max	300.000000	159.000000	184.000000	1860.000000	11.000000	

Hours_Sleep

```
163.000000
count
          7.680982
mean
          0.663934
std
          5.000000
min
25%
          7.500000
50%
          8.000000
75%
          8.000000
max
          12.000000
```

2.1 1.1 Percentile

2.1.1 25%, 50% and 75% - Percentiles

Observe the output of the above cell for 25%, 50% and 75% of all the columns. Let's explain for Average_Pulse: * 25% of all of the training sessions have an average pulse of 100 beats per minute or lower. If we flip the statement, it means that 75% of all of the training sessions have an average pulse of 100 beats per minute or higher. * 75% of all the training session have an average pulse of 111 or lower. If we flip the statement, it means that 25% of all of the training sessions have an average pulse of 111 beats per minute or higher.

```
[3]: avg_pulse = full_health_data["Average_Pulse"]
    print("parcentile_10", np.percentile(avg_pulse, 10))
    print("parcentile_25", np.percentile(avg_pulse, 25))
    print("parcentile_50", np.percentile(avg_pulse, 50))
    print("parcentile_75", np.percentile(avg_pulse, 75))
parcentile_10 92.2
```

parcentile_10 92.2 parcentile_25 100.0 parcentile_50 105.0 parcentile_75 111.0

2.1.2 Question: Calculate percentiles for Max Pulse.

You should answer a follow up question in the activity sheet.

```
[15]: # Get the data from the Max Pulse column
    max_pulse = full_health_data["Max_Pulse"]
    print("parcentile_10", np.percentile(max_pulse, 10))
    print("parcentile_25", np.percentile(max_pulse, 25))
    print("parcentile_50", np.percentile(max_pulse, 50))
    print("parcentile_75", np.percentile(max_pulse, 75))

parcentile_10 120.0
    parcentile_25 124.0
```

2.2 1.2 Standard Deviation

parcentile_50 131.0
parcentile_75 141.0

Standard deviation is a number that describes how spread out the observations are.

A mathematical function will have difficulties in predicting precise values, if the observations are "spread". Standard deviation is a measure of uncertainty.

A low standard deviation means that most of the numbers are close to the mean (average) value.

A high standard deviation means that the values are spread out over a wider range.

 Duration
 42.862432

 Average_Pulse
 14.580131

 Max_Pulse
 16.353571

 Calorie_Burnage
 273.384624

 Hours_Work
 3.911718

 Hours_Sleep
 0.661895

dtype: float64

2.2.1 1.2.1 Coefficient of variation

In the above cell, what does standard deviation numbers mean?

The coefficient of variation is used to get an idea of how large the standard deviation is.

Mathematically, the coefficient of variation is defined as:

Coefficient of Variation = Standard Deviation/Mean

 Duration
 0.367051

 Average_Pulse
 0.124857

 Max_Pulse
 0.140043

 Calorie_Burnage
 2.341122

 Hours_Work
 0.033498

 Hours_Sleep
 0.005668

dtype: float64

2.3 1.3 Variance

Variance is another number that indicates how spread out the values are.

In fact, if you take the square root of the variance, you get the standard deviation. Or the other way around, if you multiply the standard deviation by itself, you get the variance!

```
[6]: var = np.var(full_health_data)
print(var)
```

```
      Duration
      1837.188076

      Average_Pulse
      212.580225

      Max_Pulse
      267.439271

      Calorie_Burnage
      74739.152847

      Hours_Work
      15.301536

      Hours_Sleep
      0.438105
```

dtype: float64

2.4 1.4 Correlation

Correlation measures the relationship between two variables.

A function has a purpose to predict a value, by converting input (x) to output (f(x)). We can say also say that a function uses the relationship between two variables for prediction.

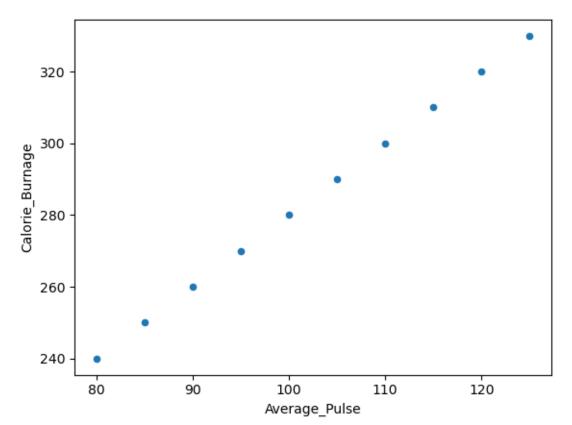
2.4.1 Correlation Coefficient

The correlation coefficient measures the relationship between two variables.

The correlation coefficient can never be less than -1 or higher than 1. * 1 = there is a perfect linear relationship between the variables * 0 = there is no linear relationship between the variables * -1 = there is a perfect negative linear relationship between the variables

Perfect Linear Relationship (Correlation Coefficient = 1) it exists a perfect linear relationship between Average_Pulse and Calorie_Burnage.

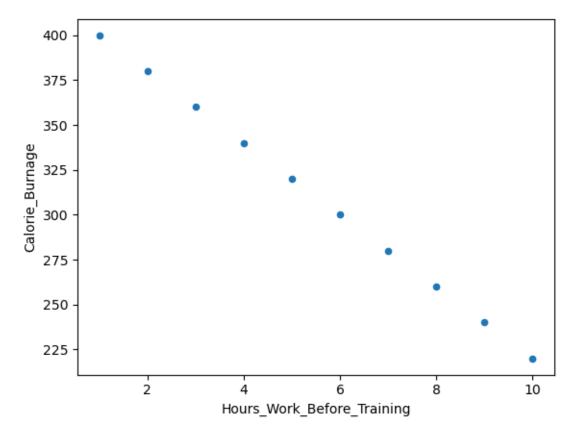
```
{'Duration':60, 'Average Pulse':95, 'Max Pulse':130,'Calorie Burnage':
 →270, 'Hours_Work':8, 'Hours_Sleep':7},
        {'Duration':60, 'Average_Pulse':100, 'Max_Pulse':140,'Calorie_Burnage':
 →280, 'Hours_Work':0, 'Hours_Sleep':7},
        {'Duration':60, 'Average_Pulse':105, 'Max_Pulse':140,'Calorie_Burnage':
 →290, 'Hours_Work':7, 'Hours_Sleep':8},
        {'Duration':60, 'Average_Pulse':110, 'Max_Pulse':145,'Calorie_Burnage':
 →300, 'Hours_Work':7, 'Hours_Sleep':8},
        {'Duration':45, 'Average Pulse':115, 'Max_Pulse':145, 'Calorie_Burnage':
 4310, 'Hours_Work':8, 'Hours_Sleep':8},
        {'Duration':60, 'Average Pulse':120, 'Max_Pulse':150, 'Calorie_Burnage':
 →320, 'Hours_Work':0, 'Hours_Sleep':8},
        {'Duration':45, 'Average_Pulse':125, 'Max_Pulse':150,'Calorie_Burnage':
 →330, 'Hours_Work':8, 'Hours_Sleep':8},
    ]
    return data
health_data = pd.DataFrame.from_dict(create_linear_health_data())
health_data.plot(x ='Average_Pulse', y='Calorie_Burnage', kind='scatter')
plt.show()
```



Perfect Negative Linear Relationship (Correlation Coefficient = -1) We have plotted fictional data here. The x-axis represents the amount of hours worked at our job before a training session. The y-axis is Calorie_Burnage.

If we work longer hours, we tend to have lower calorie burnage because we are exhausted before the training session.

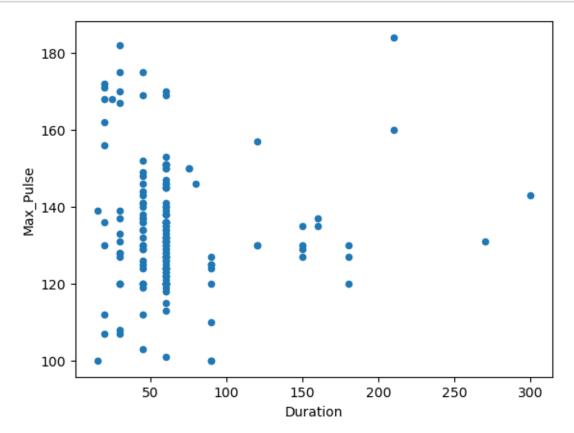
The correlation coefficient here is -1.



No Linear Relationship (Correlation coefficient = 0) As you can see, there is no linear relationship between the two variables. It means that longer training session does not lead to higher Max_Pulse.

The correlation coefficient here is 0.

```
[9]: full_health_data.plot(x ='Duration', y='Max_Pulse', kind='scatter')
plt.show()
```



2.5 1.5 Correlation Matrix

A matrix is an array of numbers arranged in rows and columns.

A correlation matrix is simply a table showing the correlation coefficients between variables.

We can use the corr() function in Python to create a correlation matrix. We also use the round() function to round the output to two decimals:

```
[10]: Corr_Matrix = round(full_health_data.corr(),2)
    print(Corr_Matrix)

# Drop 2 columns - Hours_Work and Hours_Sleep to view the matrix nice.
#
    health_part = full_health_data.drop(columns=['Hours_Work', 'Hours_Sleep'])
    Corr_Matrix = round(health_part.corr(),2)
    print(Corr_Matrix)
```

	Duration	Average_Pulse	${\tt Max_Pulse}$	Calorie_Burnage	\
Duration	1.00	-0.17	0.00	0.89	
Average_Pulse	-0.17	1.00	0.79	0.02	
Max_Pulse	0.00	0.79	1.00	0.20	
Calorie_Burnage	0.89	0.02	0.20	1.00	
Hours_Work	-0.12	-0.28	-0.27	-0.14	
Hours_Sleep	0.07	0.03	0.09	0.08	
	-	K Hours_Sleep			
Duration	-0.12	0.07			
Average_Pulse	-0.28	0.03			
Max_Pulse	-0.27	0.09			
Calorie_Burnage	-0.14	0.08			
Hours_Work	1.00	-0.14			
Hours_Sleep	-0.14	1.00			
	Duration	Average_Pulse	${\tt Max_Pulse}$	Calorie_Burnage	
Duration	1.00	-0.17	0.00	0.89	
Average_Pulse	-0.17	1.00	0.79	0.02	
Max_Pulse	0.00	0.79	1.00	0.20	
Calorie_Burnage	0.89	0.02	0.20	1.00	

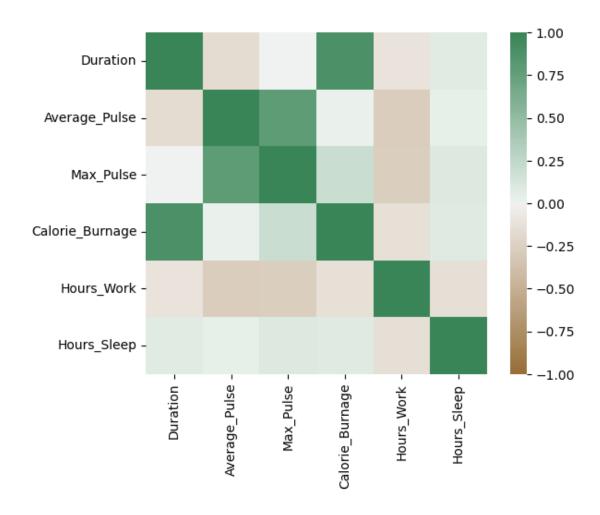
Using a Heatmap We can use a Heatmap to Visualize the Correlation Between Variables:

```
[11]: import matplotlib.pyplot as plt
import seaborn as sns

correlation_full_health = full_health_data.corr()

axis_corr = sns.heatmap(
    correlation_full_health,
    vmin=-1, vmax=1, center=0,
    cmap=sns.diverging_palette(50, 500, n=500),
    square=True
)

plt.show()
```



2.6 1.6 Correlation Does not imply Causality

Correlation measures the numerical relationship between two variables.

A high correlation coefficient (close to 1), does not mean that we can for sure conclude an actual relationship between two variables.

A classic example:

- During the summer, the sale of ice cream at a beach increases
- Simultaneously, drowning accidents also increase as well

Question: Does this mean that increase of ice cream sale is a direct cause of increased drowning accidents?

2.7 1.7 Linear Regression

The term regression is used when you try to find the relationship between variables.

In Machine Learning and in statistical modeling, that relationship is used to predict the outcome of events.

We will use Scikit-learn to train various regression models. Scikit-learn is a popular Machine Learning (ML) library that offers various tools for creating and training ML algorithms, feature engineering, data cleaning, and evaluating and testing models. It was designed to be accessible, and to work seamlessly with popular libraries like NumPy and Pandas.

We see how to apply a simple regression model for predicting Calorie_Burnage on various factors such as Average Pulse or Duration.

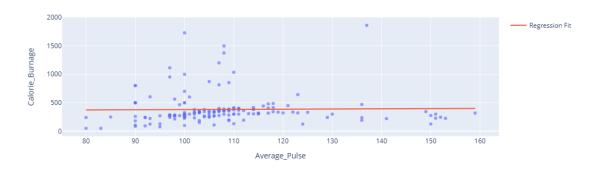
```
import numpy as np
import plotly.express as px
import plotly.graph_objects as go
from sklearn.linear_model import LinearRegression

df = full_health_data
X = df.Average_Pulse.values.reshape(-1, 1)

model = LinearRegression()
model.fit(X, df.Calorie_Burnage)

x_range = np.linspace(X.min(), X.max(), 100)
y_range = model.predict(x_range.reshape(-1, 1))

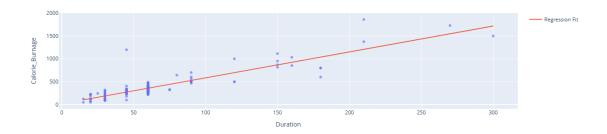
fig = px.scatter(df, x='Average_Pulse', y='Calorie_Burnage', opacity=0.65)
fig.add_traces(go.Scatter(x=x_range, y=y_range, name='Regression Fit'))
fig.show()
```



Question: We have seen earlier how to apply a simple regression model for predicting Calorie_Burnage from Average_Pulse. There might be another candidate Duration in addition to Average_Pulse. You will need to repeat the above linear regression process to find relationsthip between Calorie_Burnage and Duration.

Comment on the both regression lines: Calorie_Burnage - Average_Pulse and Calorie_Burnage -

Duration.



task-objective-7-1p

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```
[45]: import numpy as np
      import pandas as pd
      import plotly.express as px
      import plotly.graph_objects as go
      from sklearn.linear_model import LinearRegression
      from sklearn.metrics import mean_squared_error
[41]: # Load CSV file
      df = pd.read_csv("DHT22_data.csv")
                 Timestamp Humidity Temperature
[41]:
            20240722005331
                                57.9
                                57.6
      1
            20240722005341
                                             18.5
      2
            20240722005351
                                57.5
                                             18.6
      3
            20240722005401
                                58.2
                                             18.7
      4
            20240722005411
                                57.6
                                             18.7
                                             21.1
      2690 20240722082211
                                54.3
      2691 20240722082221
                                54.3
                                             21.1
                                54.2
                                             21.1
      2692 20240722082231
      2693 20240722082241
                                54.2
                                             21.1
      2694 20240722082251
                                54.4
                                             21.1
```

[2695 rows x 3 columns]

Before Removing any Outliers

```
[42]: # Create an instance Linear Regresison
#model = LinearRegression()

# Get the predictor and the output
X = df["Temperature"].values.reshape(-1,1)
y = df["Humidity"]

# Fit the model
model.fit(X,y)
```

[42]: LinearRegression()

```
[44]: # Draw a scatter plot as well as the regression line

X_regression_line = np.linspace(start = X.min() , stop = X.max() , num = 100)

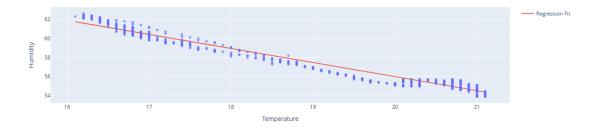
y_regression_line = model.predict(X_regression_line.reshape(-1,1))

fig = px.scatter(df, x = "Temperature" , y = "Humidity" , opacity = 0.65)

fig.add_traces(go.Scatter(x = X_regression_line , y = y_regression_line , name_

→= "Regresison Fit"))

fig.show()
```



```
[50]: # Calculate the MSE of the this model
    # Make predictions based on the original data
    y_pred = model.predict(X)

mse = mean_squared_error(y,y_pred)
    print(f"Mean Square Error of the original model: {mse}")
```

Mean Square Error of the original model: 0.18567125120983452

```
[52]: # Calculate the R^2 score of the model
print(f"R^2 score of the original model: {model.score(X,y)}")
```

R^2 score of the original model: 0.9654677620565366

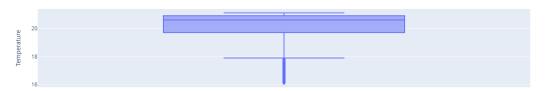
The model's performance, as indicated by a low Mean Squared Error (MSE) and a high accuracy score, suggests that it is making predictions with a good degree of precision and reliability. This strong performance implies that the original feature 'Temperature' is effectively capturing the underlying relationship between temperature and humidity. Therefore, 'Temperature' serves as a valuable predictor for 'Humidity' in the model.

Removing Outliers

```
[61]: # Create a box plot to check the distribution and outliers
fig_box = px.box(df, y = "Temperature", title = "Temperature Distribution")
```

fig_box.show()

Temperature Distribution



As observed in our generated box plot, the lower bound for our data is 17.9, which we identified using the interactive features of the plot. However, it's clear that there are several data points falling below this lower bound, indicating the presence of outliers. These outliers can perhaps skew our analysis and potentially lead to inaccurate results so we need to filter out those data points.

```
[83]: filtered_df = df[df["Temperature"] >= 17.9]
filtered_df
```

```
[83]:
                 Timestamp
                             Humidity
                                       Temperature
            20240722005331
      0
                                 57.9
                                               18.5
      1
            20240722005341
                                 57.6
                                               18.5
      2
            20240722005351
                                 57.5
                                               18.6
      3
            20240722005401
                                 58.2
                                               18.7
      4
            20240722005411
                                 57.6
                                               18.7
                                               21.1
      2690 20240722082211
                                 54.3
      2691 20240722082221
                                 54.3
                                               21.1
      2692 20240722082231
                                 54.2
                                               21.1
      2693 20240722082241
                                 54.2
                                               21.1
      2694 20240722082251
                                 54.4
                                               21.1
```

[2209 rows x 3 columns]

```
[84]: # Create a model Linear Regression model
model_filter = LinearRegression()

# Get the predictor and the output of the filter dataframe
X_filter = filtered_df["Temperature"].values.reshape(-1,1)
y_filter = filtered_df["Humidity"]

# Fit the model
model_filter.fit(X_filter,y_filter)
```

```
[84]: LinearRegression()
```

```
[86]: # Draw a s scatter plot as well as the regression line

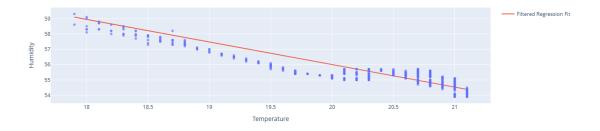
fig_filter = px.scatter(filtered_df, x = "Temperature" , y = "Humidity" ,u

opacity = 0.65)

fig_filter.add_traces(go.Scatter(x = X_regression_filter , y = u

y_regression_filter , name = "Filtered Regression Fit"))

fig_filter.show()
```



```
[87]: # Calculate the MSE of the this model
# Make predictions based on the filtered data frame
y_pred_filter = model_filter.predict(X_filter)

mse_filter= mean_squared_error(y_filter,y_pred_filter)
print(f"Mean Square Error of the filtered model: {mse_filter}")
```

Mean Square Error of the filtered model: 0.12422197252908723

 R^2 score of the filtered model: 0.7287189918274133

After filtering the data and implementing the Linear Regression model, we noticed a modest drop in Mean Squared Error (MSE), indicating a minor improvement in prediction precision. However, this increase came at a considerable cost: the model's accuracy declined from 0.965 to 0.729. This significant loss in accuracy suggests that the process of deleting outliers may have unintentionally deleted important data points from the 'Temperature' column.

Removing Outliers Completely using IQR

```
[89]: # Create a box plot to check distribution and outliers

fig_box_rm = px.box(filtered_df , y = "Temperature" , title = "Temperature

→Distribution")

fig_box_rm.show()
```

```
Temperature Distribution

21
20
19
18
```

Our generated box plot demonstrates that a single round of outlier elimination was insufficient, as the freshly generated box plot still contains many outliers. To resolve this, we will use the Interquartile Range (IQR) methodology, which is a more reliable means of detecting and deleting outliers. Following this thorough outlier removal, we'll examine the remaining data points to see if they still give a reliable factor for predicting humidity.

Additionally, since the outliers are incredibly dense so if we remove 1 or 2 times it will still contain outliers. So we need to remove and update the box plot multiple times.

```
[90]: # Function to remove outliers
def remove_outliers_iqr(df,column):
    # Calculate the Q1 (25th percentile) and Q3 (75th percentile)
Q1 = df[column].quantile(0.25)
Q3 = df[column].quantile(0.75)

# Calculate the IQR
IQR = Q3 - Q1
Lower_Bound = Q1 - 1.5 * IQR
Upper_Bound = Q3 + 1.5 * IQR
# Filter the DataFrame to include only values within the bounds
df_filtered = df[(df[column] >= Lower_Bound) & (df[column] <= Upper_Bound)]
return df_filtered</pre>
```

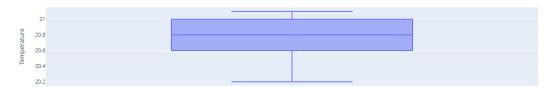
```
[92]: # Remove outliers multiple times until no outliers presented in the filtered → dataframe

# Initialize a flag
outliers_removed = True
```

```
[92]:
                Timestamp Humidity Temperature
     808
           20240722030817
                               55.0
                                            20.2
     809
                               55.1
                                            20.2
           20240722030827
          20240722030837
     810
                               55.1
                                            20.2
     811 20240722030847
                                            20.2
                               55.1
     812
           20240722030857
                               55.1
                                            20.2
     2690 20240722082211
                                            21.1
                               54.3
     2691 20240722082221
                                            21.1
                               54.3
     2692 20240722082231
                               54.2
                                            21.1
     2693 20240722082241
                               54.2
                                            21.1
     2694 20240722082251
                               54.4
                                            21.1
```

[1844 rows x 3 columns]





```
[94]: # Now proceed with the step of building the model
    # Create a model Linear Regression model
    model_filter_final = LinearRegression()

# Get the predictor and the output of the filter dataframe
X_filter_final = filtered_df["Temperature"].values.reshape(-1,1)
y_filter_final = filtered_df["Humidity"]

# Fit the model
model_filter_final.fit(X_filter,y_filter)
```

[94]: LinearRegression()

```
[95]: X_regression_rm = np.linspace(start = X_filter_final.min() , stop = X_filter_final.max() , num = 100 )
y_regression_rm = model.predict(X_regression_rm.reshape(-1,1))
```

```
[96]: # Draw a s scatter plot as well as the regression line

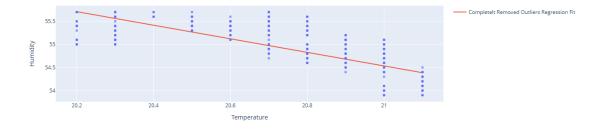
fig_filter_rm = px.scatter(filtered_df, x = "Temperature" , y = "Humidity" ,u

opacity = 0.65)

fig_filter_rm.add_traces(go.Scatter(x = X_regression_rm , y = y_regression_rm ,u

oname = "Completelt Removed Outliers Regression Fit"))

fig_filter_rm.show()
```



```
[98]: # Calculate the MSE of the this model
    # Make predictions based on the removed outliers data frame
    y_pred_rm = model_filter.predict(X_filter_final)

mse_rm= mean_squared_error(y_filter_final,y_pred_rm)
    print(f"Mean Square Error of the removed outliers model: {mse_rm}")
```

Mean Square Error of the removed outliers model: 0.09808668697882954

```
[100]: # Calculate the R^2 score of the model
```

R^2 score of the removed outliers model: 0.5180194628320673

In our final model, all data points classified as outliers have been eliminated entirely. While the Mean Squared Error (MSE) decreased little, the accuracy ratings dropped significantly.

In conclusion, despite the removal of outliers in multiple stages, the slope of the regression line remained constant, showing that the underlying relationship between the variables was consistent. This implies that, while the outliers may have added some variability, they did not substantially affect the direction or strength of the relationship reflected by the slope.

More importantly, our solution demonstrates that, while outliers can occasionally affect exploratory data analysis (EDA) and cause imbalances, they also contain essential information that is critical for model development. Removing these outliers may appear to be a good way to tidy up the data, but it can have a substantial influence on the model's performance because these points frequently capture important fluctuations in the data that are required for correct predictions. Therefore, careful thought is required when selecting whether to delete outliers, as they may contribute more to the model's accuracy than initially apparent.